## University of Calgary

# Natural Gas Processing Principles and Technology - Part I 

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## Purpose of this Document

1. To study the physical, chemical and engineering principles used in the handling of natural gas, substitute natural gas, their associated liquids, and the other compounds obtained from them.
2. To apply these principles to actual design and operating problems.

## Preface

The gas processing industry in the past 25 years has developed extensively. Many different qualities of gas have been discovered and are being processed. Many different processing schemes are used to accomplish the same ends. This book tries to outline the major ways that this is being done, and to make the reader aware of the main areas of technology that are considered in gas processing and handling.
This book is intended for practising engineers of all disciplines as a guide for them in the gas processing industry as gas engineers come from all branches of engineering.
At the end of most chapters, typical problems that might be encountered in industry are given. As these are practical problems, more than the principles of the particular chapter have to be used to solve the problems.
The Gas Processors Suppliers Association Engineering Data Book ${ }^{1}$ has been referred to extensively for data and other material as it is the basic reference book for the industry.

This book has been developed from the lecture notes developed by the author for a course given by him at the University of Calgary in the Department of Chemical Engineering over the past 24 years, and at other centres in both North America and Europe. During that period, several people have lectured in various sections of the course and have helped in the preparation of the text. These are, with the address when they participated in the course or their present address are as follows:

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Also, as the notes are based on the author's more than 30 years in the gas processing industry, he wishes to acknowledge the many persons not already acknowledged who contributed data and suggestions incorporate in the book.

The more recent revisions have been made to bring the notes up-to-date and to show both metric units and English units whenever appropriate. The problem of using metric units is that the source of much of the data is the 9th edition of GPSA Metric Data book, which is based on 1972 data. There is now available a 10th edition of this book which was published in 1987 that gives English units only. This is a much more complete reference book and as such will be used extensively in class.

### 1.0 Introduction

- Course objective, definition of terms, summary of Different fields touched on, etc.
- Typical gas analysis.
- Pipeline gas specifications and by-product specifications.
- The chemical composition of natural gas and the effect of these chemicals.
- Typical definitions used in natural gas processing.
- Simplified flow scheme of handling natural gas.


### 1.1 Natural Gas

Natural gas is defined as gas obtained from a natural underground reservoir. It generally contains a large quantity of methane along with heavier hydrocarbons such as ethane, propane, isobutane, normal butane, etc. Also, in the raw state it often contains a considerable amount of nonhydrocarbons, such as nitrogen, hydrogen suiphide and carbon dioxide. There are some traces of such compounds as helium, carbonyl sulphide and various $n \sim r c a p t a n s$. It is also generally saturated with water. Table 1.1 below gives some examples of the analysis of various types of gas.

Table 1.1: Typical Raw Gas Composition

| Geological Era | Mesozoic (Baldonnel) <br> Mole \% | Paleozoic (Kaybob South) <br> Mole \% | Solution Gas <br> Mole \% |
| :--- | :---: | :---: | :---: |
| $\mathrm{N}_{2}$ | 0.32 | 0.94 | 2.45 |
| $\mathrm{H}_{2} \mathbf{S}$ | 4.37 | 17.89 | 0.00 |
| $\mathrm{CO}_{2}$ | 2.41 | 3.49 | 0.11 |
| Methane | 85.34 | 56.53 | 91.94 |
| Ethane | 4.50 | 7.69 | 13.85 |
| Propane | 1.50 | 3.38 | 7.30 |
| Isobutane | 0.25 | 0.87 | 1.06 |
| n-Butane | 0.48 | 1.73 | 2.15 |
| Isopentane | 0.15 | 0.71 | 0.36 |
| n-Pentane | 0.21 | 0.76 | 0.48 |
| Hexane | $0.47+$ | 1.48 | 0.18 |
| Heptane plus | - | 4.53 | 0.12 |

### 1.2 Why Process Natural Gas?

Gas that is sold for commercial use is quite different in composition to the gas given in Table 1.1. A typical composition of a gas that is sold directly as an industrial fuel is given in Table 1.2.

## Table 1.2: Typical Pipeline Gas Composition

[^1]|  | From a Field Plant Mole \% | From a Straddle Plant Mole \% |
| :--- | :---: | :---: |
| $\mathbf{N}_{2}$ | 0.30 | 0.35 |
| $\mathrm{C}_{1}$ | 91.63 | 98.60 |
| $\mathrm{C}_{2}$ | 5.72 | 1.05 |
| $\mathrm{C}_{3}$ | 1.63 | - |
| $\mathrm{iC}_{4}$ | 0.29 | - |
| $\mathrm{nC}_{4}$ | 0.31 | - |
| $\mathbf{i C}_{5}$ | 0.12 |  |

The gas that is sold is not specified by chemical composition, but rather by a series of specific properties that have to be met. These are given in Table 1.3 and Table 1.4. To change the raw gas in the reservoir, which is at pressures from $600 \mathrm{psig}(4000 \mathrm{kPa})$ or lower to $5000 \mathrm{psig}(35000 \mathrm{kPa})$ or higher and is generally saturated with water vapour, to a gas of the composition of Table 1.2 it can be seen that the gases of the compositions given in Table 1.1 will need considerable processing.

All the acid gas compounds, $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{CO}_{2}$, must be removed, and if it is economical, or required for environmental reasons the $\mathrm{H}_{2} \mathrm{~S}$ should be converted to elemental sulphur. Also, all the free liquids, both hydrocarbon and water, have to be removed. In fact, generally all the hydrocarbons heavier than pentanes are removed as well as considerable amounts of propane and butane. The removal of these compounds requires an understanding of the laws of fluid flow, distillation, heat transfer, etc. These subjects, along with others, will be discussed later in the book.

### 1.3 Chemical Composition of Natural Gas

Natural gas is a complex mixture of hydrocarbon and non-hydrocarbon constituents and exists as a gas under atmospheric conditions. Virtually hundreds of different compounds may be present in natural gas in varying amounts. Even two wells producing from the same reservoir may produce gases of different composition as the reservoir is depleted.
The complex nature of natural gas is exemplified by the American Petroleum Institute's Research Project 6 , which determined the individual constituents of a naturally occurring petroleum hydrocarbon mixture. Using a sample of Ponca City Field petroleum, this project isolated 172 compounds. Natural gases may have a similar complexity. Fortunately, however, the major components in most natural gases are paraffin hydrocarbons with smaller amounts - usually only traces - of olefin hydrocarbons, naphthenic hydrocarbons, mercaptans, and non-hydrocarbon compounds.
The components of natural gas are either aliphatic (chain) or cyclic (ring) hydrocarbons. Their structures are as follows.

## Aliphatic or Chain Hydrocarbons

Aliphatic hydrocarbons occur in two forms: paraffin hydrocarbons and olefin hydrocarbons. The most common are saturated hydrocarbons.

- $\mathrm{CH}_{4}$ - Methane (predominant)
- $\mathrm{C}_{2} \mathrm{H}_{6}$ - Ethane
- $\mathrm{C}_{3} \mathrm{H}_{8}$ - Propane
- $\mathrm{C}_{4} \mathrm{H}_{10}$ - Butane
- $\mathrm{C}_{5} \mathrm{H}_{12}$ - Pentane
- $\mathrm{C}_{6} \mathrm{H}_{14}$ - Hexane
- $\quad \mathrm{C}_{7} \mathrm{H}_{16}$ - Heptane

The structural formula for methane is


## Isomers

Isomers are compounds having the same composition and molecular weight but different properties due to a different structural arrangement. The structural formulae for butane isomers are as follows:


Normal butane
Isobutane

## Olefin hydrocarbons

Olefin hydrocarbons have the general formula of $\mathrm{C}_{n} \mathrm{H}_{2 n}$ and are classed as unsaturated hydrocarbons. They usually occur only in traces.
$\mathrm{C}_{2} \mathrm{H}_{4}$ - Ethene
$\mathrm{C}_{3} \mathrm{H}_{6}$ - Propene
$\mathrm{C}_{4} \mathrm{H}_{8}$ - Butene
The structural formula for butene is


## Cyclic or Ring Hydrocarbons

Cyclic hydrocarbons also occur in traces most of the time. They are of two kinds: naphthenic, and aromatic, hydrocarbons. For simplicity, only the ring structures will be shown.

## Naphthenic hydrocarbons

Naphthenic hydrocarbons are saturated cyclic hydrocarbons with the general formula of $\mathrm{C}_{n} \mathrm{H}_{2 n}$


Cyclopropane


Cyclobutane


Cyclopentane


Cyclohexane

## Aromatic hydrocarbons

Aromatic hydrocarbons are unsaturated cyclic hydrocarbons classified by the number of sixcarbon rings in the molecule. The structures of benzene, toluene, and ethyl benzene are as follows:


Benzene
Toluene (Methyl benzene) Ethyl benzene
Structures of more complex aromatics such as xylenes in which two or more methyl groups or side chains are attached to the benzene ring are shown below:



Metaxylene


Paraxylene

## Nonhydrocarbon Components

Some non-hydrocarbon components of natural gas are as follows:

| Nitrogen | $\mathrm{N}_{2}$ |
| :--- | :--- |
| Carbon dioxide | $\mathrm{CO}_{2}$ |
| Hydrogen sulfide | $\mathrm{H}_{2} \mathrm{~S}$ |
| Helium | He |
| Water vapor | $\mathrm{H}_{2} \mathrm{O}$ |

Carbonyl sulfide COS

Carbon disulfide $\quad \mathrm{CS}_{2}$
Sulfur S
Mercaptans *RSH
Note: R represents an alkyl group

## Methyl Mercaptan and Ethyl Mercaptan

Methyl mercaptan and ethyl mercaptan are the two mercaptan compounds most commonly found in natural gas. Their structures are as follows:



Methyl mercaptan

## Ethyl mercaptan

The effect of the various compounds on natural gas will now be discussed.

## Nitrogen ( $\mathrm{N}_{2}$ )

This compound is quite inert and does not contribute to the gas in any way. It should be noted that gases with high $\mathrm{N}_{2}$ content often have high helium content.

## Hydrogen Sulphide $\left(\mathrm{H}_{2} \mathrm{~S}\right)$

This compound is the cause of the sourness in natural gas. It is one of the most dangerous of industrial gases. For example, if a person is exposed to a concentration of $0.06 \%$ in air for two minutes, it will probably result in his death. Thus, $\mathrm{H}_{2} \mathrm{~S}$ has to be removed from the raw gas. This is done primarily by the process of sweetening. The $\mathrm{H}_{2} \mathrm{~S}$ content of gas is reduced to less than either 0.25 (. 4 ppm ) or 1 grain ( 16 ppm ) per 100 CF of gas, depending on the pipeline the gas is being sold to. Thus, 1 grain pipeline gas contains less than $0.0016 \% \mathrm{H}_{2} \mathrm{~S}$. The actual metric specifications are $6 \mathrm{mg} / \mathrm{in}$ or $23 \mathrm{mg} / \mathrm{m}^{3}$

## Carbon Dioxide ( $\mathrm{CO}_{2}$ )

This compound is an acid gas like $\mathrm{H}_{2} \mathrm{~S}$, but it is not nearly so undesirable. It does not support combustion and thus does not contribute to the gas. The normal maximum acceptable concentration in pipeline gas is $2 \%$. Often gases of higher contents are accepted from small fields as it does not pay to remove the $\mathrm{CO}_{2}$ if only it is present. The sweetening process also is used for the removal of $\mathrm{CO}_{2}$

## Carbonyl Sulphide (COS)

This is a compound that often appears in raw gases with high concentration of $\mathrm{H}_{2} \mathrm{~S}$ in them. It is generally reported in grains per 100 CF (or in ppm or $\mathrm{mg} / \mathrm{m}^{3}$ ). It has the undesirable property of forming nonregenerable compounds with one of the most commonly used sweetening agents, monoethanol amine. This causes increased chemical consumption of this agent. Other sweetening agents such as "diethanol amine", "sulphinol", etc., can be used to absorb it. The COS is generally broken down in the regeneration step with these agents.

[^2]
## Methane ( $\mathrm{CH}_{4}$ or $\mathrm{C}_{1}$ )

This is the prime compound in natural gas.

## Ethane ( $\mathrm{C}_{2} \mathrm{H}_{6}$ or $\mathrm{C}_{2}$ )

This compound occurs as the second largest component of all natural gases. It has a considerably higher gross heating value than methane (1769 BTU's/SCF versus 1010 BTU's/SCF 33 of gas or 66.0 MJ/m versus $37.7 \mathrm{MJ} / \mathrm{m}$ ).

## Propane ( $\mathrm{C}_{3} \mathrm{H}_{8}$ or $\mathrm{C}_{3}$ )

This compound is a significant part of pipeline gas. However, if there is much present in the raw gas, say $2.0 \%$ or greater, then it is generally more economical to absorb it and recover it as a liquid and sell it as a liquid fuel.

## Isobutane ( $\mathrm{iC}_{1}, \sim \mathrm{H}_{10}$ or $\mathrm{iC}_{4}$ )

This compound is normally extracted as liquid. It is used as a component in the manufacture of high octane gasoline (alkylate).

## n Butane ( $\mathrm{nC}_{4} \mathrm{H}_{10}$ or $\mathrm{nC}_{4}$ )

This compound is normally extracted as a liquid. It is generally used as a blending agent in motor gasoline.

## Pentanes and Heavier ( $\mathrm{C}_{5} \mathrm{H}_{12}$ or $\mathrm{C}_{5}$ or heavier)

These compounds appear in pipeline gas only in small quantities. They are mostly in the form of liquids when entering the processing plant. They are separated and are the primary compound in condensate.

## Mercaptans $\left(\mathrm{CH}_{3} \mathrm{SH}\right.$ - methyl mercaptan or $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{SH}$ - ethyl mercaptan)

These are very foul smelling compounds that, in very small quantities can be used as gas odorants, but in larger quantities make the gas offensive to certain consuming areas.

### 1.4 Further Discussions on Pipeline Gas Specifications

Table 1.3 lists the various specifications used for gas purchased in Western Canada. In the previous section, the reasons for some of the specifications are given. However, a review of the other is necessary.

## Table 1.3: Typical Pipeline Gas Specifications

| Specification <br> Item | Trans Canada |  <br> Southern | Westcoest For <br> US Use | Westcoast For <br> BC Use | Canadian - <br> Western |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Minimum <br> Heating Value <br> Btu/SCF | 950 | 975 | 1000 | 1000 | 950 |
| Hydrocarbon <br> Dewpoint, $F$ | 15 @ 800 <br> psia | 15 @ 800 <br> psia | Free of <br> Liquids | Free of <br> Liquids. | 15 @ 500 psia |
| Water Content | 4 | 4 | 4 | 4 | Equivalent to |


| Lb/MMSCF |  |  |  |  | dewpoint |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Hydrogen <br> Sulphide <br> Grains per 100 <br> CF | 1 | 0.25 | 0.25 | 1 | 1 |
| Mercaptans <br> Grains per 100 <br> CF | No spec | 0.20 | 5.0 | No spec | No spec |
| Total Sulphur <br> Grains per 100 <br> CF | 20 | 1.0 | 20 | 20 | 10 |
| Carbon <br> Dioxide, <br> mole\% | 2 | 2 | No spec | No spec |  |
| Oxygen <br> Content, mole <br> \% | No spec | 0.4 | 0.2 | No spec |  |
| Delivery <br> Temperature, <br> F | 120 | 120 | No spec. | No spec | 120 |
| Delivery <br> Pressure, psig <br> max. | 900 | 900 | varies | varies | 500 |

## Table 1.4: General Metric Specifications

| Specification Minimum | Traditional Value | Rationalized SI Specifications |
| :--- | :--- | :--- |
| Heating Value | 950 BTU 's/scf | $34.5 \mathrm{MJ} / \mathrm{m}^{3}$ |
| Hydrocarbon Dew Point | $15^{\circ} \mathrm{F}$ at 800 psia | $-10^{\circ} \mathrm{C}$ at 5500 kPa |
| Water Content | $4 \mathrm{lbs} / \mathrm{MMSCF}$ | $65 \mathrm{mg} / \mathrm{m}^{3}$ |
| $\mathrm{H}_{2}$ S Content | $1 / 4$ grain $/ 100 \mathrm{CF}$ | $6 \mathrm{mg} / \mathrm{m}^{3}$ |
| Total Sulfur Content | 1 grain $/ 100 \mathrm{CF}$ | $23 \mathrm{mg} / \mathrm{m}^{3}$ |

### 1.4.1 Special specifications

Wobbe No. $=\frac{\text { Gross HeavyValue in BTU } / \text { SCF }}{\sqrt{\text { Specific Gravity }}}$
This is a measure of the burning qualities of the gas. Gases mixed together should have Wobbe number within $10 \%$.

## Heating Value

This is necessary so that the consumer can properly set his firing equipment. Most pipeline companies give a bonus for increased BTU content above 1000/SCF (on gross basis as explained in Chapter 2).

## Hydrocarbon Dewpoint

[^3]This specification is necessary to prevent the condensation of liquid hydrocarbons in pipelines transmitting gas to markets or in the lines feeding consumers. When a deep cut extraction plant straddles a pipeline some distance down the line, this specification is not too important as long as free liquids do not form and remain in the transmission lines.

## Water Content

This specification is necessary to prevent condensation of liquid water in the pipelines as the presence of free water is conducive to the formation of hydrates. The specification of 14 lbs of water/MMSCF is equivalent to a dew point of $+18^{\circ} \mathrm{F}\left(-9^{\circ} \mathrm{C}\right)$. As the lowest buried pipeline temperature that has been measured in operating conditions is $+25^{\circ} \mathrm{F} \mathrm{C} \sim 14^{\circ} \mathrm{C}$ ) this specification gives a reasonable degree of safety.

## $\mathrm{H}_{2} \mathrm{~S}$ Content

This specification is explained in the previous section.

## Mercaptan Content

This specification is explained in the previous section. It is particularly applicable for gas going to California as the customers there are used to very sweet smelling gas.

