# Applying Artificial Neural Networks to Business, Economics and Finance

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#### ABSTRACT

This paper surveys the significance of recent work on emulative neural networks (ENNs) by researchers across many disciplines in the light of issues of indeterminacy. Financial and economic forecasters have witnessed the recent development of a number of new forecasting models. Traditionally, popular forecasting techniques include regression analysis, time-series analysis, moving averages and smoothing methods, and numerous judgmental methods. However, all of these have the same drawback insofar as they require assumptions about the form of population distribution. Regression models, for example, assume that the underlying population is normally distributed.

ENNs are members of a family of statistical techniques, as are flexible nonlinear regression models, discriminant models, data reduction models, and nonlinear dynamic systems. They are trainable analytic tools that attempt to mimic information processing patterns in the brain. Because they do not necessarily require assumptions about population distribution, economists, mathematicians and statisticians are increasingly using ENNs for data analysis.

JEL: C3, C32, C45, C5, C63, F3, G15.

Keywords: Artificial Neural Networks, Dynamic Interrelations, Forecasting.

#### 1. INTRODUCTION

This paper surveys the significance of recent work on emulative neural networks (ENNS) by researchers across many disciplines in the light of issues of indeterminacy. Financial and economic forecasters have witnessed the recent development of a number of new forecasting models. Traditionally, popular forecasting techniques include regression analysis, time-series analysis, moving averages and smoothing methods, and numerous judgmental methods. However, all of these have the same drawback insofar as they require assumptions about the form of population distribution. Regression models, for example, assume that the underlying population is normally distributed.

ENNs are members of a family of statistical techniques, as are flexible nonlinear regression models, discriminant models, data reduction models, and nonlinear dynamic systems (Sarle, 1994; Cheng and Tetterington, 1994). They are trainable analytic tools that attempt to mimic information processing patterns in the brain (Krishnaswamy, Gilbert, Pashley, 2000). Because they do not necessarily require assumptions about population distribution, economists, mathematicians and statisticians are increasingly using ENNs for data analysis. Not only do they not require assumptions about the underlying population but are also powerful forecasting tools that draw on

the most recent developments in artificial intelligence research.

As Hardin (2002) observes in his essay, "Indeterminacy and Basic Rationality," statistical methods, such as neural networks, were developed partly as the product of the ordinal revolution in economics and choice theory. As he points out, because our choices have social and interactive contexts, it would be extremely difficult to construct a theoretical model that is capable of tracing out all of these potential and actual responses and interactions. Such models are bound to exhibit fundamental indeterminacy. These interdeterminacies are the inevitable product of strategic interactions among rational individuals who understand that their actions, or inactions, are going to be followed by reactions - those of the other participants in the strategic game and those of the environment.

In such circumstances, one may find that responses are not similar, let alone unique.

This is especially true when we add the time dimension to the discussion. A player may react in ways very different to what was presupposed in response to an unexpected reaction by one's opponent. Such models are inherently dependent upon, and sensitive to, initial conditions, which may not permit accurate predictions even for very near-future states (Brown and Chua,

1998; Smith, 1998; Stone, 1989; Bau and Shachmurove, 2002). As Domotor and Batitsky (2002) point out, a creeping amplification of error will eventually wipe out all predictive accuracy. Even the solar system, reported to be the oldest paradigm of a regular, predictable dynamical system, is unpredictable on the time scale of millions of years.

Supposing such a complex model could be constructed, once the model is subject to empirical testing, the problem of aggregation arises. Although ENNs perform well in the presence of missing data, large data sets are required to train them (Gilbert, Krishnaswamy, and Pashley, 2000). This in turn leads to Arrow's impossibility theorem because of the central difficulty with focusing on individual preferences due to the aggregation of those preferences into a general choice rule, where it may be impossible to determine an optimal allocation of resources in the face of disagreement.

For example, in the case of an election, Arrow's theorem starts with a finite set of outcomes (candidates for office), a finite set of voters and their individual preferences over outcomes. The individual preferences are an unrestricted domain, satisfying the Pareto principle, and they are independent of irrelevant alternatives (independence from other influences). Thus, Arrow's Impossibility Theorem states that it

is not possible to derive a complete and consistent social choice rule exclusively from individual preferences, except in dictatorships, which are characterized by an inability to determine the intensity of preference (Arrow, 1963; see also Hardin, 2000).

ENNS assume that we do not know that we are incapable of conceiving, designing, or constructing such a complicated interactive model of human behavior. The remaining option is to try to learn from past observations, to deduce the main patterns of future events by tracing painstakingly similar interactions found in historical data. Rather than seeking, or imposing, some determinate principle, or even attributing uniqueness to the solutions generated for the complex makings of an indeterminate world, we let historical data conveniently guide us through the indeterminable maze being confronted (see Krippendorff, 2002).