## Total Sulphur

This specification is also set for the same reason as the mercaptan specification; that is, to control the foul smelling compounds. These can be, besides mercaptans, thiophenes and disulphides. Also, sulphur compounds can be a catalyst poison in some reactions involving natural gas.

## $\mathrm{CO}_{2}$ Content

This was discussed in the previous section.

## $\mathrm{O}_{2}$ Content

This is not an important specification as 0 is not normally present. It is a hold-over from manufactured gas specifications.

## Delivery Temperature

This is set, sometimes, to have consistent metering and also to protect pipeline coatings.

## Delivery Pressure

This is set so that the pipeline company can properly design their system. The higher, the better for the pipeline company.

### 1.5 Definitions

Please also see GPA Publication 1167 _77 "Glossary Definition of Words and Terms Used in the Gas Processing Industry". This is now included in Chapter 1 of the English Unit version of the GPSA Engineering Data Book.
It is desirable to define several of the terms that will be used in the book. Some of the main ones are as follows:

Pipeline gas or Residue Gas or Sales Gas

Sour Gas
Sweet Gas'
Wet Gas
Dry Gas
g.p.m. for a gas

Rich Gas

Lean Gas

Pentanes +
Condensates

Natural gasoline

Lean Oil
Rich Oil
Lean Solution
Rich Solution

Gas that has the quality to be used as a domestic or industrial fuel. It meets the specifications set by a pipeline transmission company, and/or a distributing company
Gas that contains more than 1 grain of $\mathrm{H}_{2} \mathrm{~S} / 100 \mathrm{SCF}$. Generally much more than this.
Gas in which the hydrogen sulphide content is less than 1 grain per 100 SCF.
Gas that contains more than 0.1 gallons (u.s.) of condensate per 1000 CF of gas.
Gas that contains less than 0.1 gallons of condensate per 1000 CF of gas.
Gallons of liquid per 1000 CF of gas. This can be US or Imperial Gallons.
Gas containing a lot of compounds heavier than ethane, about 0.7 US gallons of $\mathrm{C}_{3}+$ per 1000 CF of feed to an absorption unit.
Gas containing very little propane and heavier - or the effluent gas from an absorption unit.

The pentane and heavier fraction of hydrocarbon liquid.
The hydrocarbon liquid fraction obtained from a gas stream containing essentially pentanes.
A specification product of a certain vapour pressure. See GPSA data book for the various grades.
Absorption oil sent to an absorber.
Absorption oil containing absorber material. The effluent from an absorber.
A stripped sweetening solution.
A sweetening solution containing absorbed acid gases.

### 1.6 Calculations Involving Gas Composition

Often it is desirable to calculate certain figures regarding raw gas based on its chemical compositions. For example, let us calculate the long tons of sulphur/MMSCF, the pentanes+ BBIs/MMSCF and propane+ in US gallons per MSCF for the gas given in Table 1.6

The pentanes plus content is determined by finding the US Gallons per 1000 CF from the table (sum of $\mathrm{iC}_{5}, \mathrm{nC}_{5}, \mathrm{C}_{6}+$ ) and multiplying by 1000 and converting to BBIs:

$$
\frac{0.413(1000)}{42}=\frac{9.8 B B l s}{M M S C F}
$$

Table 1.5: Gas Composition

| Comp. | Mole \% | US Gallon per mole | US Gallon per 1000 CF |
| :--- | :---: | :---: | :---: |
| $\mathrm{N}_{2}$ | 0.69 | 4.16 | -- |
| $\mathrm{H}_{2} \mathrm{~S}$ | 6.14 | 5.17 | -- |
| $\mathrm{CO}_{2}$ | 1.00 | 6.38 | -- |
| $\mathrm{C}_{1}$ | 82.15 | 6.40 | -- |
| $\mathrm{C}_{2}$ | 6.30 | 10.12 | -- |
| $\mathrm{C}_{3}$ | 1.84 | 10.42 | 0.504 |
| $\mathrm{iC}_{4}$ | 0.38 | 12.38 | 0.124 |
| $\mathrm{nC}_{4}$ | 0.50 | 11.93 | 0.156 |
| $\mathrm{iC}_{5}$ | 0.30 | 13.85 | 0.110 |


| $\mathrm{nC}_{5}$ | 0.20 | 13.71 | 0.072 |
| :--- | :--- | :--- | :--- |
| ${ }^{*} \mathrm{C}_{6+}$ | 0.50 | 17.46 | 0.231 |
|  |  |  | Total |

* Assume to have properties of $\mathrm{nC}_{7}$

The propane ${ }^{+}$content of the gas as is shown in the Table is 1.197 gallons per 1000 CF. The calculation of propane content alone is as follows:

$$
=\frac{1.84}{100}\left(\frac{1000}{379}\right)(10.42)=0.54 \frac{\text { US Gallons }}{1000 C F}
$$

The sulphur content is found as follows:

$$
\frac{1.84}{100} \frac{10^{6}}{379} \frac{32}{2240}=\frac{2.32 L T}{M M S C F}
$$

The equivalent metric calculation is shown below.
For propane find the $\mathrm{m}^{3}$ of $\mathrm{C}_{3}$ liquid per $1000 \mathrm{~m}^{3}$ of gas

$$
\frac{1.84}{100} \frac{1000}{23.6} \frac{0.08684}{1000}=0.06770 \quad \text { cu.m. }
$$

(for liquid propane) thus must be divided by 1000 to get to moles. For sulphur content in tonnes $(1000 \mathrm{~kg}) / 1000 \mathrm{~m}$ of gas

$$
\frac{6.14}{100} \frac{1000}{0.0236} \frac{32}{1000}=0.08325
$$

### 1.7 By-Products from Natural Gas

The by-products that are recovered from processing natural gas are generally propane, mixed butanes (sometimes this is split into iso and normal butane), condensate or pentanes plus, and sulphur.
Propane and Butanes: The use of propane and butanes were given in a previous section. The primary specifications for propane and butane are given in Tables 1.7 and 1.8.

Table 1.6: LPG Specifications ${ }^{\nabla}$

| Item | Propane | Butane |
| :--- | :--- | :--- |
| Vapor Press. Max, psig at 100 F | 208 | 70 |
| Residue or butane content \% | 2 | Not a spec. |
| $95 \%$ boiling point | Not a significant spec. | $34^{\circ} \mathrm{F}$ |

[^4]| Volatile suphur grains/IO0 CF | 15.0 | 15.0 |
| :--- | :--- | :--- |
| Dryness | by valve freeze test. | No free moisture. |
| Corrosive Compounds | Free from (\#1 by copper strip) | Free from (\#1 by copper strip) |

"Valve Freeze" method of ASTM (Test D2713-81)
Table 1.7: LPG Specifications Metric Equivalents

| Item | Propane | Butane |
| :--- | :--- | :--- |
| Vapour Press. Max kPa gauge at $37.8^{\circ} \mathrm{C}$ | 1434 | 483 |
| $95 \% \mathrm{BP}$ | -- | $2.2^{\circ} \mathrm{C}$ |
| Volatile sulphur $\mathrm{mg} / \mathrm{m}^{3}(15$ grains $)$ | 343 | 343 |
| Volatile sulphur $\mathrm{mg} / \mathrm{m}^{3}(10$ grains $)$ | 229 | 229 |

In the HD-5 specification for propane, additional restrictions such as 10 grains of sulphur/100 CF, $5 \%$ maximum propylene (C3H6), $90 \%$ minimum C3 are added. In the winter time Canadian companies often use a higher vapour pressure specification than allowed by HD- 5 because of the cold conditions.

Table 1.8: Required Characteristics of Liquefied Petroleum Gases

| Item | Commercial Propane | Commercial Butane | Method of Test |
| :---: | :---: | :---: | :---: |
| Vapour pressure at $40^{\circ} \mathrm{C}$, max kPa (gage) | 1550 | 520 | ISO 4256 |
| Volatility <br> C4 hydrocarbons, mol percent, max <br> C5 hydrocarbons, mol percent, max <br> C5 and heavier hydrocarbons, mol percent, max | $\begin{aligned} & 7.5 \\ & -- \\ & 0.1 \end{aligned}$ | $2.0$ | $\begin{aligned} & \text { ISO } 7941 \\ & \text { ISO } 7941 \\ & \text { ISO } 7941 \end{aligned}$ |
| Unsaturates, mol percent | Report ${ }^{(3)}$ | Report ${ }^{(3)}$ | ISO 7941 |
| Butadienes, mol percent, max | 0.5 | 0.5 | ISO 7941 |
| Residual Matter mg/kg, max | 50 | 50 | (4) |
| Relative density, at $15^{\circ} \mathrm{C}, \mathrm{kg} / \mathrm{m}^{3}$ | Report | Report | ISO $3993{ }^{(5)}$ |
| Corrosiveness to Copper, max | 1 | 1 | ISO 6251 |
| Sulfur, mg/kg, max | 50 | 50 | (6) |
| Hydrogen sulfide | pass | pass | (7) |
| Moisture content | pass | -- | (8) |
| Free water content | -- | None ${ }^{(9)}$ |  |

Note to Table 1.8:
Certain national standards arA/or regulations may prescribe lower vapor pressure limits.
Vapor pressure may be calculated from compositional data. An ISO method is undek development. However, in case of dispute about the vapor pressure, ISO 4256 shall prevail.

[^5]Certain nattotial star4ards may prescribe a limitation on unsaturgtes.
A suitable ISO method is being investigated. Until an ISO method is available, th appended Shell Method Series 5145 1513-2 is recommended.
Relative density may be calculated from compositional data. An ISO method is undet development.
A suitable ISO method is bein; developed. Until an ISO method is available, test in accordance with a procedure that is technically equivalent to ASTM D-2784-BO (1983 Annual bc'ok of ASTM Standar"s, Section 5, page 699).

A suitable ISO method is being developed. Until an ISO mothod is available, test in accor4~nco with a procedure that is technically equivalent to ASTM D-2420-81 (. 1983 Annual Book of ASTM Standards, Sect:ion 5, page 344).

## Ethane

One of the present Canadian specification for ethane is
$\mathrm{C}_{2} \quad 95$ Mole \% Min.
$\mathrm{CO}_{2}$ 2.0 Mole \% Max.
$\mathrm{C}_{1} \quad$ 2.0 Mole \% Max.
$\mathrm{C}_{3} \quad$ 2.0 Mole \% Max.
$\mathrm{H}_{2} \mathrm{~S} \quad 100 \mathrm{ppm}$ Max.

## Pentanes

Pentanes plus is normally just the heavier portion of the liquids recovered from a gas processing plant. Generally, a specification of 12-14 psia for a Reid Vapour Pressure has to be met, and often the quantity of butane is limited to $3 \%$ for full credit as pentanes + varies quite considerably both as to its distillation and as to its composition. A detailed discussion of the chemical composition of condensate is given in a paper by M. Gawlak ${ }^{1}$.

## Sulphur

Sulphur is generally recovered by burning the $\mathrm{H}_{2} \mathrm{~S}$ recovered from the regeneration of the sweetening solution with a controlled amount of air. The following equations show the reactions that normally occur:

$$
\begin{aligned}
& \mathrm{H}_{2} \mathrm{~S}+1.5 \mathrm{O}_{2} \rightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{SO}_{2} \\
& 2 \mathrm{H}_{2} \mathrm{~S}+\mathrm{SO}_{2} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}+3 \mathrm{~S}
\end{aligned}
$$

The specification for sulphur is $99.5 \%$ pure, yellow in colour, and with no arsenic or selenium present. Texas Gulf Sulphur have set up a colour specification that makes sure that less than $0.05 \%$ C is present if their specification is met. See Error! Reference source not found. for Sulphur Specs.

### 1.8 General Processing Schemes

The steps in processing a raw, sour, rich natural gas saturated with water are shown schematically in Error! Reference source not found.. The raw gas in the reservoir is assumed to be at 4000 psig $(28,000 \mathrm{kpa})$ and $150^{\circ} \mathrm{F}\left(65^{\circ} \mathrm{C}\right)$. It is brought to the surface via the tubing in the well where it is
reduced in pressure to the operating pressure of the gas gathering line (normally less than 1440 psig) $(10,140 \mathrm{kpa})$. This is for the use of 600 psi ANSI fitting valves. Since the gas cools, when it is reduced in pressure, some of the water of saturation condenses out. This is conducive to hydrate formation. Similarly, as the gas is transmitted to the processing plant, if the distance is more than two miles, the gas will cool to ground temperatures of $+25^{\circ} \mathrm{F}\left(-4^{\circ} \mathrm{C}\right)$ to $30^{\circ} \mathrm{F}\left(-1^{\circ} \mathrm{C}\right)$ and water will also condense out. This, of course, will be conducive to formation of hydrates which will plug the pipelines. Therefore, at the well site hydrate prevention processes have to be used. These are either the heating of the gas to keep it above its hydrate point or the dehydration of the gas to remove the water. The gas is then transmitted to the processing plant via a pipeline. The flow will be generally two phase.

Upon entering the plant, the gas enters a separator where the liquids are dropped out. The gas is then sent to a sweetening unit where the acid gases are removed; generally by a sweetening agent such as monoethanol amine (MEA), diethanol amine (DEA), sulphinol, and others. The gas leaving the sweetening unit is now sweet, but is still saturated with water vapour and still contains a considerable amount of heavy hydrocarbons.

## Table 1.9: Sulphur Product Specifications

A sulphur product meeting the following specifications will normally satisfy the requirements of the major consumers of sulphur such as manufacturers of sulphuric acid, chemicals, fertilizers, etc.:

| Purity | $99.5 \%-99.8 \%$ by weight (dry basis) |
| :--- | :--- |
| Acidity $\left({\mathrm{as} \mathrm{H}_{2} \mathrm{SO}_{4} \text { ) }}^{\text {Moisture }}\right.$ | Less than $0.05 \%$ by weight |
| Ash | Nil to $1.0 \%$ by weight |
| Carbonaceous Matter | Less than $0.1 \%$ by weight |
| Arsenic, Tellurium, Selenium | Coss than $0.15 \%$ by weight |
| Colour | Bright yellow at ambient temperature. |

Note: The colour of sulphur is an important property because it gives an immediate indication of product purity. The sulphur is a bright yellow if the impurity content is less than about $0.02 \%$ by weight. Small amounts of carbon (soot) change the bright yellow colour to dull yellow or green; "dark" sulphur in which the yellow colour has a shade of grey or brown usually contains $0.1 \%-0.5 \%$ by weight of carbon. For sulphuric acid manufacturer, however, sulphur colour is usually less important than ash and heavy metal contents.

These both must be removed so that the water dewpoint and hydrocarbon dewpoint specifications can be met. This is done by several processes. For example, the gas may be chilled by refrigeration to below the dewpoint for both the water and the hydrocarbon so that the water and heavy hydrocarbon condense out. In this case, glycol is added to the gas stream at the beginning of the process to prevent hydrates or freezing. In another series of processes, the heavy hydrocarbons may be removed by absorption and the water removed by dehydration.
${ }^{\diamond}$ Contents of less than 0.25 ppmw of arsenic and 2.0 ppmw of Selenium and Tellurium are usually considered as 'Commercially Free'.

The liquid hydrocarbons from the separation facilities and from the hydrocarbon dewpoint control facilities are sent to fractionation facilities for the separating of the hydrocarbons into individual compounds.

The acid gas $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{CO}_{2}$ are sent to a sulphur recovery unit in which the $\mathrm{H}_{2} \mathrm{~S}$ is reacted with $\mathrm{O}_{2}$ from air to form elemental sulphur.

The recovery level of sulphur is set by governmental authorities. The $\mathrm{CO}_{2}$ and $\mathrm{SO}_{2}$ (that part of' the $\mathrm{H}_{2} \mathrm{~S}$ not converted to S ) is rejected to the atmosphere.


Figure 1.1: Overall Gas Processing Scheme

## References

1. M. Gawlak, Gas Processing/Canada, Sept./Oct. 1971, P. 26

## Reading List

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2. Henningser, G., and D. Bergenson, "Natural Gas Composition and Productions" Energy Processing Canada, July/August 1974 P. 32.
3. Cannon, R., "Gas Processing Developments Set Stage for 1984 to be a Banner Year", Oil and Gas Journal, July 18, 1983.
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5. Stenson, F., "Waste to Wealth", Friesen 1985.

### 2.0 Physical Properties of Light Hydrocarbons and Other Associated Compounds

- Physical properties.
- Heating value.
- Critical properties.
- Equations of state.
- Compressibility factors for gases and other physical properties.
- Special effects of sour gas.


### 2.1 Introduction

The physical properties of the fluids we are dealing with in natural gas processing are of prime importance in the design of equipment and facilities to handle these fluids. Some of the important properties are:

1. Density and/or the compressibility of a gas
2. Density of a liquid
3. Specific heats
4. Enthalpies
5. Entropies
6. Free energies
7. Heat of combustion
8. Heat of reaction
9. Viscosities
10. Thermal conductivities
11. Surface tension

There are available for individual compounds considerable data on the effect of temperature and pressure on the various properties given above. For example the GPSA Data Book on Fig. 16-1, and on other pages, give a lot of data for individual compounds and some data for mixtures. Also, Maxwell ${ }^{6}$ and Katz $^{7}$ are good references. A book providing the thermal properties of hydrocarbon has been published by Canjar and Manning ${ }^{16}$. Another good reference is by C.J. Sciance, C.J. Clover, and C.M. Shepvich. ${ }^{8}$

From the above and from other data we are primarily interested in predicting the properties of mixtures of pure compounds at varying temperature, pressures and compositions.

### 2.2 Densities

Let's start by finding the densities of gases. To do this we must calculate the compressibility of gases. Let us review some basic laws. First we have the Ideal Gas Law:

Equation 2-1

$$
P V=R T
$$

for 1 mole of gas. This law is a combination of the old Boyle's Law and Charles' Law. It assumes that the molecules occupy no space and have no attractive forces. It applies at low pressures and when compounds are a long way from their condensing temperatures.

Another law that we use considerably is a form of Dalton's Law or the Ideal Solution Law. That is, the sum of mole fraction of each compound present multiplied by the physical property of each pure compound at the conditions of the system gives the value of the physical property at the condition of the system. This law is used considerably.
The Ideal Gas Law is not too applicable to light hydrocarbons and their associated fluids. It is necessary to use more refined equations. There are two general methods of correcting the Ideal Gas Law equation:

1. By using an expanded equation of state
2. By using a correction factor in the equation $P V=R T$
ie.
Equation 2-2

$$
P V=Z R T
$$

This method is used a great deal in light hydrocarbon work. However, equations of state are coming more into use because of the availability of computers.

### 2.2.1 Equations of State

One of the first and most famous was developed by Van der Waals in 1873. This equation is:
Equation 2-3

$$
\left(P+\frac{a}{v^{2}}\right)(V-b)=R T
$$

where " $a$ " is the attractive force between the molecules and " $b$ " is the volume occupied by the molecules. For each compound a different value of "a" and "b" has been developed. The Chemical Engineer 's Handbook gives data for the contents.
Another famous equation is the Beattie Bridgeman equation developed in 1927. The equation is:
Equation 2-4

$$
P=\frac{R T}{V^{2}}\left(1-\frac{c}{V T^{3}}\right) V+B_{0}\left(1-\frac{b}{V}\right)-\frac{A_{0}}{V^{2}}\left(1-\frac{a}{V}\right)
$$

where $A_{0}, B_{0}, a, b$, and $c$ are constants for a particular gas. This applies to pure compounds and mixtures of gases of similar chemical species. It cannot be used for liquid vapour phase behaviour.

This equation is the basis for the virial equation of state of which the one discussed next is a prime example.
These two previously mentioned equations are not used much now but rather the following equations are used.
An equation that has been useful in the prediction of PVT in two phase regions is the Benedict-Webb-Rubin equation (BWR), developed in 1940, and modified by Starling in 1970, ${ }^{1,2}$ (BWRS)

Equation 2-5

$$
P=R T \rho+\left(B_{0} R T-A-\frac{C_{0}}{T^{2}}+\frac{D_{0}}{T^{3}}-\frac{E_{0}}{T^{4}}\right) \rho^{2}+\left(b R T-a-\frac{d}{T}\right) \rho^{3}+\left(a+\frac{d}{T}\right) \alpha \rho^{6}+\frac{c \rho^{3}}{T^{2}}\left(1+\chi \rho^{2}\right) \exp \left(-\chi \rho^{2}\right)
$$

where: $\mathrm{B}_{\mathrm{o}}, \mathrm{A}_{\mathrm{o}}, \mathrm{C}_{\mathrm{o}}, \mathrm{D}_{\mathrm{o}}, \mathrm{E}_{\mathrm{o}}, \mathrm{b}, \mathrm{a}, \alpha, \mathrm{c}, \mathrm{d}, \gamma$ are constants for a particular compound. For example, the constants for light hydrocarbons, N 2 , and $\mathrm{CO}_{2}$ as determined by Hopke \& Lin ${ }^{3}$ are given in Error!
Reference source not found.. The units used in this table are:

$$
\begin{aligned}
& \text { Pressure = psia } \\
& \text { Density = (lbmoles) (cu. ft.) } \\
& \text { Temperature }={ }^{\circ} \text { Rankine } \\
& \mathrm{R}=10.7335\left(\text { psia cu ft) }\left(\mathrm{lbmole}{ }^{\circ} \mathrm{R}\right)\right.
\end{aligned}
$$

To handle mixtures the following set of equations are used for each constant according to Hopke \& Lin.

Table 2.1: The Optimal BWRS Parameters

|  | $\mathrm{CH}_{4}$ | $\mathrm{C}_{2} \mathrm{H}_{6}$ | $\mathrm{C}_{3} \mathrm{H}_{8}$ | I-C4 $\mathrm{H}_{10}$ | $\mathrm{N}-\mathrm{C}_{4} \mathrm{H}_{10}$ | $\mathrm{I}-\mathrm{C}_{5} \mathrm{H}_{12}$ | $\mathrm{N}-\mathrm{C}_{5} \mathrm{H}_{12}$ | $\mathrm{N}_{2}$ | $\mathrm{CO}_{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bo | 0.69663 | 0.940341 | 1.15091 | 1.41699 | 1.38780 | 1.61871 | 1.54342 | 0.686293 | 0.473428 |
| $\mathrm{A}_{0} / 10^{4}$ | 0.703241 | 1.50851 | 2.20325 | 3.01020 | 3.12799 | 3.93334 | 3.95713 | 0.424533 | 0.762197 |
| $\mathrm{C}_{0} / 10^{8}$ | 3.31272 | 26.0615 | 75.3232 | 137.356 | 159.698 | 257.683 | 284.646 | 0.974169 | 20.8025 |
| $\gamma$ | 1.39930 | 3.04151 | 5.50136 | 8.82944 | 9.00761 | 12.7727 | 13.0384 | 1.19172 | 1.26588 |
| b | 0.861307 | 2.69564 | 6.36610 | 10.6254 | 11.2723 | 16.7246 | 18.8648 | 0.559419 | 9.976469 |
| $\mathrm{a} / 10^{3}$ | 2.75239 | 17.3349 | 55.8356 | 101.674 | 113.271 | 184.751 | 207.942 | 0.921051 | 6.05085 |
| $\alpha$ | 0.453145 | 1.03845 | 2.17606 | 4.37780 | 4.24116 | 7.10095 | 6.99803 | 0.48971 | 0.32038 |
| c/10 ${ }^{9}$ | 0.508281 | 5.94592 | 23.3092 | 52.3431 | 62.8476 | 120.128 | 131.746 | 0.112862 | 2.41003 |
| Do/10 ${ }^{10}$ | 1.41063 | 20.7312 | 75.6999 | 160.026 | 195.633 | 349.884 | 412.701 | 0.362181 | 15.5050 |
| d/10 ${ }^{5}$ | 0.684469 | 5.98254 | 18.744 | 40.6431 | 46.7125 | 84.3874 | 97.2323 | 0.282061 | 3.48824 |
| Eo/10 ${ }^{11}$ | 1.26531 | 90.0981 | 437.431 | 1056.56 | 1381.81 | 2894.06 | 3518.30 | 0.327911 | 107.933 |

To handle mixtures the following set of equations are used for each constant according to Hopke \& Lin.

[^6]Table 2.2: Mixing Rules - BWRS Equation

$$
\begin{array}{ll}
B_{0}=\sum_{i} x_{i} B_{0 i} & b^{1 / 3}=\sum_{i} x_{i} b_{i}^{1 / 3} \\
A_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{3} x_{i} x_{j} A_{0 i}{ }^{1 / 3} A_{0 j}{ }^{1 / 2} & a^{1 / 3}=\sum_{i} x_{i} a_{i}^{1 / 3} \\
C_{0}=\sum_{i} \sum_{j}\left(\frac{m_{1 j}}{2}\right)^{3} x_{i} x_{j} C_{0 i}{ }^{1 / 2} C_{0 j}{ }^{1 / 2} & \alpha^{1 / 3}=\sum_{i} x_{i} \alpha_{i}^{1 / 3} \\
\chi^{1 / 2}=\sum_{i} x_{i} \chi_{i}^{1 / 2} & c^{1 / 3}=\sum_{i} x_{i} c_{i}^{1 / 3} \\
D_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{4} x_{i} x_{j} D_{0 i}{ }^{1 / 2} D_{0 j}{ }^{1 / 2} & d^{1 / 3}=\sum_{i} x_{i} d_{i}^{1 / 3}
\end{array}
$$

where $\mathrm{x}_{\mathrm{i}}$. is the mole fraction of the "ith" component for the homogeneous phase under consideration, and parameters with subscript "i" refer to the "ith" pure component, $m_{i j}$ is the interaction parameter between binary mixtures, and is equal to 2.0 for $\mathrm{i}=\mathrm{j}$. Another common interaction coefficient is $\mathrm{k}_{\mathrm{ij}} ; \mathrm{m}_{\mathrm{ij}}=2\left(\mathrm{l}-\mathrm{k}_{\mathrm{ij}}\right)$.

The values of $\mathrm{m}_{\mathrm{ij}}$ between binaries of hydrocarbons, $\mathrm{N}_{2}$, and $\mathrm{CO}_{2}$, as determined by Hopke \& Lin, are given in the following table.

Table 2.3: Optimal Interaction Parameters $\boldsymbol{m}_{i j}$

|  | C1 | C2 | C3 | I-C4 | N-C4 | I-C5 | N-C5 | Nitrogen |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Carbon <br> Dioxide |  |  |  |  |  |  |  |  |
| C1 | 2.000 |  |  |  |  |  |  |  |
| C2 | 1.999 | 2.000 |  |  |  |  |  |  |
| C3 | 1.998 | 2.011 | 2.000 |  |  |  |  |  |
| I-C4 | 1.997 | 1.998 | 1.999 | 2.000 |  |  |  |  |
| N-C4 | 1.997 | 1.998 | 1.999 | 2.000 | 2.000 |  |  |  |
| I-C5 | 1.996 | 1.997 | 1.998 | 1.999 | 1.999 | 2.000 |  |  |
| N-C5 | 1.996 | 1.997 | 1.998 | 1.999 | 1.999 | 2.002 | 2.000 |  |
| Nitrogen | 1.954 | 1.926 | 1.913 | 1.883 | 1.883 | 1.921 | 1.921 | 2.000 |
| Carbon <br> Dioxide | 1.943 | 1.928 | 1.913 | 1.894 | 1.898 | 1.900 | 1.887 | 2.015 |

Another set of mixing rules also using interaction coefficients $\left(\mathrm{k}_{\mathrm{i}}\right)$ has been proposed by Bishnoi \& Robinson ${ }^{4}$

This equation is used for predicting all PVT data and vapour liquid phase behaviour of inulticomponent mixtures. Another equation of state that has gained favour is the Redlich Kwong ${ }^{19}$ equation which was published in 1949.

Equation 2-7

$$
P=\frac{R T}{V-b}-\frac{a}{T^{0.5} V(V+b)}
$$

or $Z$, the compressibility factor as given in the other type of equation, can be expressed as follows:
Equation 2-8

$$
Z=\frac{1}{1-h}-\frac{A^{2}}{B}\left(\frac{h}{1+h}\right)
$$

Where

$$
h=\frac{b}{V}=\frac{B P}{Z}
$$

where $a, b$, or $A, B$ are adjustable parameters of a particular gas and can be calculated from the gases critical properties.

$$
\begin{aligned}
& A^{2}=\frac{a}{R^{2} T^{2.5}} \quad B=\frac{b}{R T} \\
& a=0.4278 T_{C}^{2.5} \frac{R^{2}}{P_{C}} \\
& b=0.0867 \frac{R T_{C}}{P_{C}}
\end{aligned}
$$

Soave ${ }^{9}$ recently proposed a modification that has been used for calculating equilibrium " k " data very successfully. This change is as follows:

$$
P=\frac{R T}{V-b}-\frac{a(T)}{V(V+b)}
$$

Or

$$
Z^{3}-Z^{2}+Z\left(A-B-B^{2}\right)-A B=0
$$

Where

$$
\begin{aligned}
A & =\frac{a P}{R^{2} T^{2}} \\
B & =\frac{b P}{R T}
\end{aligned}
$$

Mixing rules using the interaction coefficients have developed for the constants "a" and "b" or A and $B$, i.e.

Equation 2-11

$$
a_{i j}=\left(1-k_{i j}\right)\left(a_{i} a_{j}\right)
$$

where $a_{i j}=$ constant for the a for a mixture of $a_{i}$ and $a_{j}$ $\mathrm{k}_{\mathrm{ij}}=$ the interaction coefficient for the binary i and j .
Another recent equation that has been proposed is the Peng and Robinson ${ }^{17}$ equation, which can be expressed as

Equation 2-12

$$
P=\frac{R T}{V-b}-\frac{a(T)}{V(V+b)+b(V-b)}
$$

This equation seems to cover the ranges of temperature and pressure very well. Also most physical properties are calculated close to experimental values.
BWRS and EK equations can be used with liquids or for calculating enthalpies, etc. For example, to use the BWRS for enthalpy, the following equation is used for correcting the effect of pressure on enthalpy:

$$
\begin{aligned}
& H_{T, P}-H_{T, 0}=\left(B_{0} R T-2 A_{0}-\frac{4 C_{0}}{T^{2}}+\frac{5 D_{0}}{T^{3}}-\frac{6 E_{0}}{T^{4}}\right) \rho+0.5\left(2 b R T-3 a-\frac{4 d}{T}\right) \rho^{2}+0.2 \alpha\left(6 a+\frac{7 d}{T}\right) \rho^{5} \\
& +\frac{c \rho^{2}}{T}\left[3\left(\frac{1-\exp \left(-\chi \rho^{2}\right)}{\chi \rho^{2}}\right)-0.5 \exp \left(-\chi \rho^{2}\right)+\gamma \rho^{2} \exp \left(-\chi \rho^{2}\right)\right]
\end{aligned}
$$

### 2.2.2 Compressibility Factors

The second type of method is the correction factor method. That is, we apply a correction factor to the ideal gas equation:

Equation 2-14

$$
P V=Z R T
$$

$\mathrm{V}=$ volume of a mole of gas
$Z=$ correction factor and is a function of

$$
T_{r}=\frac{T}{T_{c}}
$$

and

$$
P_{r}=\frac{P}{P_{c}}
$$

Figure 16-3 through Figure 16-11 of the GPSA Data book give data on "Z" as a general correlation. To handle mixtures, the law of corresponding states is applied. This is as follows:
"Substances should have similar properties at similar corresponding states. A corresponding state is that distance from the critical temperature or critical pressure expressed on an absolute basis."
This was developed by van der Waal. Thus to handle mixtures we calculate the reduced temperature and pressure for the mixture and then read of $f$ the proper " $Z$ ". The " $T_{c}$ " and " $P_{c}$ " for mixtures are the so called pseudo values and are the values found by multiplyingthe mole fraction of a component present by the value of the property as if it was a pure compound and then summing the values.

## Example Problem 2.1

Find the compressibility factor and the actual density of gas of the composition given in the table below when the gas is at 1000 psig and $100^{\circ} \mathrm{F}$.

| Comp. | Mole $\%$ | $\mathbf{T}_{\mathbf{c}}{ }^{\circ} \mathbf{R}$ | $\mathbf{p T}_{\mathbf{c}}$ | Pc psia | $\mathbf{p P}_{\mathbf{c}}$ | Mole wt | p Mole wt | Comments |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{N}_{2}$ | 1.65 | 227 | 3.7 | 492 | 8.1 | 28 | 0.5 |  |
| $\mathrm{C}_{1}$ | 89.60 | 343 | 318. <br> 0 | 668 | 605.0 | 16 | 14.3 |  |
| $\mathrm{C}_{2}$ | 4.99 | 550 | 27.4 | 710 | 35.5 | 30 | 1.5 |  |
| $\mathrm{C}_{3}$ | 2.03 | 666 | 13.6 | 616 | 13.5 | 44 | 0.9 |  |
| $\mathrm{iC}_{4}$ | 0.37 | 735 | 2.7 | 529 | 2.0 | 58 | 0.2 |  |
| $\mathrm{nC}_{4}$ | 0.62 | 765 | 4.7 | 551 | 3.4 | 58 | 0.4 |  |
| $\mathrm{iC}_{5}$ | 0.19 | 830 | 1.6 | 483 | 0.9 | 72 | 0.1 |  |
| $\mathrm{nC}_{5}$ | 0.14 | 846 | 1.2 | 489 | 0.7 | 72 | 0.1 |  |
| $\mathrm{C}_{6}$ | 0.31 | 914 | 2.8 | 440 | 1.4 | 86 | 0.3 |  |
| $\mathrm{C}_{7}+$ | 0.10 | 102 | 1.0 | 362 | 0.4 | 114 | 0.1 | Use properties of $\mathrm{C}_{8}$ |
|  |  | 4 |  | 376. |  | 670.9 |  | 18.4 |

## Therefore:

pseudo $T_{c}=376.7^{\circ} \mathrm{R}$
pseudo $\mathrm{P}_{\mathrm{c}}=670.9$ psia
average molecular weight $=18.4$
Equation 2-16

$$
T_{r}=\frac{T}{T_{c}}=\frac{560}{376.7}=1.48
$$

Equation 2-17

$$
P_{r}=\frac{P}{P_{c}}=\frac{1014.7}{670.9}=1.52
$$

From the graph on Figure 16-3 on the GPSA Manual
Z $=0.855$
Now find the density of 1 cubic foot at the operating condition
Equation 2-18

$$
\rho=\frac{P M_{W}}{Z R T}=\frac{1014.7(18.4)}{0.855(10.73)(560)}=3.7 \mathrm{lbs} / \mathrm{cu} . \mathrm{ft}
$$

This method is pretty good for mixtures of light hydrocarbons or other similar groups of compounds. Example Problem 1a shows this problem done in Metric units.
1a. The metric values in the problem are
Pressure $=6996 \mathrm{kPa}$ or 69, Atmos.
Temperature $=32^{\circ} \mathrm{C}$
or $305^{\circ} \mathrm{K}$
$T_{r}$ and $P_{r}$ will be the same. The actual density in gram/cc will be

$$
\rho=\frac{P M_{W}}{Z R T}=\frac{69(18.4)}{0.855(82.057)(305)}=0.059 \mathrm{gram} / \mathrm{cc}
$$

Figure 4-13 in $\mathrm{Katz}^{7}$ shows how well individual compounds compare.
For example at a $P_{r}=2.0$ the " $Z$ " for $C_{1}, C_{3}$ and $C_{5}$ is shown in Table 2.4.
Table 2.4: Comparison of Compressibility Factors

| "Z" Values |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{T}_{\mathbf{r}}$ | $\mathbf{C}_{\mathbf{1}}$ | $\mathbf{C}_{3}$ | $\mathbf{C}_{\mathbf{5}}$ | From NGPSA Manual For Gas at These Conditions |
| 1.1 | 0.39 | 0.405 | 0.415 | .37 |
| 1.2 | 0.575 | 0.595 | 0.620 | .55 |
| 1.3 | 0.700 | 0.740 | 0.755 | .685 |
| 1.5 | 0.840 | 0.880 | 0.905 | .820 |

However the generalized compressibility chart can be used with good accuracy for light hydrocarbons with less than $5 \% N_{2}$ present. It was developed by Standing and Katz ${ }^{10}$
For natural gases in which composition is not known, on Fig. 16-6 of the GPSA Data Book gives the pseudo critical pressure and temperatures versus gas gravity. It should be noted that the
pseudo critical temperature and pressure are not necessarily anywhere near actual values. Consider a phase envelope as shown in Figure 2.1.