In such cases, one proceeds under the assumption that it should be more helpful to imitate the past rather than estimating the proximity of the initial conditions to their putative later effects. This is because in economics and finance, as in any human behavior, initial conditions or past observations depend on future values owing to expectations; hence, the price of a house today does not depend solely on its

price yesterday or ten years ago but also on the expectations of future demand for, and supply of, such assets in general and this house in particular.

ENNs are capable of processing data and performing calculations that humans are not adept at performing mentally. Their answers, therefore, must be accepted on faith, yet ENNs themselves are at the mercy of the sample data and the quality of their features (Weiss and Kulikowski, 1991; Hinton, 1992; Ripley, 1993; Sarle, 1994). And they process data and make forecasts much in the same way as statistical algorithms perform estimations.

In applications specific to the financial and economic fields, the main focus for ENN technology so far has been with data involving variables in non-linear relations. Granger (1991) maintains that in financial and economic data, non-linear relationships are more likely to occur than linear relationships. This claim is supported by tests such as the regression test and the neural network test, which confirms this non-linearity through the rejection of linearity and chaos where justifiable.

Consequently, new tests based on ENN systems have increased in popularity among economists. Researchers have examined the application of ENNs to financial markets, where the non-linear

properties of financial data create too many difficulties for traditional methods of analysis (see Omerod, Taylor, and Walker, 1991; Grudnitski and Osburn 1993; Altman, Marco, and Varetto 1994; Michie, Spiegelhalter and Taylor, 1994; Kaastra and Boyd 1995; and Swanson and White, 1995).

The remainder of my paper is organized as follows. Section 2 explains the background and principles behind emulative neural networks in general. Section 3 more specifically looks into the multilayer perceptron model. Section 4 discusses some of the advantages and disadvantages to using ENNS. Section 5 presents some of the recent applications of ENNs to business, economics, and finance. Section 6 concludes.

# 2. BACKGROUND AND PRINCIPLES

### A. BACKGROUND

ENNs are information processing systems whose structure and function are modeled after the cognitive processes and organizational structure of neuro-biological systems. They are a class of models developed by cognitive scientists interested in understanding the biological nervous system and simulating the computational methods of the brain.

ENNs are generally used as models for intelligence, learning, and data analysis. For data analysis, ENNs are used in numerous fields of inquiry, ranging from airport noise and

property values (Collins and Evans, 1994) to student grade point average movements (Gorr, Nagin, and Szczypula, 1994) and agricultural crop yields (Joerding, Li, and Young, 1994; Wang, 1994).

ENNs have been applied in modeling market response (Dasgupta, Dispensa, and Ghose, 1994), collective behavior (Artyushkin, 1990), telecommunication flows (Fisher and Gopal, 1994), real estate valuation (Worzala, Lenk, and Silva, 1995), and even the determinants of military expenditure (Refenes, Kollias, and Zapranis, 1995). They are also used for analyzing relations among economic and financial phenomena, forecasting, data filtration, generating time-series, and optimization (Hawley, Johnson, and Raina, 1990; Refenes, 1995; Gately, 1996; White, 1988; White 1996).

The most basic components of ENNs are highly interconnected processing elements, called neurons, which work independently in parallel (Hush and Horn, 1993; Luger and Stubblefield, 1993; Corsten and May, 1996; Jain and Mao, 1996). It is anticipated that self-organization of the neural interconnections will result in an artificial intelligence akin to human learning.

However, the intelligence and value of ENNs are still highly debated (see Chatfield, 1993; Refenes, 1994; Levine, 2000). On the one hand, neural networks are capable of

processing vast amounts of data and making extremely accurate forecasts, but on the other hand, many authors argue that despite their accurate forecasting capacities, neural networks are not intelligent in the human sense, too incapable of insightful imagination (Weiss and Kulikowski, 1991; Hinton, 1992; Ripley, 1993; Sarle, 1994; Abdi and Edelman, 1999).

Furthermore, a difference in terminology raises a barrier to communication between economists and ENNs practitioners. What economists and statisticians call independent variables are called *inputs* in the neural network literature; dependent variables are known as training values; estimated values are called *outputs*; residuals are the same as *errors*; estimation is interchangeably represented by training, learning, adaptation, and *self-organization*; the neural network counterpart to an estimation criterion is called either an error, cost, or Lyapunov function; training patterns or training pairs are observations in the statistical literature; transformations are known as functional links; interpolation and extrapolation are called generalization (Hinton, 1992; White, 1992; Sarle, 1994; Bishop, 1995; Devroye, Gyorfi and Lugosi, 1996; Ripley, 1996). In the neural network literature, training sets are commonly used in a manner that corresponds to the sample in statistics.

#### **B. PRINCIPLES**

The neuron is a basic functional element of the brain (see Paper by Gur et al. 2002). An individual neuron consists of a cell body, dendrites, and an axon. Every individual neuron receives electrical stimuli from other neurons through the dendrites, which is then amplified or de-amplified by the synapse and summated. If the sum of all stimuli is greater than the neuron's resistance threshold, provided by the cell body, then the neuron fires, producing a stimulus that passes through the axon to another neuron (Gleitman, 1991).

These synaptic connections are used to carry messages from one neuron to another. The strength of these connections varies. Neurons store information and learn meaningful patterns by strengthening their inter-connections. The synaptic process, modeled mathematically, serves as the theoretical basis for artificial neural networks.

This section demonstrates the basic structure and behavior of artificial neurons. These neurons, on their own, are very simple structures and are generally more useful when connected together as part of a larger network.

A set of inputs  $x_i$ , a set of weights  $w_i$ , a threshold, u, an activation function, f, and a signal neuron output, y, where i is the degree (number of inputs) of the neuron. The weights

represent the amplification or de-amplification of the process.

Typically, the values of the inputs,  $x_i$ , are external and are stimuli from the environment. Alternatively, they may be generated from the outputs of other artificial neurons. They can be discrete values from a set, such as  $\{0,1\}$ , or realvalued numbers.

The weights, w<sub>i</sub> are real-valued numbers that determine the contribution of each input to the neuron's weighted sum and eventually its output. The goal of neural network training algorithms is to determine the best possible set of weight values for the problem under consideration. Finding the optimal set is often a trade-off between computation time and minimizing the network error.

The threshold, u, is a real number that is subtracted from the weighted sum of the input values. Sometimes the threshold is referred to as a bias value. In this case, the real number is added to the weighted sum. For simplicity, the threshold can be regarded as another input / weight pair, where  $w_0 = u$  and  $x_0 = -1$ .

The activation function, f, can be very simple; for example, there is the unit step function (see below). However, the artificial neuron model has been expanded to include other functions such as the sigmoid, piecewise linear,

and Gaussian functions. The activation functions that are often considered are shown below.

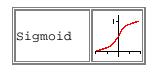
A possible representation of the Unit Step equation is:

$$f(x) = \begin{cases} 0 & \text{if } x < 0 \\ \\ 1 & \text{if } x = 0 \end{cases}$$

Unit Step	

The Sigmoid equation is:

$$f(x) = 1/(1 + e^{-\beta x})$$



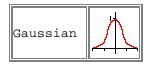
The piecewise equation is:

$$l if x = x_{max}$$



The Gaussian equation is:

$$f(x) = [1/(2?s)^{0.5}] e^{[-(x-\mu)(x-\mu)/2ss]}$$



The artificial neuron output, y, computes its output according to the equation shown below. This is the output of the activation function for the current weighted sum, less the threshold. This value can be discrete or real depending on the activation function used. Once the output has been calculated, it can be passed to another neuron (or group of neurons) or sampled by the external environment. The interpretation of the neuron output depends upon the problem under consideration. For example, in pattern classification, an output of 1 would imply the input belongs to a certain class.

 $y = f(w_1 x_1 + w_2 x_2 + w_3 x_3 + ... w_n x_n + u)$ 

 $y = f(w_0 x_0 + w_1 x_{1+} w_2 x_{2+} w_n x_n)$ 

Now, because usually learning is involved, one may want to include a learning formula for weight updating

 $W_{i}^{\text{new}} = w_{i}^{\text{old}} + k,$ 

where k is a function involving a learning constant and errors at various (input, output and hidden) layers of the network (see more below). The output of the neuron, which depends on the neuron's threshold, is a non-linear transformation of the weighted sum of its total input, usually the asymmetric sigmoid or the hard limiter (Kollias and Refenes, 1996).

## Perceptron Learning Process

This section presents a simple form of supervised learning entitled the perceptron-learning algorithm. Using this procedure, one can train the perceptron to act as a binary logic unit. We start with the simplest example of a Single-Layer Perceptron Neural Networks. A single-layer perceptron network consists of one or more artificial neurons in parallel. Each neuron in the single layer provides one network output and is usually connected to all of the external (or environmental) inputs. Figure 1 is an example of a single-neuron, single-layer perceptron network.