Figure 2.1: Actual and Pseudo Critical Points
For gas mixtures containing significant quantities of sour gas the " $z$ " is not correct as calculated from the Standing Katz chart. A method has been developed by E. Wichert and K. Aziz at the University of Calgary. This method is quite simple and has been Checked by Comparison of over 1000 actual measurements. The authors have also developed a more detailed method using the Redlich Kwong equation that is applicable to a computer. The actual computer program is available through the CNGPA Research program. ${ }^{12}$
The simple graphical method depends on finding " $\varepsilon$ " the pseudo critical temperature adjustment factor. This factor is a function of the $\%$ of $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{CO}_{2}$ present. Figures 2.2 and 2.3 show this. Figure 2.3 is just a blow up of the data at lower \% acid gas. The method is as follows:

1. Calculate the pseudo $T_{c}$ and pseudo $P_{c}$ for a mixture in the regular manner.
2. Find value for " $\varepsilon$ " depending on the composition.
3. Find sour gas $p T_{c}$ ' from

Equation 2-19
$p T_{c}{ }^{\prime}=p T_{c}-\varepsilon$
4. Find sour gas $\mathrm{pP}_{\mathrm{c}}$ ' from $B$ is the mole fraction of $\mathrm{H}_{2} \mathrm{~S}$ in the gas.

Equation 2-20
$p P_{c}^{\prime}=\frac{p P_{c} p T_{c}^{\prime}}{p T_{c}+B(1-B) \varepsilon}$
where $B$ is the mole fraction of $\mathrm{H}_{2} \mathrm{~S}$ in the gas
5. Calculate pseudo reduced temperature and pressure using above data.
6. Read "Z" from regular Standing and Katz chart, Fig. 16-3 GPSA Data book.

Find the compressibility factor for the gas of the composition given below and compare it with the measured value of 0.671 at $2000 \mathrm{psig}(13,890 \mathrm{kpa})$ and $80^{\circ} \mathrm{F}\left(26.6^{\circ} \mathrm{C}\right.$. The pseudo critical pressure for the mixture is $834 \mathrm{psia}(5750 \mathrm{kpa})$ and the pseudo critical temperature $432^{\circ} \mathrm{R}\left(240^{\circ} \mathrm{K}\right)$.

| Composition |  |
| :---: | :---: |
|  | Mole \% |
| $\mathrm{N}_{2}$ | 0.66 |
| $\mathrm{H}_{2} \mathrm{~S}$ | 25.65 |
| $\mathrm{CO}_{2}$ | 4.73 |
| $\mathrm{C}_{1}$ | 67.57 |
| $\mathrm{C}_{2}$ | 0.56 |
| $\mathrm{C}_{3}+$ | 0.83 |
|  | 100.00 |

Using the regular method of finding the reduced pressures and temperatures we get:

$$
P_{r}=\frac{2014}{834}=2.44
$$

$$
T_{r}=\frac{540}{432}=1.25
$$

From the graph on Figure 16-3 of the GPSA Manual,

$$
Z=0.585
$$

Next check by Wichert and Aziz method.

English Units
Metric Units
$240-17=223$

Equation 2-24
$p P_{c}^{\prime}=834\left(\frac{401}{432+6}\right)=770$

$$
p T_{c}^{\prime}=432-31=401
$$

Equation 2-23
$5750\left(\frac{223}{240+3.28}\right)=5270$

Equation 2-25
SourGas $T_{r}=\frac{540}{401}=1.36$

$$
\frac{300}{223}=1.35
$$

SourGas $P_{r}=\frac{2014}{770}=2.62$

$$
\frac{13890}{5212}=2.64
$$

Equation 2-27
SourGas $Z=0.69$

Measured value was about 0.671 .
Note: Whenever you have a sour gas containing 10\% or greater acid gases you should probably correct the compressibility factors by using one of the sour gas correction factor methods.
If further refinement of " $Z$ " is necessary (i.e. with liquids present, $\mathrm{H}_{2} \mathrm{O}, \mathrm{N}_{2}$ or various unusual compounds such as could be more expected in petrochemical work), then we can modify "Z" by use of the "acentric" factor " $\omega$ " and the value of " $Z$ " for a simple fluid and the deviation from a simple fluid:

Equation 2-28

$$
Z=Z^{0}+\omega Z^{\prime}
$$

$Z^{\circ}$ is the compressibility factor for a simple fluid
$Z^{\prime}$ is the compressibility factor correction for deviation from a simple fluid.
$\omega$ acentric factor is a measure of deviation from an idealized simple fluid (argon, krypton, etc.)

$$
\omega=-\left(\log P_{r}{ }^{0}+1.00\right) \quad \text { at } T_{r}=0.700
$$

or by the equation
Equation 2-29

$$
\omega=\frac{3}{7} \frac{\log P_{c} / 14.7}{\frac{T_{c}}{T_{B}}-1.00}-1.00
$$

where

$$
\begin{aligned}
& \mathrm{P}_{\mathrm{c}}=\text { critical pressure } \\
& \mathrm{T}_{\mathrm{C}}=\text { critical temperature } \\
& \mathrm{T}_{\mathrm{B}}=\text { Boiling point }
\end{aligned}
$$

This equation can be used for mixtures when individual " $\omega$ " are not available. Figure 16-21 GPSA Data Book gives some data for " $\omega$ ".
To find $Z^{\circ}$ and $Z^{\prime}$ figures 2.4 and 2.5 can be used. These are charts reproduced from an article by K.S. Pitzer ${ }^{5}$.

To actually find $Z$ for a gas the following procedure is used:

1. Find " $\omega$ " for a gas mixture by multiplying the value x for each compound by the mole fraction of each component present.
2. Find $Z^{\circ}$ and $Z^{\prime}$ from figures 2.4 and 2.5 after finding the systems $P_{r}$ and $T_{R}$

To see the effect of this change the following comparison between $\mathrm{NH}_{3}$ and $\mathrm{CH}_{4}$ is given in Table 2.5.

Table 2.5: Actual Compressibilities $\mathbf{C H}_{4}$ and $\mathbf{N H}_{3}$

| Reduced Pressure ( $\mathrm{P}_{\mathrm{r}}$ ) | 2.0 |  | 2.0 |  |
| :---: | :---: | :---: | :---: | :---: |
| Reduced Temperature ( $\mathrm{T}_{\mathrm{r}}$ ) | 1.0 |  | 2.0 |  |
| Z ${ }^{\circ}$ | 0.330 |  | 0.958 |  |
| Z' | - 0.123 |  | + 0.155 |  |
|  | $\mathrm{CH}_{4}$ | $\mathrm{NH}_{3}$ | $\mathrm{CH}_{4}$ | $\mathrm{NH}_{3}$ |
| $\omega$ | 0.013 | 0.250 | 0.013 | 0.250 |
| $\omega Z^{\prime}$ | - 0.0016 | - 0.0308 | + 0.0020 | + 0.0383 |
| $Z=Z^{\circ}+\omega Z^{\prime}$ | 0.328 | 0.299 | 0.960 | 0.997 |



Figure 2.2: Pseudo Critical Temperature Correction Factor, $\varepsilon$, $q$
See Metric GPSA Data Book for values in ${ }^{\circ} \mathrm{C}$


Figure 2.3: Pseudo Critical Temperature Correction Factor, "Normal Operating Range", $\varepsilon$, 9

See Metric GPSA Data Book for values in ${ }^{\circ} \mathrm{C}$


Figure 2.4: Generalized Compressibility Factor for Simple Fluid


Figure 2.5: Generalized Compressibility Factor Correction for Deviation from Simple Fluid

### 2.2.3 Liquid Densities

For liquids at low pressures and room temperatures the liquid volumes are additive and the liquid density can be calculated from the composition and temperature density charts (Fig. 16-IZ, GPSA Data Book). This procedure assumes ideal solutions. Note that methane and ethane data are given as the apparent density. Another way is to calculate density exclusive of $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ and use the chart on P. 167 of the GPSA Manual (1966 Ed.) to find system with $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$. This procedure is based on the equation

$$
V=x_{c 1} \bar{V}_{c 1}+x_{c 2} \bar{V}_{c 2}+\sum_{i=3}^{n} x_{c i} \bar{V}_{c 1}
$$

where $\bar{V}_{c 1}$ and $\bar{V}_{c 2}$ are the effective molar volumes of methane and methane. Figure 2.6 gives the data for this calculation.

At high pressure it is necessary to correct the density. Figure 16-15 GPSA Data Book shows how to do this.

The various equations of state, i.e. the BWRS, the Redlich Kwong, Soave and the Peng-Robinson methods, can also be used to calculate liquid densities as well. In fact most cou~uter programs of these equations give both the liquid and gas densities of a two-phase mixture.

### 2.2.4 Density of Cryogenic Liquids

As the temperatures of separation decrease any liquids produced contain increasing amounts of methane and ethane. Equation 31 (and Table 2.6 and Table 2.7) expresses an empirical density correlation for liquified natural gas (LNG). It is for liquids with a molecular weight less than 33, containing less than 5 mole \% nitrogen, oxygen and isoparaffins, in the temperature range -140 to $184^{\circ} \mathrm{C}\left(-220\right.$ to $\left.-300^{\circ} \mathrm{F}\right)$


Figure 2.6: Density of Remainder of System Grams Per CC

$$
\rho=\frac{\sum x_{i} M_{i}}{\sum\left(x_{i} V_{i}\right)-x_{m} C}
$$

where:
$\rho=$ density in kg/cu meter
$x_{i}=$ mol. fr. of component "i"
$M_{i}=$ mol. wt. of component "i"
$V_{i}=$ molar volume of "i" from Table 2.6
$x_{m}=$ mol. fr. of methane
C = correction factor for volume reduction from Table 2.7

### 2.3 Thermodynamic Properties

The next set of physical properties to discuss are thermodynamic properties. These include enthalpy, or heat capacity, latent heats and specific heats.

### 2.3.1 Outline of Properties

## Enthalpy or Heat Capacity

" H " is the total amount of heat required to raise a unit of mass to a predetermined temperature and pressure from a base temperature and pressure.

Equation 2-32

$$
\Delta H=\Delta E+\Delta P V \text { for a substance }
$$

where:
$E$ is the internal energy
P is the pressure
$V$ is the specific volume
Table 2.6: Molar Volumes of Individual Components

| Component | Mol. Mass kg/kmole | $-175^{\circ} \mathrm{C}$ | $-170^{\circ} \mathrm{C}$ | $-165^{\circ} \mathrm{C}$ | $-160^{\circ} \mathrm{C}$ | $-155^{\circ} \mathrm{C}$ | $-150^{\circ} \mathrm{C}$ | $-145^{\circ} \mathrm{C}$ | $-140^{\circ} \mathrm{C}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{4}$ | 16.042 | $\begin{aligned} & 0.0363 \\ & 6 \end{aligned}$ | $\begin{aligned} & 0.0369 \\ & 6 \end{aligned}$ | $\begin{aligned} & 0.9375 \\ & 7 \end{aligned}$ | $\begin{aligned} & 0.0382 \\ & 1 \end{aligned}$ | $\begin{aligned} & 0.0389 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0.0396 \\ & 4 \end{aligned}$ | $\begin{aligned} & 0.0404 \\ & 2 \end{aligned}$ | $\begin{aligned} & 0.0412 \\ & 6 \end{aligned}$ |
| $\mathrm{C}_{2} \mathrm{H}_{6}$ | 30.068 | $\begin{aligned} & 0.0468 \\ & 2 \end{aligned}$ | $\begin{aligned} & 0.0472 \\ & 1 \end{aligned}$ | $\begin{aligned} & 0.0476 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0.0480 \\ & 0 \end{aligned}$ | $0.0484$ | $\begin{aligned} & 0.0488 \\ & 2 \end{aligned}$ | $\begin{aligned} & 0.0492 \\ & 5 \end{aligned}$ | $\begin{aligned} & 0.0496 \\ & 9 \end{aligned}$ |
| $\mathrm{C}_{3} \mathrm{H}_{8}$ | 44.094 | $\begin{aligned} & 0.0612 \\ & 2 \end{aligned}$ | $0.0616$ | $\begin{aligned} & 0.0620 \\ & 8 \end{aligned}$ | $\begin{aligned} & 0.0625 \\ & 2 \end{aligned}$ | $\begin{aligned} & 0.0629 \\ & 8 . \end{aligned}$ | $\begin{aligned} & 0.0634 \\ & 4 \end{aligned}$ | $\begin{aligned} & 0.0639 \\ & 2 \end{aligned}$ | $\begin{aligned} & 0.0644 \\ & 0 \end{aligned}$ |
| $\mathrm{n}-\mathrm{C}_{4} \mathrm{H}_{10}$ | 58.120 | $\begin{aligned} & 0.0754 \\ & 3 \end{aligned}$ | $\begin{aligned} & 0.0758 \\ & 9 \end{aligned}$ | $\begin{aligned} & 0.0763 \\ & 5 \end{aligned}$ | $\begin{aligned} & 0.0768 \\ & 2 \end{aligned}$ | $\begin{aligned} & 0.0772 \\ & 9 \end{aligned}$ | $\begin{aligned} & 0.0777 \\ & 8 \end{aligned}$ | $\begin{aligned} & 0.0782 \\ & 6 \end{aligned}$ | $\begin{aligned} & 0.0787 \\ & 6 \end{aligned}$ |


| $\mathrm{i}-\mathrm{C}_{4} \mathrm{H}_{10}$ | 58.120 | 0.0755 | 0.0760 | 0.0765 | 0.0771 | 0.0776 | 0.0781 | 0.0787 | 0.0792 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 7 | 8 | 9 | 1 | 4 | 8 | 3 | 8 |
| $\mathrm{n}-\mathrm{C}_{5} \mathrm{H}_{12}$ | 72.146 | 0.0889 | 0.0894 | 0.0399 | 0.0904 | 0.0909 | 0.0915 | 0.0920 | 0.0926 |
|  |  | 4 | 4 | 5 | 7 | 9 | 2 | 6 | 0 |
| $\mathrm{i}-\mathrm{C}_{5} \mathrm{H}_{12}$ | 72.146 | 0.0095 | 0.0900 | 0.0906 | 0.0911 | 0.0916 | 0.0922 | 0.0927 | 0.0933 |
|  |  | 7 | 8 | 0 | 3 | 7 | 1 | 5 | 0 |
| $\mathrm{n}-\mathrm{C}_{6} \mathrm{H}_{14}$ | 86.172 | 0.1032 | 0.1038 | 0.1043 | 0.1048 | 0.1054 | 0.1060 | 0.1065 | 0.1071 |
|  |  | 6 | 0 | 4 | 9 | 5 | 2 | 9 | 6 |
| $\mathrm{~N}_{2}$ | 28.016 | 0.0399 | 0.0418 | 0.0440 | 0.0468 | 0.0502 | 0.0542 | 0.0591 | 0.0849 |
|  |  | 6 | 1 | 7 | 3 | 1 | 8 | 5 | 6 |
| $\mathrm{O}_{2}$ | 32.00 |  | 0.0298 | 0.0306 | 0.0315 | 0.0325 | 0.0336 |  |  |

Molar Volume, $\mathrm{m}^{3} / \mathrm{kmole}$, at various temperatures
Table 2.7: Correction, C, for Volume Reduction of LNG Mixtures

| Molecular Mass of Mixture $\mathbf{x}_{1} \mathbf{M}_{1}$ | $-140{ }^{\circ} \mathrm{C}$ | $-145{ }^{\circ} \mathrm{C}$ | $-150{ }^{\circ} \mathrm{C}$ | $-155^{\circ} \mathrm{C}$ | $-160^{\circ} \mathrm{C}$ | $-165^{\circ} \mathrm{C}$ | $-170^{\circ} \mathrm{C}$ | $-175{ }^{\circ} \mathrm{C}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 16.0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 16.2 | 0.06 | 0.05 | 0.05 | 0.04 | 0.04 | 0.04 | 0.03 | 0.03 |
| 16.4 | 0.13 | 0.12 | 0.122 | 0.10 | 0.10 | 0-09 | 0.08 | 0.07 |
| 16.6 | 0.20 | 0.18 | 0.17 | 0.16 | 0.15 | 0.13 | 0.12 | 0.11 |
| 16.8 | 0.26 | 0.25 | 0.23 | 0.21 | 0.19 | 0.19 | 0.16 | 0.15 |
| 17.0 | 0.33 | 0.31 | 0.29 | 0.27 | 0.24 | 0.23 | 0.21 | 0.19 |
| 17.2 | 0.40 | 0.37 | 0.35 | 0.32 | 0.30 | 0.27 | 0.25 | 0.23 |
| 17.4 | 0.47 | 0.44 | 0.40 | 0.38 | 0.35 | 0.32 | 0.30 | 0.27 |
| 17.6 | 0.54 | 0.49 | 0.46 | 0.43 | 0.40 | 0.37 | 0.34 | 0.31 |
| 17.8 | 0.60 | 0.55 | 0.51 | 0.48 | 0.44 | 0.41 | 0.38 | 0.35 |
| 18.0 | 0.66 | 0.61 | 0.57 | 0.53 | 0.49 | 0.45 | 0.42 | 0.38 |
| 18.5 | 0.81 | 0.75 | 0.70 | 0.65 | 0.60 | 0.56 | 0.52 | 0.48 |
| 19.0 | 0.95 | 0.88 | 0.82 | 0.76 | 0.71 | 0.66 | 0.61 | 0.57 |
| 19.5 | 1.09 | 1.01 | 0.94 | 0.88 | 0.81 | 0.76 | 0.70 | 0.65 |
| 20.0 | 1.21 | 1.13 | 1.05 | 0.98 | 0.91 | 0.85 | 0.79 | 0.74 |
| 21.0 | 1.42 | 1.34 | 1.25 | 1.17 | 1.10 | 1.03 | 0.96 | 0.89 |
| 22.0 | 1.61 | 1.53 | 1.43 | 1.35 | 1.26 | 1.18 | 1.10 | 1.03 |
| 23.0 | 1.75 | 1.65 | 1.56 | 1.48 | 1.39 | 1.31 | 1.23 | 1.15 |
| 24.0 | 1.85 | 1.76 | 1.67 | 1.58 | 1.49 | 1.41 | 1.33 | 1.26 |
| 25.0 | 1.92 | 1.83 | 1.74 | 1.66 | 1.58 | 1.50 | 1.42 | 1.34 |

$\mathrm{c} \times 10 \mathrm{~m}^{3} / \mathrm{kmole}$, at various temperatures

## Latent Heat

Heat required for a change of phase can be expressed by Clausius Chapeyron equation:
Equation 2-33
$\frac{d P}{d T}=\frac{\Delta H}{T \Delta V}$

## Specific Heats

This is defined as the amount of heat required to raise a unit of mass a degree of temperature. They are measured at

Constant pressure Cp
Constant volume Cv
For a perfect gas it can be shown

$$
C p=C v+R \text { for a mole of a compound }
$$

where:
$R$ is the gas constant.
This equation is used in calculating the ratio of specific heats for a mixture which is used in compression calculations.