The perceptron-learning algorithm can be described as

follows:

- Initialize the weights and threshold to small random numbers.
- Present a vector to the neuron inputs and calculate the output.
- 3. Update the weights according to:

 $w_{i}(t+1) = w_{i}(t) + ?(d-y)x_{i}$ 

where d is the desired output, t is the iteration number, and eta is the gain or step size, where 0.0 < ? < 1.0

4. Repeat steps 2 and 3 until the iteration error is less than a user-specified error threshold or a predetermined number of iterations have been completed

Notice that learning only occurs when an error is made; otherwise, the weights are left unchanged. During training, it is often useful to measure the performance of the network as it attempts to find the optimal weight set. A common error measure or cost function used is sum-squared error. It is computed over the entire input vector / output vector pairs in the training set and is given by the equation below:

$$E = (1/2) ||y^{(1)} - d^{(1)}||^{2} + ||y^{(2)} - d^{(2)}||^{2} + ||y^{(p)} - d^{(p)}||^{2}$$

where p is the number of input/output vector pairs in the training set.

The power of neural computing comes from the threshold concept. It provides a way to transform complex interrelationships into simple yes-no situations. When the combination of several factors begins to become overly complex, the neuron model posits an intermediate yes-no node to retain simplicity.

ENNS consist of interconnected layers that contain neuron-like units called processing elements. These processing elements allow an algorithm to "learn" and eventually recognize meaningful patterns in the data. As a given algorithm learns by synthesizing more training records, the weights between its interconnected processing elements strengthen and weaken dynamically.

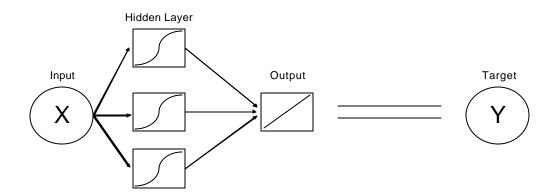
The computational structure of artificial neural networks has attractive characteristics such as graceful degradation, robust recall with noisy and fragmented data, parallel distributed processing, generalization to patterns outside of the training set, non-linear modeling, and learning (Tours, Rabelo, and Velasco, 1993). They are unique in that they learn meaningful patterns in data through inductive inference and memorization. Determinacy may play a key role here, employing

the rational choice of picking more rather than less value when given the weights of the preferences; thus, each of these processes yield determinate outcomes up to the limit of the device.

## 3. THE MULTILAYER PERCEPTRON MODEL

One of the most useful and successful applications of neural networks to data analysis is the multilayer perceptron model (MLP). Multilayer perceptron models are non-linear neural network models that can be used to approximate almost any function with a high degree of accuracy (White 1992). An MLP contains a hidden layer of neurons that uses non-linear activation functions, such as a logistic function. Figure 1 offers a representation of an MLP with one hidden layer and a single input and output. The MLP in figure 1 represents a simple non-linear regression.

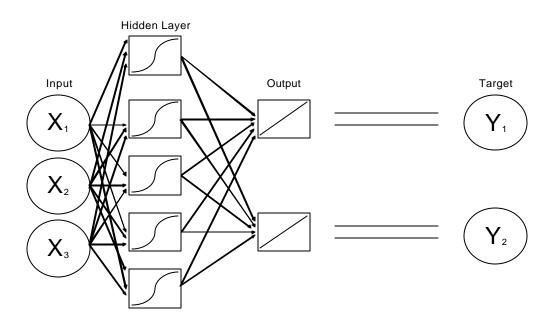
# Figure 1: Multi-layer Perceptron with a Single Input and output



The number of inputs and outputs in the MLP, as well as the

number, can be manipulated to analyze different types of data. Figure 2 presents a multilayer perceptron with multiple inputs and outputs. The MLP in figure 2 represents multivariate multiple nonlinear regression.

Figure 2: Multi-layer Perceptron with Multiple Inputs and outputs



The complexity of the MLP can be adjusted by varying the amount of hidden layers. Different amounts of hidden layers can transform an MLP from a simple parametric model to a flexible non-parametric model (White, 1992; Kuan and White, 1994; Fine, 1999; Husmeier, 1999). An MLP consisting of only one layer is very close to the projection pursuit regression model, which allows computation of explicit formulae for bias and error about the mean in orientation estimates and curve estimates.

However, the projection pursuit model uses a flexible nonlinear smoother whereas the MLP uses an already determined activation function in the hidden layer. The activation function determines the activation or the internal state of a neuron. It is applied to the weighted inputs, and it results in an output signal. As the number of hidden layers is allowed to increase, an MLP becomes a useful alternative to kernel regression analysis, a nonparametric approach that makes no assumptions regarding the functional form of the unknown function (Green, 2000), and smoothing splines. These spleens are parametrically linear, and they are quick to fit a nonlinear regression curve.

The Kernel method performs a local averaging of the observations when estimating the regression function. Analogously, one can estimate derivatives of small order of the regression function. Crucial for the kernel regression estimation is the choice of global or local bandwidths. Too small ones will lead to a wiggly curve while too large ones will smooth away important details.

Spline regressions are estimations methods that investigate both shifts of slopes and intercepts by approximating the shifts and changes in intercepts by separate linear function with dummy variables. The process is similar to estimating two or more separate regressions at once without losing degree of freedom by using linear restrictions on the estimated coefficients. If the variances differ across the different regression lines, however, one ambiguity does arise in the estimation of the disturbance variance. With a nonlinear activation function, MLP is genuinely nonlinear in the parameters and therefore takes more computer time to fit than kernels or splines (White, 1992; Eubank, 1994).

There are different uses for MLPs with more than one hidden layer. In principal component analysis, a linear model for dimensionality reduction in which inputs and targets are the same variables, one hidden layer is insufficient for improving upon principal components. A non-linear generalization of principal components can be obtained with the addition of two hidden layers, where the second layer serves as a bottleneck and the first and third layers provide the second non-linearity (Sarle, 1994).

Cascading a group of single layer neurons forms multilayerperceptron models. In a three-layer network, for example, there

is an input layer, an output layer, and a hidden layer wherever intermediate nonlinear transforms occur. The complexity of the model can be varied according to how many layers are incorporated. The nodes of different layers are densely interconnected through direct links. At the input layers, the nodes receive the values of input variables and multiply them through the network, layer by layer.

The middle layer nodes are often characterized as featuredetectors. The number of hidden layers and the number of nodes in each hidden layer can be selected arbitrarily, but too many nodes in the middle layer produce a neural network that merely memorizes the input data and lacks the ability to generalize. Most commonly, the hidden layer includes at least 75% of the number of input nodes. The initial weights of the connections can be chosen randomly. In thousands of iterations, the neural net's weights shift subtly, allowing it to learn (memorize) the patterns and recall them in the future (Baets, 1994).

The random choosing of the initial conditions generates a state of indeterminacy in terms of possible patterns or outcomes. Specifically, from an observer's perspective, the process is not observationally determinable (Krippendorff, 2002).

The computed output is compared to the known output. If

the computed output is "correct" (identical), then nothing more is necessary. If the computed output is "incorrect", then the weights are adjusted to make the computed output closer to the known output. This process is continued for a large number of cases, or time-series, until the net gives the correct output for a given input. The entire collection of cases learned is called a "training sample" (Connor, Martin, and Atlas, 1994; Anderson, 1995; Anderson and Rosenfeld, 1998; Kecman, 2001).

In most real world problems, the neural network is never 100% correct. ENNs are programmed to learn up to a given threshold of error. After the neural network learns up to the error threshold, the weight adaptation mechanism is turned off, and the net is tested on known cases it has not seen before. The application of the neural network to unseen cases gives the true error rate. In a well-trained neural network, the error threshold and the true error should be identical (Baets, 1994).

The outputs are never 100% correct. Recall that the networks themselves are not correct or incorrect; it is their outputs that are such. But networks can be analyzed for component or structural redundancy.

Although well-trained neural networks have determinate error rates, the outputs of each ENN follow the indeterminacy theory. The most likely solution is never 100% accurate; thus,

the solutions are never exactly the same. The primary cause of this is the indeterminacy of weight adjustment during the "training" process, which may differ each time for each ENN.

# 4. ADVANTAGES AND DISADVANTAGES TO USING ARTIFICIAL NEURAL NETWORKS

Econometric models as well as ENNs can be used as forecasting tools, but each tool requires a different method using different procedures, each of which offers specific advantages and disadvantages.

ENNs have many advantages over conventional methods of analysis. First, they have the ability to analyze complex patterns quickly and with a high degree of accuracy.

Second, artificial neural networks make no assumptions about the nature of the distribution of the data. They are not, therefore, biased in their analysis. Instead of making assumptions about the underlying population, ENNs with at least one middle layer use the data to develop an internal representation of the relationship between the variables. Consequently, better results can be expected with neural networks when the relationship between the variables does not fit an assumed model.

Third, since time-series data are dynamic in nature, it is necessary to have non-linear tools in order to discern

relationships among time-series (Maasoumi, Khotanzad, and Abaye, 1994). ENNs are best at discovering these types of relationships.