## Entropy - "S"

Another well known property that is used in some calculations is the entropy which depends only on the condition of the system. It can be defined by the equation:

Equation 2-35

$$
d S=\frac{d Q}{T}
$$

where:
$Q$ is the heat absorbed by the system.
For a change of phase and for most applications we know $d Q=d H$. Therefore, at a constant temperature and pressure we can write:

Equation 2-36

$$
\Delta S=\frac{\Delta H}{T}
$$

## Free Energy

We also will consider later another thermodynamic property called the free energy $F$. It is defined by the equation:

$$
F=H-T S
$$

where:
$F$ is a measure of the useful work done exclusive of expansion work.

For a chemical reaction the change of free energy can be expressed by the equation:

$$
\Delta F^{0}=R T \ln K
$$

where:
K is the chemical equilibrium constant.
Also we can write the equation:
Equation 2-39

$$
\Delta F^{0}{ }_{P-R}=\Delta H^{0}{ }_{P-R}-T \Delta S^{0}{ }_{P-R}
$$

where:
the subscripts P and R respectively represent products and reactants of a chemical equation.

### 2.3.2 Enthalpies

The enthalpies of pure compounds are given in many tables, in Chemical Engineer's Handbook, in Maxwell ${ }^{6}$, in $\mathrm{Katz}^{7}$ and in the GPSA Data Book. In the Metric GPSA Data Book from Figures 17-4 to 17-9 there are Mollier charts for several compounds. In the new English GPSA Data Book figure numbers are different. These plot enthalpy versus entropy at various temperature, pressures, etc. Similarly, the book "Thermo Properties of Hydrocarbons" ${ }^{16}$ gives this data. Also Maxwell, p. 98 onward, gives data on individual compounds.
For mixtures of gases at high pressure there is a problem. It can be shown that

$$
\left(\frac{\partial H}{\partial P}\right)_{T}=V-T\left(\frac{\partial V}{\partial T}\right)_{P}
$$

or with the compressibility factor
Equation 2-41

$$
\left(\frac{\partial H}{\partial P}\right)_{T}=-\frac{R T^{2}}{P}\left(\frac{\partial Z}{\partial T}\right)_{P}
$$

Katz on $P .133$ shows a plot of the change of enthalpy vs $P_{r}$ at various $T_{r}$ where $P_{r}$ is the reduced pressure and $T_{r}$ is the reduced temperature. A similar graph on $P .134$ and $P .136$ show the effect with slightly different parameters for enthalpies.

We are interested in mixtures which complicate the calculations. There are several methods. Here are two:

## Total Enthalpy Charts

In the GPSA Data Book there are a series of charts giving the enthalpies vs temperatures and mole weights at various pressures. Charts are given for liquids and gas at an ideal gas, 150 psia to 3000 psia. Similar figures and data are given in the metric GPSA book from 1400 to $20,800 \mathrm{kPa}$. These charts are generally good for gaseous mixtures. The basic assumption in that a mixture of hydrocarbons in vapour state has the same enthalpy of a single compound having the same mole weight as mixture. These charts are good for doing a quick calculation of heat duties.

## Curl and Pitzer Method

Another way to calculate the difference in enthalpy at high pressures is to follow the method of R.F. Curl and K.S. Pitzer ${ }^{20}$. This method is explained in detail in the GPSA Data Book, P. 17-1. It makes use of the acentric factor " w " and the use of factors for a simple fluid and the deviation from a simple fluid. The equation used is:

Equation 2-42

$$
H^{0}-H=R T_{C}\left[\left(\frac{H^{0}-H}{R T_{C}}\right)^{0}+\varpi\left(\frac{H^{0}-H}{R T_{C}}\right)\right]^{1}
$$

where:
$H^{\circ}$ is the ideal gas enthalpy
$H$ is enthalpy at the desired condition

$$
\begin{aligned}
& \left(\frac{H^{0}-H}{R T_{C}}\right)^{0}=\text { effect of pressure on a simple fluid } \\
& \left(\frac{H^{0}-H}{R T_{C}}\right)^{1}=\text { the correction for the deviation from a simple fluid for pressure. }
\end{aligned}
$$

The values for these items are given in the GPSA Data Book as follows:
$\mathrm{H}^{\circ}$ is plotted vs. temp. in Figure 17-1 \& 17-12
$\omega$ is given in Figure 16-1 (Pg. 16.3)
$\left(\frac{H^{0}-H}{R T_{C}}\right)^{0}$ for a simple fluid is given graphically on Figure 17-13.
$\left(\frac{H^{0}-H}{R T_{C}}\right)^{1}$ is given graphically on Figure 17-14.
To handle mixtures the procedure is to find the average $\omega$ by mole fraction
pseudo $T_{c}$ by mole fraction
pseudo $P_{c}$ by mole fraction
Then use these values in the equation given previously.
The example problem given below shows the application of the total enthalpy method.

## Example Problem 2.2

Calculate the duty required to chill 100 MMSCFD of a gas at 937 psig of the composition listed below from $40^{\circ}$ to $0^{\circ} \mathrm{F}$ using propane as a refrigerant.

| Component | Mole \% |
| :--- | :--- |
| $\mathrm{N}_{2}$ | 0.00 |
| $\mathrm{C}_{1}$ | 95.62 |
| $\mathrm{C}_{2}$ | 3.01 |
| $\mathrm{C}_{3}$ | 0.67 |
| $\mathrm{iC}_{4}$ | 0.18 |
| $\mathrm{nC}_{4}$ | 0.20 |
| $\mathrm{iC}_{5}$ | 0.09 |
| $\mathrm{nC} \mathrm{C}_{5}$ | 0.09 |
| $\mathrm{C}_{6}+$ | 0.14 |

## Solution

First find the amount of heat to be removed in the chillers. This is found by enthalpy calculations. Let's first see if there is much liquid condensed. Run a flash calculation at $0^{\circ} \mathrm{F}$. Assume $\mathrm{P}_{\mathrm{k}}=3000$ psia. The following is the result of a computer flash calculation:

| Comp. | Moles of Feed | $k^{937} 0$ | Moles Vapour | Moles Liquid | Mole Wt | P Mole Wt. of Vapour | P Mole Wt. Mix | P Mole Wt. Liquid |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}_{1}$ | 95.62 | 2.174 | 95.586 | 0.044 | 16 | 15.29 | 15.30 | 9.26 |
| $\mathrm{C}_{2}$ | 3.01 | 0.457 | 3.005 | 0.006 | 30 | 0.91 | 0.90 | 2.36 |
| $\mathrm{C}_{3}$ | 0.67 | 0.131 | 0.666 | 0.005 | 44 | 0.29 | 0.29 | 2.89 |
| $\mathrm{iC}_{4}$ | 0.18 | 0.065 | 0.177 | 0.003 | 58 | 0.10 | 0.10 | 2.29 |
| $\mathrm{nC}_{4}$ | 0.20 | 0.046 | 0.196 | 0.005 | 58 | 0.10 | 0.11 | 3.81 |


| $\mathrm{iC}_{5}$ | 0.09 | 0.018 | 0.086 | 0.004 | 72 | 0.06 | 0.06 | 3.79 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{nC}_{5}$ | 0.09 | 0.014 | 0.086 | 0.004 | 72 | 0.06 | 0.06 | 3.79 |
| $\mathrm{C}_{6}{ }^{+}$ | 0.14 | 0.004 | 0.119 | 0.004 | 84 | 0.11 | 0.12 | 4.42 |
|  |  |  | 99.923 | 0.076 |  | 16.92 | 16.94 | 32.61 |

Let us use the enthalpy chart method. We will use primarily the 1000 psia chart.
Number of Ibs. flowing:

$$
\frac{100,000,000}{379} \frac{16.94}{24}=186,235 \quad \mathrm{lbs} / \mathrm{hr}
$$

$\mathrm{H}_{40^{\circ} \mathrm{F}}=200 \mathrm{BTU}$ 's/lb. (Figure 17-12 GPSA Data Book)
$\mathrm{H}_{\mathrm{O}^{\circ} \mathrm{F}}=170$ for gas (Figure 17-14 GPSA Data Book)
$\mathrm{H}_{\mathrm{O}{ }^{\circ} \mathrm{F}}=-10$ for liquid (Figure 17-14 GPSA Data Book and mole wt of 32.6)
Heat Content Inlet

$$
\begin{aligned}
& =200(186,235) \\
& =37,247,000 \text { BTU/hr. }
\end{aligned}
$$

Heat Content Outlet (convert mole liquid a gas \% to mass \%)
Vapour $=170(186,235)(.9985)$
Liquid $=-10(186,235)(.0015)$
Total $=31,609,466$ B'IU's/hr
Duty (Difference) $=5,037,534$ BTU's/hr
Now let us do the problem in metric units.
Flow is $283,100 \mathrm{~m}^{3} /$ day
Pressure is 6556 kPa
Temperature is 4.4 C in and -17.7 out.
Kg flowing $=\frac{2.831,000}{23.6} \frac{16.94}{24}=84670 \mathrm{~kg} / \mathrm{hr}$
$=84670 \mathrm{~kg} / \mathrm{hr}$
at 6200 kPa - Figure 17-11 SI GPSA Data Book
$\mathrm{H}_{4.4}=500 \mathrm{KJ} / \mathrm{kg}$ gas
$\mathrm{H}_{-17.7}=440 \mathrm{KJ} / \mathrm{kg}$ gas
$\mathrm{H}_{-17.7}=-105 \mathrm{KJ} / \mathrm{kg}$ liquid $(\mathrm{MW}=32.6)$
Heat Content Inlet
$84670(500)=42,335,000 \mathrm{KJ} / \mathrm{hr}$
Heat Content Out:

$$
\begin{aligned}
\text { Vapour } & =440(84670)(.9985) \\
& =37,198,918 \mathrm{~kJ} / \mathrm{hr}
\end{aligned}
$$

Liquid $\quad=-105(84670)(.0015)=-13,335 \mathrm{~kJ} / \mathrm{hr}$
Total $=37,185,583 \mathrm{~kJ} / \mathrm{hr}$
Duty (Difference) $=5,149,417 \mathrm{~kJ} / \mathrm{hr}$
= 1440.4 KW

### 2.3.3 Correlation Methods

All the various correlations i.e. BWRS, Soave, Redlich Kwong, Prausnik, etc. give enthalpy data for each individual mixture. These of course are more accurate and should be used for detailed design.
A study of J. Powers (presented at the 1971 Annual Convention of the NGPA) showed the results of 8 different enthalpy correlations at temperatures from $-250^{\circ} \mathrm{F}$ to $+250^{\circ} \mathrm{F}$
$-156^{\circ} \mathrm{C}$ to $+121^{\circ} \mathrm{C}$ ) and at pressures from 0 psig to 2000 psig ( 101 to 13890 kPa ). Here are the average deviations of the values of some of the important correlations.
\% Deviation from Actual Value

|  | \% Deviation from Actual Value |
| :--- | :--- |
| Power's Generalized Correlation | 1.57 |
| Rice Property III | 1.60 |
| Modified BWR | 1.67 |
| CPY | 3.46 |
| Johnson \& Colver | 2.04 |
| NGPA - old values | 11.88 |
| NGPA - new values | 2.00 |

The newer Soave, Peng Robinson correlations give much better accuracy.
We have been discussing essentially the enthalpies of gas. We should also discuss liquids and mixtures of liquids. For systems that remain liquid the difference in enthalpy between two temperatures is found by multiplying $\mathrm{C}_{\mathrm{p}}\left(\mathrm{T}_{1}-\mathrm{T}_{2}\right)$ or subtracting the enthalpies. Figures 17-14 and 17-15 of the GPSA Data Book gives enthalpies of saturated liquids. When we have liquids and vapours occurring together we have to take into account the heat accompanying a change of phase or the latent evaporization or condensation. Latent heats for pure compounds can be found from the thermo property tables or the Mollier diagrams given in the GPSA Data Book from the data in Maxwell, p. 94 to 127.
To handle the case of compounds at conditions above their critical points but still in a liquid, use the data shown in Maxwell for gases in solution, shown in Figure 2.7.


Figure 2.7: Enthalpy of Gases in Solution
Therefore- the procedure when we have either vapourization or condensation occurring in an exchanger is to calculate composition of vapour and liquid at outlet condition as well as at the inlet conditions. Then proceed as follows:

If you are chilling a rich gas in which there is lots of condensation and you wish to find heat duty:

1. Find enthalpy at inlet temperature and pressure
2. Run a flash calculation at outlet temperature and pressure to see amount and composition of liquid and gas phases. Calculate the weight fraction of liquid and gas present.
3. Calculate enthalpy of each phase at outlet conditions using compositions found from 2.
4. Multiply each enthalpy by the wei~it fraction of the appropriate phase and add enthalpies together.
5. Subtract enthalpy in 1) from 4) and multiply by lbs/hr flow rate to find duty in BTU' s per hour.

### 2.3.4 Processes Using Enthalpy

Joule Thomson Expansion. This is expressed by the equation
Equation 2-43

$$
\mu=\left(\frac{\partial T}{\partial P}\right)_{H}
$$

where:

$$
\mu=\text { Joule-Thomson coefficient }
$$

This type of expansion occurs through a throttling valve, i.e. a well choke or a refrigeration chiller feed valve. The process occurs at constant enthalpy. Therefore, the Mollier type diagram can be used to find the temperature on a change of pressure. Also a chart such as Figure 15-23 of the GPSA Data Book on page 15-17, can be used. Further, National Tank has published a good chart
on thAs, as shown in $\mathrm{H}_{2} \mathrm{~S}$ are present in the gas. This has been discovered by some field work by G. Palmer and others of Maloney Steelcraft Ltd.

### 2.3.5 Process Using Entropy

Adiabatic compression or expansion takes place at constant entropy. Thus the Mollier chart can also be used in this regard. See pg. 17-19 of GPSA Data Book for further explanation of this calculation. This is particularly important in compressor and expander calculations.

### 2.4 Heats of Combustion

The next property to mention is the heating value or the heat of combustion. These are two kinds of heating values:
6. Gross Value - This is the value obtained by measuring the heat formed and cooling the products of combustion to 600F including condensing the water vapour. A very important part of the calculation of this value is the reference state, i.e. BTU's/lb weight in a vacuum or air, whether it is ideal gas or liquid or whatever. The GPSA has set up a standard for this calculation for mixture. The ideal gas heating value is calculated by the equation:

Equation 2-44
$H_{\text {ideal }}=\sum_{i} x_{i} H_{i}$
where $\mathrm{x} 1, \mathrm{x} 2 \ldots . \mathrm{x}$, , are the mole fraction of each component. $\mathrm{H} 1, \mathrm{H} 2 \ldots . \mathrm{H}$,, are the ideal gas heating values from Table 2.6 for each component. The real gas heating value H is set by the equation:

Equation 2-45

$$
H_{r}=\frac{H_{\text {ideal }}}{Z}
$$

$Z$ is found from
Equation 2-46

$$
Z=1-\left(x_{1} \sqrt{b_{1}}+x_{2} \sqrt{b_{2}}+\ldots \ldots \ldots+x_{n} \sqrt{b_{n}}\right)^{2}
$$

A correlation for H if present is also given in the GPSA Data Book. Data for equation 2-45 is also found in Table 2.8 or Metric values in 2.9. GPSA Standard 2172-72 explains this calculation further as does page 16-34 of the GPSA Data Book. Gas specific gravity can also be calculated using equation 2-45.

Net Value - In this case the water is not considered to be condensed. In most applications in the gas industry the gross heating value is used. In older gas contracts the gross value is stated as saturated with water vapour at $60^{\circ} \mathrm{F}$ and 30 Hg pressure. To find the heating value in this case multiply the gross dry basis by 0.9825 . A calorimeter on pipelines measures the heat content as saturated with water vapour. The newer contracts just take a continuous sample, analize same and then calculate the gross heating value using the latest GPA data.