Fourth, neural networks perform well with missing or incomplete data. Whereas traditional regression analysis is not adaptive, indiscriminately processing older data together with new data, ENNs readjust their weights as new input data becomes available (Kuo and Reitch, 1994, Pao, 1989; Gilbert, Krishnaswamy, and Pashley, 2000). Fifth, compared with an econometric model, it is easier to use ENNs where a forecast needs to be obtained in a shorter period of time.

Since economic, financial and social systems are complex and subject to human reactions and counter-reactions by different agents or players, it is difficult, if not impossible, to write down a complete model with all the potential reactions and counter-reactions determined. Given such complexity, it is close to impossible to try to approximate in any details a model based on first principal of, for example, utility maximizations or profit maximization. In such complex systems, it is natural to turn to models, which emulate and simulate the economy or the society in question. That is exactly what the neural network methodology is capable of delivering.

Such models are difficult to understand and are

impractical to handle if one tries to control all of the possible variables and potential outcomes in the systems and account for all their dynamic interactions. This is exactly the nature of these problems, which are facing the problem of indeterminacy.

One treatment of indeterminacy involves probability and statistics; the other is the fuzziness of input and output variables and the fact that economic and finance data arrived in different time intervals are always subject to major revisions. Using the neural vocabulary, the transfer function, described in Section 2B, can often be multi-valued, and the weights and other (e.g., learning) parameters can at best be only intervalvalued. Traditional econometrics techniques are not able to handle such models due to these indeterminacies. ENNs suggest an alternative not by solving or reducing the indeterminacy but by being able nevertheless to forecast with some degree of accuracy.

However, there are some drawbacks connected with the use of ENNS. For one, ENNS are not all-purpose problem solvers. Thus far, there is no structured methodology available for choosing, developing, training, and verifying an ENN. There is no standardized paradigm for development. The output quality of ENNS may be unpredictable regardless of the design and

implementation schedule. Some researchers maintain that no estimation or prediction errors are calculable when using ENNs (Caporaletti, Dorsey, Johnson, and Powell, 1994) due to constant "learning" by the process. Also, ENNs are "black boxes," for it is impossible to figure out how relations in their hidden layers are estimated (Li, 1994, Gilbert, Krishnaswamy, and Pashley, 2000).

The difficulty in prediction from the lack of comprehension of the system's internal relations is a perfect example of observational indeterminability. The main factor in this indeterminacy is that ENNs are autopoietic systems, producing their own patterns from a set of inputs that will be needed to operate the very network of production in the future (Krippendorff, 2002).

One may claim that regression models are generally based on first principles and law of motions, which has theoretical foundations (typical in physics) whereas ENN modeling is based on emulation or simulation. The latter is much weaker from the standpoint of identification of structure and explanatory power; therefore, it is important to understand what network methodology offers and fails to offer when, e.g. compared with the traditional derivation of equations of motion for a given dynamical system, based on fundamental laws.

Another drawback is that neural networks have long training times. Excessive iterations are required to train neural networks (Gilbert, Krishnaswamy, and Pashley, 2000). Reducing training time is crucial because building a neural network forecasting system is a process of trial and error; hence, the more experiments a researcher can run in a finite period of time, the more confident he can be of the result. The network also tends to base its predictions of future events on "memories" of similar situations from the past (Ruggiero 1994). In the case of financial markets, neural nets quantify the influence of major financial variables and the impact that these relationships have on the future price movement of the target market (Gorr, 1994).

The nets learn from carefully crafted training data containing such variables as interest rates, currency prices, commodity prices, the slope of the yield curve, the movement in major commodity prices, the movement in major financial averages, internal market data, technical indicators, and so forth.

Neural networks are data-dependent, so the algorithms are only as good as the data shown to them (Meade, 1995). In this light, ENNs may be thought as weakly deterministic systems that converge to a predictable eigen-behavior (see also Krippendorff,

2002).

After the learning process, when given specific input data, it may be possible to predict a general solution that would be produced by an ENN. Since the future is often drastically different from the past in financial markets, the user needs to test the predictions on out-of-sample ranges in order to ensure the reliability of the network. The results are generally indeterministic. Kanas (2001) used out-of-sample data of monthly returns forecasts for Dow Jones and the Financial Times stock indices, using both a linear and neural network model. Neither model performed well in predicting directional changes in the two indices, but they did help to support the conclusion that the underlying relationship between stock prices is not linear (Kanas 2001).

ENNS may become a bit overzealous and undertake to fit a curve to some data even when there is no relationship. They tend to under- or over- fit data (Gilbert, Krishnaswamy, and Pashley, 2000). It is always possible to build a neural net or a mathematical function that exactly fits all the historical data such as a time series, but the predictive capability of such a system is relatively nonexistent. This over-fitting is because the noise and anomalies in the data do not allow the net to predict with any accuracy. This is also the nature of

indeterminacy in social systems we have discussed throughout this paper.