Table 2.8: Properties of Natural Gas Components (Imperial)

| Component | Ideal Gas Specific Gravity | Ideal Gas Heating Value ${ }^{\text {a }}$ Btu/cf at $60^{\circ} \mathrm{F}, \mathbf{1 a t m}(\mathbf{7 6 0} \mathrm{mm}$ $\mathrm{Hg})$ | Comppressibility Factor ${ }^{\text {b }} \mathbf{Z}$, at $60^{\circ} \mathrm{F}, 1 \mathrm{~atm}$ | Summation Factor, $\sqrt{b}$ |
| :---: | :---: | :---: | :---: | :---: |
| Hydrocarbons |  |  |  |  |
| Methane | 0.5539 | 1009.7 | 0.9981 | 0.0436 |
| Ethane | 1.0382 | 1768.8 | 0.9916 | 0.0917 |
| Propane | 1.5225 | 2517.5 | 0.9820 | 0.1342 |
| Isobutane | 2.0068 | 3252.7 | 0.9696 | 0.1744 |
| n~Butane | 2.0068 | 3262.1 | 0.9667 | 0.1825 |
| Isopentane | 2.4911 | 4000.3 | 0.9482 (f) | 0.2276 |
| n -Pentane | 2.4911 | 4009.6 | 0.9435 (f) | 0.2377 |
| n-Hexane | 2.9753 | 4756.2 | 0.920 (f) | 0.283 |
| n-Heptane(g) | 3.4596 | 5502.8 | 0.920 (f) | 0.283 |
| Hexanes plus | (h) | (h) | (h) |  |
| Nonhydrocarbons |  |  |  |  |
| Air | 1.0000 | ---- | 0.99959 | 0.0202 |
| Carbon Dioxide | 1.5195 | ---- | 0.99432 | 0.0640 (d) |
| Carbon Monoxide | 0.9671 | 321.37 | 0.99953 | 0.0217 |
| Helium | 0.1382 | ---- | 1.00048 | -0.017 (e) |
| Hydrogen | 0.0696 | 325.02 | 1.00060 | ---- |
| Hydrogen Sulfide | 1.1765 | 637 (c) | 0.9903 | 0.0985 |
| Nitrogen | 0.9672 | ---- | 0.99973 | 0.0164 |
| Oxygen | 1.1048 | ---- | 0.99927 (i) | 0.0270 |

a) NGPA Publication 2145-71: "Physical Constants of Paraffin Hydrocarbons and Other Components of Natural Gas" for hydrocarbons; IGT Bulletin 32 for nonhydrocarbons.
b) ASTM DS 4A: "Physical Constants of Hydrocarbons C1 to C,~5" for C, - C4; IGT Bulletin 32 for other components.
c) For combustion to gaseous SO 2 .
d) Pseudo value for mixtures containing less than 20 \% CO2.
e) Pseudo value for mixtures containing less than $1 \% \mathrm{He}$.
f) For the hypothetical gas.
g) Applicable for mixtures containing less than 0.05 percent heptanes.
h) Properties of hexanes plus fractions may vary widely, and should be determined, by a mutually agreeable method.
i) AGA Report No. 3, 1969.

Note: To prevent confusion, note that Ideal Specific Gravities shown in IGT Bulletin No. 32 are based on 1961 molecular weights and referenced to real air; values in this Table are based on 1969 molecular weights and ref evenced to ideal air.

Table 2.9: Properties of Natural Gas Components (Metric)

| Component | Ideal Gas Relative Density | Ideal Gross Heating Value ${ }^{\text {a }}$ $\mathrm{Mj} / \mathrm{m}^{3} @ 15^{\circ} \mathrm{C}, 101.325 \mathrm{kPa}$ (abs) | Comppressibility Factor ${ }^{\text {b }}$ Z <br> @ $15^{\circ} \mathrm{C}, 101.325 \mathrm{kPa}$ (abs) | Summation Factor, $\sqrt{b}$ |
| :---: | :---: | :---: | :---: | :---: |
| Hydrocarbons |  |  |  |  |
| Methane | 0.5539 | 37.694 | 0.9981 | 0.0436 |
| Ethane | 1.0382 | 66.032 | 0.9915 | 0.0922 |
| Propane | 1.5225 | 93.972 | 0.9810 | 0.1378 |
| Isobutane | 2.0068 | 121.426 | 0.9665 | 0.1830 |
| n~Butane | 2.0068 | 121.779 | 0.9641 | 0.1895 |
| Isopentane | 2.4911 | 149.319 | 0.948 (f) | 0.2280 |
| n-Pentane | 2.4911 | 149.654 | 0.942 (f) | 0.2408 |
| n-Hexane | 2.9753 | 177.556 | 0.910 (f) | 0.3000 |
| n-Heptane(g) | 3.4596 | 205.431 | 0.852 (f) | 0.3847 |
| Hexanes plus | (h) | (h) | (h) |  |
| Nonhydrocarbons |  |  |  |  |
| Air | 1.0000 | ---- | 0.9996 | 0.0200 |
| Carbon Dioxide | 1.5195 | ---- | 0.9943 | 0.0640(d) |
| Carbon Monoxide | 0.9671 | ---- | 0.9995 | 0.0224 |
| Helium | 0.1382 | ---- | 1.0005 | -0.017 (e) |
| Hydrogen | 0.0696 | 12.091 | 1.0006 | ---- |
| Hydrogen Sulfide | 1.1765 | 23.791(c) | 0.9903 | 0.0985 |
| Nitrogen | 0.9672 | ---- | 0.9997 | 0.0173 |
| Oxygen | 1.1048 | ---- | 0.9993 (i) | 0.0265 |

a) GPSA Engineering Data Book (SI), Fig. 16-1.
b) For combustion to gaseous 502 .
c) Pseudo value for mixtures containing less than $20 \% 002$.
d) Pseudo value for mixtures containing less than $1 \% \mathrm{He}$.
e) For the hypothetical gas.
f) The error in calculating heating value is less than $0.05 \%$ when the gas contains less than $1 \%$ of C6 paraffin.
g) and C, aromatics and less than $0.05 \%$ of $01+$ paraffins and C9+ aromatics.
h) Properties of hexanes plus fractions may vary widely, and should be determined by a mutually agreeable method.
i) AGA Report No.3,1969.

Note: lb prevent confusion, note that Ideal Specific Gravities (Relative Densities) shown in LGT Bulletin No. 32 are based on 1961 molecular masses and referenced to real air; values in this Table are based on 1969 molecul, ar masses and referenced to ideal air.


Figure 2.8: Natural Gas Expansion-Temp. Reduction Curve Based on .7 Sp. Gr. Gas

### 2.5 Viscosity

Another important property is viscosity. It is defined by:

$$
\mu=\frac{\text { Shearing Stress }}{\text { Rate of Shear Stress }}
$$

It is the internal friction in a fluid that reduces fluid flow. Viscosity is measured normally in metric units of centipoise. Multiply by .000672 to convert to British Units. (lb/ft sec.)

### 2.5.1 Liquids

Data for liquids is given on Fig. 16-23 of the GPSA Data Book. Here the viscosity in centipoise is plotted versus temperature. A much more extensive discussion is given in the chapter on viscosity in Maxwell ${ }^{6}$. The conversion from absolute viscosity to other types of viscosity are given in the GPSA Data Book, i.e. Kinematic Saybolt, etc. Except at very high values pressure does not affect viscosity. The viscosity of liquid sulphur is quite special; it increases with temperature. Figure 2.9 shows the data.

### 2.5.2 Gases

Figure 16-27 (Fig. 16-25 in metric version) of the GPSA Data Book gives the viscosity of gases at low pressure (essentially atmos.) 7. for hydrocarbons. Similarly Katz ${ }^{7}$ gives data for individual compounds on Pg. 169, 170. Note that $\mathrm{N}_{2}, \mathrm{CO}_{2}, \mathrm{H}_{2} \mathrm{~S}$ air are more viscous at same temperature as compared to hydrocarbons.
The viscosity of gas at high pressure can be found by use of Fig. 16-24 of GPSA Data Book which plots temperature vs. viscosity vs. gravity at different pressures. Another way is to calculate the reduced temperature and reduced pressure and use. Fig. 16-28 in the GPSA Data Book which gives a ratio $\mu$ at high pressure vs $\mu$ atmospheric pressure.


Figure 2.9: Effect of Temp. on Viscosity of Molten Sulphur


Figure 2.10: Thermal Conductivity of Normal Paraffinic Hydrocarbons

### 2.6 Thermal Conductivities

Liquids - Hydrocarbon liquids conductivity is given in Figure 2.10. Also some data for $\mathrm{H}_{2} \mathrm{O}$ is given in Maxwell, p. 214.

Gases - Maxwell, p. 215 and 216 gives data on miscellaneous gases and hydrocarbon gases vs MW. Also Katz, Figure 4-119, p. 185 gives data at low pressures (also this is given in GPSA Data Book, Fig. 16-29). At high pressures, Lenoir, Junk and Cumming ${ }^{15}$, have developed charts similar to that used for viscosity. They give a thermal conductivity ratio vs $P_{r}$ and $T_{r}$ where thermal conductivity ratio is:

$$
\frac{k \text { at high pressure }}{k \text { at atmospheric pressure }}
$$

from 16.29

This is shown as Figure 16.31 in the GPSA Data Book.

### 2.7 Surface Tension

Data on surface tension for hydrocarbons is given in Figure 16-31. (Figure 16-29 in the metric version) of the GPSA Data Book or p. 127 of Katz. In the GPSA Data Book it is calculated from the equation:

Equation 2-47

$$
\sigma^{0.25}=\frac{P}{M}\left(d_{1}-d_{V}\right)
$$

Where:
ó = surface tension
$P=$ parachor from Figure 16-34
$M=$ molecular weight of compound
$d_{\mathrm{L}}=$ density of liquid at temperature of system
$\mathrm{d}_{\mathrm{v}}=$ density of vapour at temperature of system
Also, on P. 16-29 and 16-34 of the GPSA Data Book a method for adjusting for high pressure (Weimag and Katz method) and mixtures is given.

### 2.8 Molecular Weights of Hydrocarbons (MW)

Sometimes it is desirable to find MW of condensate. This can be done from API gravity and mean average boiling point which is determined from an ASTM distillation. See Figure 16-18 of the GPSA Data Book.

## Problems

7. A gas of the composition given below is to be recycled to recover the sulphur, condensate and Ipg's. The Energy Resources Conservation Board has stated that $60 \%$ of the volume of raw gas removed must be replaced by the recycled sweet pipeline gas produced from a
processing plant that is built for extracting the products produced.
Determine the amount of make-up gas that must be supplied to the facility to handle this requirement or the amount of gas that is available for sale.

Also, determine quantity of sulphur in long tons per day, condensate in barrels per day, butane in barrels per day and propane in barrels per day recovered by the plant.

## Data

a) Raw gas flow to the plant is 300 MMSCFD (at 14.4 psia and $60^{\circ} \mathrm{F}$ as the base measuring condition).
b) The reservoir pressure is 4300 psia - sweet gas must be returned at that pressure.
c) The design plant recovery efficiencies are:

| Sulphur | $95 \%$ |
| :--- | :--- |
| Condensate | $100 \%$ |
| Butanes | $100 \%$ |
| Propane | $85 \%$ |

d) The fuel gas required for plant operation is equivalent to $2 \%$ of the raw gas feed but sweet gas is used.
e) The gas analysis is:

| Component | Mole \% |
| :--- | :--- |
| $\mathrm{N}_{2}$ | 0.50 |
| $\mathrm{H}_{2} \mathrm{~S}$ | 17.06 |
| $\mathrm{CO}_{2}$ | 2.94 |
| $\mathrm{C}_{1}$ | 57.50 |
| $\mathrm{C}_{2}$ | 9.80 |
| $\mathrm{C}_{3}$ | 3.94 |
| $\mathrm{iC}_{4}$ | 1.06 |
| $\mathrm{nC}_{4}$ | 1.96 |
| $\mathrm{iC}_{5}$ | 0.74 |
| $\mathrm{nC}_{5}$ | 0.90 |
| $\mathrm{C}_{6}$ | 0.55 |
| $\mathrm{C}_{7}+$ | 3.05 |

f) The raw gas reservoir temperature is $200^{\circ} \mathrm{F}$.

The heating load of a processing plant is made up of 4 furnaces. The process duty on each of the furnaces is as follows. The efficiency of each is also given.

| Furnace No. | Process Heating Required BTU/hr | Design Efficiency \% * |
| :--- | :--- | :--- |
| 1 | $10 \times 10^{6}$ | 70 |
| 2 | $5 \times 10^{6}$ | 65 |
| 3 | $25 \times 10^{6}$ | 75 |
| 4 | $40 \times 10^{6}$ | 75 |

[^7]Gas is available at $\$ 1.25 / \mathrm{MMBTU}$ on an interruptable basis and $\$ 1.50 / \mathrm{MMBTU}$ on a firm basis. The fuel that is used as a standby is n-butane which can be sold for $25 \phi / \mathrm{US}$ gal when it is not used as fuel.

How many days interruption could the process plant stand per year and still break even if it used interruptable gas instead of firm gas?
A well produces gas at 25 MMSCFD. The wellhead pressure is 2000 psig at this flow rate and it is at $75^{\circ} \mathrm{F}$. The gas is delivered from the wellhead through a heater to a pipeline that operates at 1200 psig. You are to determine the heat duty of the high pressure heating coil in BTUs per hour. The sketch below shows the flow scheme.


The gas is sweet and the gravity of the gas is 0.7 .
A gas of the following composition is to be processed for ethane and propane plus recovery. The amount of gas that is available is 300 MMSCFD (at $60^{\circ} \mathrm{F}$ and 14.696 psia ). The exit gas from the plant must be returned at 985 BTU 's/SCF as measured by a Thomas Calorimeter.

| Component | Mole \% |
| :--- | :--- |
| $\mathrm{N}_{2}$ | 3.5 |
| $\mathrm{C}_{1}$ | 83.2 |
| $\mathrm{C}_{2}$ | 10.3 |
| $\mathrm{C}_{3}$ | 1.8 |
| $\mathrm{iC}_{4}$ | 0.3 |
| $\mathrm{nC}_{4}$ | 0.4 |
| $\mathrm{C}_{5}+$ | 0.5 |

Determine the barrels per day of pure ethane that can be removed. Assume that all the $\mathrm{C}_{3}+$ is removed from the incoming gas during the process. Assume fuel gas is supplied from down stream of plant (i.e. the plant residue gas).

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## Reading List

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### 3.0 Phase Behaviour of Natural Gas Systems

- What are Phases?
- The Phase Rule, PV, PT and PVT
- Diagrams
- Retrograde Phenomena
- Binary and Complex Systems
- Non-ideal Systems


### 3.1 What is a Phase?

A single continuous media containing one or more substances in which the relation between temperature, pressure and volume can be expressed by a continuous equation is a phase. Another way is to use the Clausius Clapeyron Equation which explains how a phase is changed. This equation can be expressed as follows:

$$
\frac{d P}{d T}=\frac{\Delta H}{T \Delta V}
$$

where:
$\Delta \mathrm{V}$ is the change of volume
$\Delta \mathrm{H}$ is the heat content of the phase change
$P$ is the pressure at the phase change
T is the temperature at the phase change
Thus a phase change occurs when there is a finite change in volume and heat content when the pressure and temperature are constant.

### 3.2 What are Some Phases and Their Features?

## Gases

Distinguishing feature is that it occupies the space of container and it can be compressed easily.

## Liquid

It takes the shape of the bottom part of a container. Also it is hard to compress; only under extreme pressure.

## Solid

It has definite shape and is not compressible. We can have several liquid and solid phases, however not more than one gas phase. In the gas industry we are lucky in that we only need to consider liquid and gas phases. We do have the special case of elemental sulphur in gases containing amounts of $\mathrm{H}_{2} \mathrm{~S}$. This is considered later in this section.

### 3.3 Why Study About Phases?

We encounter many physical conditions in handling fluids in which two phases are present, i.e.
a) Fluid flow in gathering lines
b) Distillation
c) Absorption
d) Heat transfer operations, i.e. vaporization.

In studying about phases we initially will try to understand visually what happens between phases and later, in another section (Vapour- liquid equilibria) set up mathematical relationships to predict phase conditions.

### 3.4 History

This is an old subject. Some of the more important pioneers are:
a) Faraday, who in 1845 worked out phase diagrams for substances such as $\mathrm{N}_{2}, \mathrm{H}_{2} \mathrm{~S}$, $\mathrm{SO}_{2}, \mathrm{CO}_{2}$, etc.
b) Andrew, who in 1869 noted the continuity of gas and liquid phases at high pressures and temperatures. This led to the concept of the critical point.
c) Gibbs, who in 1876 enunciated the phase rule.
d) Kuenen, who in 1892 discovered the retrograde condensation phenomena.

### 3.5 Single Component Systems

Let us consider a single component, three dimensional diagram. Figure 3.1 represents such a diagram. The diagram shows when a single phase and when two phases are present.


Surface A Solid and Liquid in equilibrium.
Surface B Liquid and Vapour in equilibrium.
Surface C Solid and Vapour in equilibrium.
SLG Three phases present.

## Figure 3.1: Three Dimensional Diagram for a Single Component

Also, the case of three phases present is shown as the line SLG. Let us consider projections of this model onto a two-dimensional surface. We have two normal types of diagrams.
These are:
PT diagrams (Figure 3.2) in which planes of constant volumes are taken.
PV diagrams (Figure 3.3) in which various lines of constant temperature are taken.
Note: V is specific volume (i.e. volume of one unit of Mass).


Figure 3.2: PT Diagram - Single Component
When going from $A$ to $B$ to $C$ the phases are Solid, Liquid, Gas. When going from $D$ to $E$ the phases are Solid-Gas. Some examples of solid, gas systems are:
$\mathrm{AlCl}_{3}$
Phthalic anhydride
lodine
$\mathrm{CO}_{2}$


Figure 3.3: PV Diagram - Single Component

- If we follow $T_{1}$ there is no change of phase.
- If we follow $T_{2}$ we go from liquid to liquid plus vapour to finally vapour.
- If we follow $T_{3}$ we go from solid to solid plus liquid to liquid plus vapour to vapour.
- If we follow $T_{4}$ we go from solid to solid plus vapour to vapour.

Also consider the conditions of vessel containing a certain weight of material with temperature $\mathrm{T}_{3}$. It would contain liquid of specific volume, $b$, and vapour of specific volume, $a$.
Note: lines of constant temperature are called isotherms.