An ENN's rigor thus suffers from poor generalization capability. Enough repetitions will help to produce results with extremely high R-squared values, but they will have no relevance to reality. If a user relies on the results of an ENN in the belief that an ENN has high predictive power, a series of decisions will ensue that may prove disastrous. The user should always be aware that an ENN is not a strongly deterministic system that contains explicit cause-and-effect relationships or are based on first principals. The severity of the consequences should induce a prudent user to test one's net on a number of out-of-sample data sets in order to reaffirm the predictive power of the system (Ruggiero, 1995).

However, work with hidden layer feed forward networks is progressing towards limiting this problem (Corradi and White, 1995). In feed forward networks, the weight flows from the inputs in the forward direction, never cycling back to an input node of an output node of a previous layer. Although restricted to one direction each, the choices of the weight flows are interactive and often indeterminate within each individual network.

Problems can be reduced by using already smoothed

variables, which give the system less incentive to seek to fit its own curve to the data. It is also extremely important to use only economically significant variables for inputs. Every user will have to define what one considers being the economically significant variables. Studies show that using a few well-chosen variables will give significantly better results than trying to use every economic indicator as a viable predictor (Schwartz, 1995). Developing a successful markettiming neural network requires specialized expertise in the market model.

Studies show that networks produce the best results when used in conjunction with an expert. The expert prompts the neural network at key decision nodes, and he or she allows the user to enter his opinion as to the weight, or importance, of a specific variable. By removing highly correlated signals that have a fairly direct relationship between two inputs, the user can assess more correctly the predictive power of the inputs still present and thereby construct a better model. With such checked interaction, expert-guided networks command greater predictive power. These interactive choices present a form of indeterminacy, which results from strategic interaction, differing each time for each expert.

5. APPLICATIONS OF ENNs TO BUSINESS, ECONOMICS, AND FINANCE

Emulative neural networks are used in a widening range of applications, including airline security control, investment management and risk control (Brockett, Cooper, Golden, and Pitaktong, 1994), industrial management and production (Davies, Thomas, and Shaw, 1994; Satake, Morikawa, and Nakamura, 1994; Eberts and Habibi, 1995), as well as in forecasting stock price indexes and derivative securities (Hutchinson, Poggio, and Lo, 1994; Li, 1994; Fish, Barnes, and Milam, 1995; Shachmurove and Witkowska, 2001), and predicting exchange rates (Kuan and Liu, 1995) and thrift failures.

A typical civil engineering situation in which ENNs are utilized is vehicle discharge headway at signalized intersections. In this situation, variables include driver behaviors, vehicle characteristics, and traffic environment. A three-layered ENN was created to predict this model. When the model was trained and validated with field data, it was proven to estimate fairly accurately headway for individual vehicles better than any other headway model (Hung and Tong, 2002).

ENNs have found ardent supporters among various avant-garde portfolio managers, investment banks, and trading firms. Most of the major investment banks, such as Goldman Sachs and Morgan Stanley, have dedicated departments to the implementation of neural networks. Fidelity Investments has set up a mutual fund

whose portfolio allocation is based solely on recommendations produced by an artificial neural network. The fact that major companies in the financial industry are investing resources in emulative neural networks indicates that artificial neural networks may serve as an important method of financial forecasting in the future.

ENN processing has many managerial applications. The use of ENNs for production planning and controls (PPC) has a potential to grow significantly because more than one function of a PPC system can be supported by an ENN. Such functions include forecasting in the framework of master production scheduling and consumption-driven material requirement planning; determination of lot sizes for production and procurement; capacity adjustment; scheduling; and short-term intervention into running processes (Corsten and May, 1996).

Yoon and Swales (1990) compare ENNS to discriminant analysis. The technique of discriminant analysis is generally used to build a procedure that not only consider the number of correct and incorrect classifications of the data but also takes into account the cost of each type of classification. Yoon and Swales (1990) show that the prediction of stock price performance based on an ENN model is superior to prediction based on a discriminant analysis.

Surkan and Singleton (1990) find that ENNs models perform better than discriminant analysis also in predicting future assignments of ratings to bonds. This may lead to an inaccurate assumption of determinacy, where - given a set of initial conditions - it may be presupposed that future prices of stocks and bonds may be predicted. However, the actual values (or ENN outcomes) fluctuate unpredictably, indicating a noticeable behavior of indeterminacy.