### 3.6 Critical Points

Please refer to the PV diagram (Error! Reference source not found.). When reducing the pressure along the curve ACB no change of phase occurs. Also, you remember that in Figure 3.2 the liquid vapour line stopped at a high pressure and temperature.
The point C in PV diagram and the top point on the liquid vapour line in PT diagram is called the critical point. It is the unique point for substance where the liquid and gas phase become identical. Each individual substance has a definite critical temperature and critical pressure. There is also a critical temperature and pressure for mixture which will be discussed later.
Here are some data on common critical points. Also, the boiling point is given:
Table 3.1: Critical Data (Imperial)

|  | Critical Pressure lb/in2 abs | Critical Temperature ${ }^{\circ} \mathrm{R}$ | Boiling Point ${ }^{\circ} \mathrm{F}$ |
| :---: | :---: | :---: | :---: |
| Methane | 668 | 343 | -259 |
| Ethane | 708 | 590 | -127 |
| Propane | 616 | 666 | -44 |
| i Butane | 529 | 735 | 11 |
| n Butane | 551 | 766 | 31 |
| i Pentane | 490 | 829 | 82 |
| $n$ Pentane | 489 | 846 | 97 |
| $n$ Hexane | 437 | 914 | 156 |
| $n$ Heptane | 397 | 973 | 209 |
| n Octane | 361 | 1024 | 258 |
| Carbon dioxide | 1071 | 548 | -109 |
| Hydrogen Sulphide | 1306 | 673 | -77 |
| Nitrogen | 493 | 228 | -320 |

Table 3.2: Critical Data (Metric)

|  | Critical Pressure kPa |  | Critical Temperature ${ }^{\circ} \mathbf{K}$ |
| :--- | :---: | :---: | :---: |
| Methane | 4605 | 190.5 | Boiling Point ${ }^{\circ} \mathbf{C}$ |
| Ethane | 4881 | 305.3 | -161.5 |
| Propane | 4247 | 369.8 | -88.6 |
| i Butane | 3647 | 408.0 | -42.1 |
| n Butane | 3799 | 425.0 | -11.7 |
| i Pentane | 3378 | 460.8 | -0.5 |
|  |  |  | 27.9 |

n Pentane
n Hexane
n Heptane
n Octane
Carbon dioxide
Hydrogen Sulphide
Nitrogen

| 3371 | 469.6 | 36.1 |
| :---: | :---: | :---: |
| 3013 | 507.7 | 68.7 |
| 2737 | 540.0 | 98.4 |
| 2487 | 569.2 | 125.7 |
| 7384 | 304.0 | 78.2 |
| 9004 | 373.0 | -60 |
| 3399 | 120.5 | -195.3 |

Note: The boiling point is the temperature at which the vapour and liquid phases are in equilibrium when the vapour pressure is one atmosphere.

### 3.7 Vapour Pressure

In Figure 3.2 the line between surfaces $B$ and $C$ is the vapour pressure curve and gives the pressure of single component above a pure liquid of that component at the temperature specified.

### 3.8 Summary - Single Component

a) A functional relationship of the form

Equation 3-2
$f(P, T, V)=0$
exists for single component systems. The surface which this relationship describes has dis continuities in it because of the existence of vapour-liquid, solid-liquid, and solid-vapour equilibrium.
b) The triple point is the unique pressure and temperature where solid, liquid and vapour can all exist in equilibrium for a single component system.
c) The critical point is the unique condition where the properties of the liquid and vapour phases become identical.
d) The salient features of the $\mathrm{P}-\mathrm{V}-\mathrm{T}$ surface may be conveniently projected onto $\mathrm{P}-\mathrm{T}$ and $\mathrm{P}-\mathrm{V}$ planes to facilitate both qualitative and quantitative representation.
e) An isotherm represents the intersection between the P-V-T surface and an isothermal plane.
f) The boiling point of a pure material is the temperature where the vapour pressure is one atmosphere.
g) The vapour pressure of a material is the pressure where two or more phases may co-exist at any fixed temperature.
h) The terms liquid, vapour and solid lose their significance unless at least two phases are present.

## $3.9 \quad$ The Phase Rule

Before proceeding to more complicated systems we should review the phase rule which Gibbs first enunciated in 1876. This rule applies to systems in equilibrium and states that the number of
components plus 2 equal the number of phases plus the degrees of freedom (or the number of independent variables to determine the system)

$$
C+2=P+F
$$

Where:

$$
\mathrm{C}=\text { components }
$$

$\mathrm{P}=$ number of phases
$\mathrm{F}=$ number of degrees of freedom or number of variables required-to determine-system.
Some examples are:
a) For water boiling (two phases present)
$1+2=2+F$
Thus it is necessary to specify a variable such as temperature or pressure to define the system. Thus by specifying different temperatures a vapour pressure curve can be determined.
b) For a system of methane and ethane as a liquid, three degrees of freedom are needed to define the system.

$$
\begin{aligned}
& 2+2=I+F \\
& F=3
\end{aligned}
$$

Thus you have to specify the pressure, temperature and the composition of the solution to define the system.

### 3.10 Systems of More Than One Component

A qualitative study of the phase behaviour of single component systems has revealed all of the essential features which are encountered even in complex systems. The concept of two or more phases co-existing, of vapour pressure, of the critical point, and of a continuous single phase fluid region is applicable to any system regardless of its complexity. The fundamental difference between single component systems and complex systems is that every time we add one more component we gain one additional degree of freedom. That is we may arbitrarily specify one additional variable and for a binary system, the functional relationship becomes:

$$
f(P, T, V, X)=0
$$

where:
$X$ is the composition.
It is obvious from this relation that a three dimensional model can no longer be used to pictorially represent the complete behaviour of even a vinary system. Any three dimensional representation of the behaviour of a system containing more than one component will of necessity be capable of showing the values of only three of the possible variables. The choice is arbitrary, but the most common practice is to select pressure, temperature, and composition. Every point represented on such a diagram will have a particular specific volume associated with it, as determined by the functional relationship above, but the coordinates of volume will not be represented on the diagram.
Figure 3.4 shows a schematic representation of the P-T-X behaviour of a typical binary system including part of the vapour-liquid equilibrium region. The region of solid formation has been
excluded because of the complexity of the diagram and because it is seldom pertinent in gas processing studies.

The characteristic features of the diagram are somewhat more difficult to visualize than they were in the P-V-T diagram for a single component. This is because the only lines one sees in space are those formed when two surfaces intersect non-tangentially. On a P-V-T surface this occurs every time the single phase region intersects a two phase region, but on a P-T-X diagram it never occurs at pressures and temperatures in the vapour liquid region. It will be appreciated that the additional degree of freedom means that what were points for one component are lines for two components; what were lines have become surfaces; and what were surfaces have become volumes. In this way the saturated liquid line of Figure 3.3 has
become a saturated liquid surface M in Figure 3.4 and the saturated vapour line has become a saturated vapour surface $N$. These two surfaces, commonly called the bubble point surface and the dew point surface, form the upper and lower boundaries of a vapour-liquid volume. This two-phase volume is terminated at the left side of the figure by the vapour pressure curve of pure A denoted by the line 6-7. (It will be noted that since volume has been omitted in this diagram, the curve 6-7 is really the projection of the vapour liquid surface for $A$ as seen in Figure 3.1). Similarily, the vapour pressure curve 8-9 for pure $B$ terminates the region at the right side of the diagram.
The critical point has become a critical line or critical locus for the binary system. This locus, indicated by 7-10-9, terminates the bubble and dew point surfaces at the high temperature side of the diagram.
The diagram is terminated on the P -x plane by an arbitrarily isothermal plane which leaves its trace 6-11-8 on the bubble point surface and 6-12-8 on the dew point surface.
Let us consider PT diagrams. Figure 3.5 on P .14 shows the diagram for a two component system with only liquid and vapour present.
Figure 3.6 is the PT phase diagram for a mixture of a fixed composition. In this figure let us consider going from point 1 to point 4 by increasing the pressure. At point 2 condensation starts (dew point). It continues until point 3 is reached where total condensation is experienced (bubble point), then to 4.
Another useful diagram is the TX diagram (Figure 3.7), i.e. where the pressure is constant.


Figure 3.4: Schematic Representation of P-T-x Behavior of a Typical Binary System


Figure 3.5: PT Diagram - Two Components (A \& B), Different Composition A PT diagram for constant composition can be shown as:


Figure 3.6: PT Diagram - Two Components, Constant Composition


Figure 3.7: Temperature Composition Diagram
In Figure 3.7 the top curve is the composition of the vapour and bottom curve is composition of liquid. At temperature $T_{1}$ the gas composition is $X_{G}$ and the liquid composition is $X_{L}$. This shows how two components can be separated by distillation.

We also have a useful representation by the composition diagram with P and T constant. This is shown in Figure 3.8.


Figure 3.8: Vapour Liquid Composition Diagram
This figure is also important in distillation.
Please note that Figures 3.7 and 3.8 are for ideal solutions. When non-ideal solutions occur, such conditions as maximum or minimum boiling point for mixtures occur. For example Figure 3.9 shows a temperature composition for a minimum boiling point separation.
Also note that the critical point for a binary system is not necessarily the highest temperature or pressure where two phases can exist together for any composition. The critical point is formed by the intersection of the dew point and bubble point surfaces. The highest pressure at which two phases can exist together is the cricondenbar and the maximum temperature at which two phases exist is the cricondentherm.


Figure 3.9: Non-ideal Temperature Composition Diagram

### 3.11 Definitions

Before considering further multi-component systems, let us consider a few definitions. These are:

## Bubble Point

This is defined as the temperature at which the first sign of vapour appears. It varies, of course, with pressure and is the same as the boiling point for a single component system at pressure of the system.

## Dew Point

This is defined as the temperature at which condensing takes place. This varies with pressure.
With a pure substance the bubble point and dew point are the same, but not so with a mixture. i.e. Take a mixture of

| Methane | $20 \%$ |
| :--- | :--- |
| Ethane | $20 \%$ |
| Propane | $20 \%$ |
| Isobutane | $10 \%$ |
| Butane | $10 \%$ |
| Pentane | $20 \%$ |

If the bubble point is determined it will be close to the boiling point of methane at the pressure of the system, while the dew point will be closer to the boiling point of pentane at the pressure of the system. For a system to totally condense it is at its bubble point and for a system to totally evaporate the system has to be at its dew point.

### 3.12 Multicomponent Systems

It is not possible to graphically represent the detailed behaviour of systems containing more than three components. However, the essential features may be depicted for systems of a fixed composition on P-T coordinates, much as in the case of a binary system; or in the case of systems
of variable composition, on a ternary diagram using pseudo pure components, that is, components made up of mixtures of selected components from a complex system. For example, for a system containing $\mathrm{C}_{1}$ to $\mathrm{C}_{5}$, one component could be $\mathrm{C}_{1}$, one could be $\mathrm{C}_{2}$ and $\mathrm{C}_{3}$, and the third could be $\mathrm{C}_{4}$ and $\mathrm{C}_{5}$. For obvious reasons, this latter technique is not rigorous, but nevertheless it is sometimes useful for a qualitative description of certain phase behaviour phenomena.

Figure 3.10 is an important diagram which depicts a multi-component system with a fixed composition.

Normally, on increasing the temperature of a liquid at constant pressure from $A$ to $D$ the bubble point is reached first then vapourization continues with increasing amounts being formed until 100\% vapour is formed at $C$. At constant temperature, on decreasing the pressure from $B$ to $E$, a continuing increased amount of vapour is formed.


I
Figure 3.10: Retrograde Phenomena I

### 3.13 Retrograde Phenomena

Let us next consider the case in Error! Reference source not found., when the pressure is reduced from point $X$ to point $Z$. At $W$ liquid begins to form on pressure reduction and continues until $R$ is reached where the maximum amount of liquid is developed, approximately $30 \%$, then a continued reduction of pressure causes the liquid to vapourize until the point $Y$ is reached when a $100 \%$ vapour again occurs. This phenomena is retrograde condensation and is particularly important in natural gas reservoirs, as most higher pressure gas rich reservoirs exhibit this phenomena. Thus liquids will drop out in the reservoir when the pressure is decreased and may be lost. These liquids may be re-evaporated by dry gas if a cycling scheme is used. Havlena ${ }^{1}$ et al, discuss this in some detail.
The reverse of the above procedure, i.e. going from $Z$ to $X$, is called retrograde evaporation.
Another phenomenon is, if the pressure reduction hits right at the critical temperature of the mixture, then at that point $50 \%$ of the fluid liquefies and then progressively evaporates.

Also, if the critical point is located as in Figure 3.11, between R and C an increase of temperature at constant pressure can cause liquid to drop out. This is called isobaric retrograde condensation.


Figure 3.11: Retrograde Phenomena II

### 3.14 Typical Reservoirs

Let us look at the phase envelopes of various types of reservoirs.
a) Crude Oil
b) Dry Gas
c) Wet Gas
d) Condensate

In the following Figures $T_{F}$ is the reservoir temperature and $T_{S}$ is the separator temperature. $P_{F}$ is the initial reservoir pressure.

### 3.14.1 Oil Reservoir



Figure 3.12: Oil Reservoir Phase Envelope

Reservoir temperature is less than critical. As pressure decreases during production, gas forms and continues to form.

### 3.14.2 Dry Gas Reservoir



Figure 3.13: Dry Gas Reservoir Phase Envelope
In this case, as the pressure is decreased no condensation occurs. The reservoir temperature is well above the critical. Even when the temperature is reduced to that at the separator because of the Joule- Thompson effect, no condensation occurs.

### 3.14.3 Wet Gas Reservoir



Figure 3.14: Wet Gas Reservoir Phase Envelope

This is the same as a dry gas, except that the separator temperature goes into the two phase region and liquid drops out.

### 3.14.4 Condensate Reservoir



Figure 3.15: Condensate Reservoir Phase Envelope
The reservoir temperature is between critical and cricondentherm. The reservoir will sometime in its life be in the two phase region. Condensate will also normally exist in the separator.

### 3.15 Ideal Systems

We have discussed primarily ideal systems, particularly ideal solutions. In general, the following principles have been followed:
a) Ideal Gas Law PV $=R T$
b) Dalton Law of Partial Pressure, partial pressure component $A=$ (mole fraction of $A$ in vapour) (Total Pressure)
c) Ideal Solution. Volume of solution of a mixture is equal to the sum of the volume of each individual component.
With hydrocarbons the ideal solution principle is generally followed; however, when a nonhydrocarbon is present, such as $\mathrm{CO}_{2}$,
two liquid phases can be formed. Also we can get both maximum and minimum boiling points, etc.

### 3.16 The Sulphur / $\mathrm{H}_{2} \mathrm{~S}$ System

A special case of phase behaviour occurs in gas systems in which there is a very high concentration of $\mathrm{H}_{2} \mathrm{~S}$ at high pressures. The problem that occurs is that at high pressures and temperatures gas containing high percentages of $\mathrm{H}_{2} \mathrm{~S}$ seem to dissolve elemental sulphur. The well known work of D.R. Weiland ${ }^{2}$ reports on this. Figure 3.16 shows some data for
$50 \% \mathrm{H}_{2} \mathrm{~S}$. It shows that as the temperature and pressure increase, more sulphur is dissolved. Therefore, when the gas is produced out of a reservoir and the pressure and temperature are
dropped, elemental sulphur is precipitated out. This elemental sulphur plugs the well tubing and gathering lines. J.B. Hyne ${ }^{3}$ has made a study of sour gas reservoirs in Alberta to see when the problem of deposition occurs and what causes it. He found that with high $\mathrm{H}_{2} \mathrm{~S}$ wet gas streams (i.e. those containing a lot of condensate) deposition did not occur, as the condensate seems to dissolve the deposited sulphur. He developed a correlation that indicated the probability of deposition. This is given in Figure $3.17^{5}$. This correlation plots the wellhead temperature times the wellhead pressure and $\left[1+C_{5}^{+} \%\right]$ of the gas versus the formation temperature and pressure.
Probably at high pressure $\mathrm{H}_{2} \mathrm{~S}$ forms polysulphides which disassociate on reducing pressure to $\mathrm{H}_{2} \mathrm{~S}$ and elemental sulphur according to the reaction

$$
\mathrm{H}_{2} \mathrm{~S}_{\mathrm{x}}=\mathrm{S}_{\mathrm{x}-1}+\mathrm{H}_{2} \mathrm{~S}
$$

## References

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3. J.B. Hyne, "Study Aids Prediction of Sulfur Deposition in Sour Gas Wells", Oil and Gas Journal, Nov. 25, 1968, p. 107.
4. J.B. Hyne and E.F. Muller, "The Sulphur/Hydrogen Sulphide System", Paper presented to the 19th Canadian Chemical Engineering Conference and 3rd symposium on Catalysis, Edmonton, Alberta, October 19, 1969.
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## Reading List

1. O.R. Schweitzer and C.E. Wales, "Phase Rule and Equilibria Relations", Chemical Engineering, May 27, 1963, p. 117.
2. J.H. Erbar and R.N. Maddox, "Hydrocarbon—Systems Phase Behaviour", Oil and Gas Journal, January 19, 1981, p. 68.

### 4.0 Vapour Liquid Equilibrium Data and Computations

- Importance of vapour liquid equilibrium data
- K factors
- Convergence pressures
- Calculation of dew and bubble - points
- Equilibrium flash calculations


### 4.1 Introduction

The natural gas industry is fortunate in that there is published a great deal of data on physical properties, including vapour liquid equilibrium constants. We use vapour liquid equilibrium data for:

1. Reservoir calculations.
2. Two phase pipeline flow calculations.
3. Inlet separation calculations.
4. Distillation calculations.
5. Absorption calculations.
6. Tower pressure calculations.
7. Refrigeration calculations.

We are very fortunate as compared to crude oil systems which do not have equilibrium data for individual components but have to use correlations depending on average boiling point, characterization factor, etc.

### 4.2 Equilibrium Constants

What is the equilibrium constant? It is defined as "K" where

$$
K_{i}=\frac{y_{i}}{x_{i}}
$$

where:
$y_{i}=$ mole fraction of component "i" in gas phase.
$x_{i}=$ mole fraction component " $i$ " in the liquid phase.