Trippi and DeSieno (1992) apply an ENN system to the modeling of trades in Standard and Poor's 500 index futures. They find that the dynamics of the ENN system helps to outperform a passive approach to investment (a buy-and-hold strategy) in the index; thus, they favor the implementation of ENNs to the financial decision making process.

Donaldson, Kamstra, and Kim (1993) contribute to the study of the capital asset pricing model as well as ENNs by examining the fat tails and heteroskedasticity in stock return data. Using data from the stock indexes of London, New York, Tokyo, and Toronto, they find that ENN models outperformed many traditional models, including the autoregressive conditioned heteroskedasticity (ARCH) model, in removing leptokurtosis and symmetric and asymmetric heteroskedasticity from the stock index data. This superior capability allows the ENN model to be

utilized (perhaps a little too confidently) as a deterministic tool.

A balanced assessment of the potential of ENNs is offered by Hill, Marquez, O'Connor, and Remus (1994). They find emulative neural networks to be comparable to traditional statistical methods. In regard to the forecasting potential of artificial neural networks, they find that such networks perform as well as classical statistical models for forecasting yearly time-series, but that for monthly and quarterly time-series, ENNs may actually outperform statistical models. ENNs do not necessarily outperform regression in modeling human decisionmaking, except when non-linear elements are involved. This is not a case of explicit determinacy as it is more likely an indication of a weakly deterministic system.

Kuo and Reitsch (1996) test the accuracy of forecasts produced by both multiple regression and neural network models. They test their models on ten different out-of-sample data sets and analyze the forecasting errors of each of the models. The results indicate that ENNs outperform conventional methods in all cases.

### 6. CONCLUSION

The technology of ENNs has existed theoretically for decades. However, the explosion in computational processing

power in the last ten years has revived research using such nets. Developing even a simple ENN requires millions of calculations. The shift from expensive to affordable computer processing power has fueled the growth in neural network research (Perry, 1994). ENNs are revolutionizing statistical computing in many fields as they not only "learn" autonomously, but they also are ideal for noticing non-linear relationships in data (Rummelhart and McClellend, 1986; Wasserman, 1989; Maren, Harston and Pap, 1990; Hoptroff, 1993). A perfect example of an autopoietic system, an ENN is the best available tool today for analyzing and even forecasting indeterministic data.

ENN models are becoming highly desirable statistical tools for statisticians and economists who, having internalize the hallmark of rational expectations, now firmly believe that people react to one another and to policy rules in strategic and dynamic ways. The construction of an explicitly detailed dynamic model, however, is extremely difficult, for such a model must be capable of tracing all of the potential and actual responses and interactions. Thus, models are bound to exhibit indeterminacy in the sense that it may be impossible to develop a unique solution for a given situation.

This fuzziness of input and output variables and of possible multi-valued transfer function, where the weights and

other (e.g., learning) parameters can at best be only intervalvalued, is at the basis of such indeterminacy. A model's optimal performance will result in an approximation of a solution or of a most likely outcome, which is the inevitable product of strategic interactions among variables and/or rational individuals.

The ability to deal with many processing elements makes neural computing faster than conventional computing. In addition, parallelity makes it robust and fault-tolerant in the sense that performance does not degrade significantly even if one of the nodes fails. Researchers are concluding that most economic and financial problems are non-linear; that simple cause-and-effect relationships rarely exist; that, instead, most problems encountered are fuzzy patterns, which relate to multiple variables.

Nonetheless, as many have argued (see, for example Sarle, 1994), statistics and ENNs are not competing methodologies for data analysis. Rather, the paths of statistics and ENNs often cross. There are many useful neural network models for nonlinear data analysis, such as the MLP model, and there is room for many more applications of statistics to neural networks, especially in regard to estimation criteria, optimization algorithms, confidence intervals, diagnostics, and

graphical methods (Sarle, 1994).

As they do not require an exact specification of the functional equations, emulative neural systems can be applied to predict economic phenomena - especially unrecognized, unstructured, and non-stationary processes. Thus, ENNs are highly suitable for analyzing economic systems. ENNs have proven themselves to be adequate also for searching out and identifying non-linear relationships and for pinpointing those variables that hold the highest predictive value. After extensive training, ENNs are able to eliminate substantial amounts of ambiguity in economic forecasts, although never completely overcoming indeterminacy.

The unique qualities and enormous potential of this technology assure it a leading place in the search for a better and more diversified forecasting technique and method of computer power increases, processing time analysis. As decreases, and personal computers become more and more available, the use of emulative neural networks will continue to increase. Specifically, they will be utilized as analytical tools in attempt to resolve residual questions an of indeterminacy that are likely to continue to befuddle humanity for quite some time to come.

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