### 4.3 Ideal Equilibrium Ratio

### 4.3.1 Raoult Law

For an ideal gas and liquid the following equation applies:
Equation 4-2

$$
P_{i}=P_{V P i} x_{i}
$$

This states that the partial pressure of a component above a solution is equal to the vapour pressure at temperature and pressure of system for the pure component times the mole fraction of "i" in the liquid.

### 4.3.2 Dalton's Law

Equation 4-3

$$
P_{i}=P_{t} y_{i}
$$

Partial pressure of component "i" in system = mole fraction of "i" in the gas times total pressure of system.
Combining the above equations
Equation 4-4

$$
y_{i} P_{t}=P_{V P i} x_{i}
$$

or
Equation 4-5

$$
\frac{y_{i}}{x_{i}}=\frac{P_{V P i}}{P_{t}}
$$

or as we have defined
Equation 4-6

$$
K_{i}=\frac{y_{i}}{x_{i}}=\frac{P_{V P i}}{P_{t}}
$$

The above equation is restricted to substances at low pressures, a long way from the critical pressure, that obey the ideal gas and ideal solution laws.

### 4.4 Modifications of Ideal Equilibrium Patios

The previous $K$ value is based on both ideal gas and ideal solution laws. We can extend the application of calculated K to higher pressures by use of the term fugacity "f". This is sort of an ideal vapour pressure. i.e. the fugacity = the vapour pressure when the vapour behaves as an ideal gas. It can be defined by the equation:
$\mathrm{RT} \mathrm{d} \ell \mathrm{nf}=\mathrm{VdP}$
and $f^{\circ}=P^{\circ}$ when $P^{\circ}$ approaches 0 .
Now, from the above equation it can be developed that
Equation 4-8

$$
\ln \frac{f}{P}=\frac{1}{R T} \int_{0}^{P} v d P
$$

This applies for gases. For liquids a similar type of equation can be developed using the difference between the actual change in volume and the change in volume of an ideal solution. If there is no difference the fugacity is equal to fugacity of the pure component times the mole fraction. Using fugacities and assuming ideal solutions we have:

$$
f_{i}^{v}=y_{i} f_{v i}
$$

where $f_{v i}$ is the fugacity of the component " $i$ " as a vapour at the pressure and temperature of the equilibrium system. (i.e. pure i). Similarly a Raoult Law type of equation can be developed:

Equation 4-10

$$
f_{i}^{l}=x_{i} f_{l i}
$$

$f_{\ell i}$ is the fugacity of component "i" as a liquid at the temperature and pressure of the system. (i.e. pure "i").

Now for the equilibrium

$$
f_{i}^{v}=f_{i}^{l}
$$

Equation 4-11

$$
K_{i}=\frac{y_{i}}{x_{i}}=\frac{f_{l i}}{f_{v i}}
$$

If non-ideal solutions are experienced activity coefficients $\gamma_{i}^{L}$ which are a measure of the deviation from ideal solution have to be introduced and Equation 11 becomes

Equation 4-12

$$
K_{i}=\frac{y_{i}}{x_{i}}=\frac{\chi_{i}^{L} f_{l i}}{\chi_{i}^{V} f_{v i}}
$$

### 4.5 Actual "K’s"

The above ways of calculating "K" are satisfactory part of the time but not always, particula~zly as systems approach critical conditions. Figure 4.1 shows how the K values vary depending on how they are determined. It should be noted how the actual "K" converges to 1 at high pressure. This is called the convergence pressure.

### 4.6 Measurement of Actual "K's"

Actual K's are determined by taking a mixture of pure compounds, subjecting them to various pressures and temperatures in special cells and determining by proper sampling procedures the composition in the liquid and gas phases. Sage and Lacey at Cal. Tech. pioneered a great deal of this work. Many others such as Kobayshi. at Rice University and Robinson at the University of Alberta have continued this work. From these measurements and by calculations an extensive set of K values for methane to Decane, $\mathrm{H}_{2} \mathrm{~S}$, and some other components have been published in the GPSA Data Book.

Also given in this manual are K values for various oils as a function of their boiling point. In the literature there are data for many systems -benzene, toluene, etc., also many chemical systems.
The $K$ values as plotted in the GPSA Data Book are given for various convergence pressures. That is the pressure at which for this set of data all values of " K " converge to one. This applies for any temperature and for each component.


Figure 4.1: Comparison of "K's"

### 4.7 Methods of Determining "K"

There are several methods for determining "K". The three major methods are as follows: (Starling, Bono, Carnahan and Kwok ${ }^{1}$ give a good discussion of these methods).
a) An equation of state for both the vapour and liquid phase -primarily the BWR (Benedict, Webb, Rubin ${ }^{2}$ ) equation and its modification by Starling ${ }^{15}$ is used for this although the Redlich, Kwong ${ }^{3}$ equation can also be used.
b) An equation of state can be used for the vapour and a liquid theory equation used for the liquid. Prime example is the Chao, Seader ${ }^{4}$ and the Prausnitz Chueh ${ }^{12}$ and the Soave ${ }^{18}$ methods for calculating "K".
c) A graphical correlation like the GPSA Data Book along with the proper convergence pressure. The Haddon and Grayson ${ }^{5}$ data used by the API are also of this type of approach.
We will start with a discussion of the c) approach first.

### 4.8 Convergence Pressure

To consider method c) as given above we must consider the convergence pressure. At the critical pressure and critical temperature of system "K" must equal 1.0 for all components, since we no longer have two phases but we have a single. phase. For a binary system we can see this effect if we plot K versus the pressure at a constant temperature as shown in Figure 4.2.
For two phases to exist the heavier phases' "K" must be less than one and lighter phases' "K" must be greater than 1 . Thus it can be seen that convergence pressure is the critical pressure of a binary and that it has for its critical temperature the temperature in question. The concept of convergence pressure is used as a means of correlating K data. It is calculated primarily from the composition of the system. The effect of convergence pressure selection can be seen from Figure 4.3. As can be seen at low pressure the selection of the convergence pressure is not important. At 150 psia the K values are all the same. At 500 psia $\mathrm{K}=.64$ for an 800 cony, pressure and .48 for a 5000 cony, pressure. At 1000 psia $\mathrm{K}=1$ for 800 and 1000 cony, pressure and .37 for 5000 cony. pressure.


Figure 4.2: Binary System " $K$ 's"
As was stated the convergence pressure is a means of correlating K data for a particular composition.


Figure 4.3: Effect of Convergence Pressure on "K's"
In general we can say the equilibrium constant is a function of pressure, temperature and composition or

$$
K=\phi\left(P, T, x_{1}, x_{2}, \ldots \ldots \ldots x_{n}\right)
$$

Applying the phase rule for a two phase system the number of independent variables to determine K can be expressed by

Equation 4-14

$$
K=\phi^{\prime}\left(P, T, x_{1}, x_{2}, \ldots \ldots \ldots \ldots \ldots . . . x_{n-2}\right)
$$

Now let
Equation 4-15

$$
P_{K}=\phi^{\prime \prime}\left(T, x_{1}, x_{2}, \ldots \ldots \ldots \ldots . . x_{n-2}\right)
$$

( $\mathrm{P}_{\mathrm{K}}=$ Conv. Press.)
Therefore

$$
K=\phi^{\prime \prime}\left(P, P_{K}\right)
$$

For a binary system

$$
P_{K}=\phi^{I V}(T)
$$

$$
K=\phi^{V}(P, T)
$$

Thus for a binary system $P_{k}$ is independent of the composition (or independent of the lightest component).

### 4.9 How to Find The Convergence Pressures

d) At relatively low pressure, i.e. $\frac{P}{P_{K}}<0.5$

The chart on Page 18-5 of the GPSA Data Book can be used for this. The method is to take as the lightest component present in any significant quantity ( $1.0 \%$ or greater in a raw mixture; it is usually methane) as the light component of a two component system. The heavy component is estimated from the composition of the remaining components. A visual estimate is usually good enough. Join the heavy and light component together as shown on the Figure and read off $P_{k}$ against operating temperature.
e) At conditions of $\frac{P}{P_{1}}<0.5$ there are several methods.

The method given below is probably satisfactory.
For natural gas systems it has been found that the convergence pressure is a function of temperature and the composition of the liquid phase. Hence, if the liquid phase composition is known, the convergence pressure is found by the step-wise procedure listed below.

If the liquid phase composition is unknown, it has to be assumed (estimated) and subsequently checked.

1. Identify the lightest hydrocarbon component which is present at a concentration of at least $0.1 \%$ in the liquid phase.
2. Calculate the mass average critical temperature and critical pressure for the remaining heavier components to form a pseudo binary system. (A shortcut approach good for most hydrocarbon systems is to calculate the weight average $\mathrm{T}_{\mathrm{c}}$ only.)
3. Trace the critical locus of the binary consisting of the light component and pseudo heavy component. When the averaged pseudo heavy component is between two real hydrocarbons, an interpolation of the two critical loci must be made.
4. Read the convergence pressure (ordinate) at the system temperature (abscissa) from Figure.
5. Using the convergence pressure determined in Step 4 together with the system temperature and system pressure, obtain K-values for the components from the appropriate convergence pressure K-charts.
6. If the liquid composition was initially assumed, calculate it using the K values and overall system composition.
7. If the differences between the assumed and calculated compositions are significant, repeat the entire procedure.

These are other methods.

- Haddon and Grayson5
- Winn
- Lenoir and White


## Method of Haddon and Grayson ${ }^{1}$

1. Run a flash calculation at an assumed $P_{K}$.
2. Divide liquid into two components.
a) Lightest component greater than $1.0 \%$ (moles).
b) Rest of components.
3. Calculate critical temperature of pseudo heavy components by any method. Straight mole \% can be used and then join the light and heavy components together in the form as given in figure on Page 18-5 of the GPSA Data Book.
4. Read off $P_{K}$ at the operating temperature.
5. Check if this is same as assumed value and if not redo procedure.

## Method of Winn

1. Estimate convergence pressure and calculate liquid phase analysis.

[^8]2. Calculate weight fraction analysis based on lightest component free basis.
3. Find intersection of operating temperature with binary critical pressure for each heavier component and the lightest component.
4. Multiply pressures obtained by corresponding weight fraction of heavier component. The sum of these values is the calculated $\mathrm{P}_{\mathrm{K}}$
5. Check to see if general assumption was OK Figure 4.4 shows how this is done. Also Example Problem \#1 shows this method.

## Method of Lenoir and White

1. Assume a convergence pressure and calculate a liquid phase composition (molal volumes satisfactory).
2. Divide the system into a fictitious light component and fictitious heavy component.
3. Calculate the effective BP of the light component (EBP $)_{\text {) from data on effective EP of }}$ compounds given in article and graphs showing correction factors as compared to lightest component. Note: Must estimate effective boiling point of the heavy component while doing this.


Figure 4.4: Winn Method for Convergence Pressure


Figure 4.5: Lenoir \& White Method for Convergence Pressure
4. Calculate effective $\mathrm{BP}\left(\mathrm{EBP}_{\mathrm{H}}\right)$ of heavy component in similar manner to No. 3.
5. From curves for various $E B P_{L}$ versus lines of constant $E B P_{H}$ read off convergence pressure at operating temperature.
6. Recalculate liquid component to see if assumed value is OK

A short cut method assumes that $E B P_{L} \sim \varepsilon B P$ of lightest $7 \% E B P_{H}$ is $\varepsilon B P$ of heaviest 40\%.

A typical set of curves is shown in Figure 4.5 for an EBP ${ }_{L}$ of some fixed values.
To correct for non alphatics such as $\mathrm{H}_{2} \mathrm{~S}, \mathrm{CO}_{2} . \mathrm{C}_{6} \mathrm{H}_{6}$, etc., a correction factor called the Pressure Function is calculated and depending whether the non alphatic is in the EBP or EBP $_{\mathrm{H}}$ function, it is added to the start or finish (or to both ends) of the regular $\mathrm{P}_{\mathrm{K}}$ curve. This is shown in Figure 4.5. The presence of these compounds usually give higher convergence pressures.

### 4.10 Other "K" Data Using the Convergence Pressure Concept

Haddon and Grayson developed a whole series of charts of "K" which are slightly different than the ones given in the GPSA Data Book. These charts are used as a standard by the API. The method requires the calculation of the convergence pressure as previously discussed. The method is reported to be good for heavier mixtures as found in refinery streams, etc.

### 4.11 "K" Data by Means of Analytic Methods

These methods take into account the specific behavior of each component in the mixture and in one case the relationship of the components to each other. They are particularly suited to computer calculations.

## "K" Data by the Chao-Seader Method

This was the first general correlation to try to account specifically for non idealities in the liquid phase. The equation used is

$$
K_{i}=\frac{\gamma_{i} v_{i}^{\circ}}{\phi_{i}}
$$

where:
$\gamma_{i}=$ activity coefficient of a component in the liquid solution where the fugacity of i in the liquid
Equation 4-20
$f_{i}=\gamma_{i} x_{i} f_{i}^{\text {PureL }}$
( $f_{i}^{\text {PureL }}$ is $f \ell_{i}$ in 11)
$v_{i}^{\circ}$ is the fugacity coefficient for the pure liquid component at the system conditions
Equation 4-21
$v_{i}^{\circ}=\frac{f_{i}^{\text {PureL }}}{P}$
and $\phi_{i}=$ fugacity coefficient for a component in the vapour phase

$$
\phi_{i}=\frac{f_{i}}{P_{i}}=\frac{f_{i}}{y_{i}{ }^{P}}
$$

$\gamma_{i}$ is found from the molar volume of "i" and the solubility parameter for the system according to the equation
$\ln \chi_{i}=\frac{V_{i}\left(\delta_{i}-\delta\right)^{2}}{R T}$
where
$V_{i}=$ liquid molar volume of "i"
$\delta_{\mathrm{i}}=$ solubility parameter for "i"
$\delta=$ solubility paramter for the system
The solubility parameter is defined by
Equation 4-24

$$
\delta=\frac{\Delta E^{0.5}}{V_{i}}
$$

Where:
$\Delta \mathrm{E}$ is the change in internal energy going from a liquid to a vapour. All the above can be found from properties of pure components.
$v_{i}{ }^{0}$ is found using the Pitzer accentric factor " $\omega$ ".
Equation 4-25
$\log v_{i}^{0}=\log \left(v_{i}\right)^{0}+\omega \log \left(v_{i}\right)^{1}$
where:
$v_{i}{ }^{0}=$ fugacity coefficient for a simple fluid which can be found in charts of Edmister ${ }^{14}$
$v_{i}{ }^{1}=$ fugacity coefficient correction factor from Edmister ${ }^{14}$
$\omega=$ accentric factor as discussed in Chapter 2 and listed for each compound in the GPSA Data Book in Section 16. This is the same as in the method of finding the enthalpy given in Chapter 2.

Or
$v_{i}^{0}$ and $v_{i}{ }^{0}$ can be found from the two following equations.
Equation 4-26

$$
\log \left(v_{i}\right)^{0}=A_{0}+\frac{A_{1}}{T_{R}}+A_{2} T_{R}+A_{3} T_{R}^{2}+A_{4} T_{R}^{3}+\left(A_{5}+A_{6} T_{R}+A_{7} T_{R}^{2}\right) P_{R}+\left(A_{8}+A_{9} T_{R}\right) P_{R}^{2}-\log P_{R}
$$

$$
\log \left(v_{i}\right)^{1}=A+B T_{R}+\frac{C}{T_{R}}+D T_{R}^{3}-0.25\left(P_{R}-0.6\right)
$$

where:
$A, A_{2}$, etc. are constants as are $B, C, D$, etc.
$\phi_{i}$ is found by use of the Redlich Kwong equation also given in Chapter 2. It is
Equation 4-28

$$
P=\frac{R T}{v-b}-\frac{a}{T^{0.5} V(V+b)}
$$

or in terms of the compressibility factor $z$

$$
z=\frac{1}{1-h}-\frac{A^{2}}{B}\left(\frac{h}{1+h}\right)
$$

Equation 4-30

$$
h=\frac{B P}{z}
$$

where:
$A$ and $B$ are constant for component expressed in terms of their critical conditions and are for the mixture $A_{i}$ and $B_{i}$ are for the pure component and $Z$ is the mixture.

Then $\phi_{i}$ can be found from
Equation 4-31

$$
\ln \phi_{i}=(Z-1) \frac{B_{i}}{B}-\ln (A-B P)-\frac{A^{2}}{B}\left(\frac{2 A_{i}}{A}-\frac{B_{i}}{B}\right) \ln \left(1+\frac{B P}{Z}\right)
$$

The limitations of the Chao-Seader Equation have been well discussed by Lenoir He suggests the equation is good for pressures up to $2000 \mathrm{psi}(14,000 \mathrm{kpa})$ and temperatures of $100^{\circ} \mathrm{F}$ to $500^{\circ} \mathrm{F}$ ($75^{\circ} \mathrm{C}$ to $260^{\circ} \mathrm{C}$ ). Also the liquid should not contain more than $30 \%$ methane by mole fraction.
The Grayson Streed ${ }^{16}$ modification which is a very similar method to the Chao-Seader has been used very successfully at temperatures of $-200^{\circ} \mathrm{F}$ to $900^{\circ} \mathrm{F}\left(-130^{\circ} \mathrm{C}\right.$ to $\left.480^{\circ} \mathrm{C}\right)$ and to 3000 psia (21,000 KPA)
There is also a modification by Wilson of the Redlich Kwong Equation that is available through the GPSA as the mark $V$ computer program ${ }^{9}$.
"K" Data by the Soave Redlich Kwong Equation ${ }^{18}$
As discussed in chapter 2, Soave developed a modification of the Redlich Kwong Equation
Equation 4-32

$$
P=\frac{R T}{V-b}-\frac{a T}{v(v+b)}
$$

Suitable rules for mixes using interaction coefficients are proposed.
The Soave Equation "K" is available from the GPSA as a computer program.
This program is considered to give good data over a wide range of temperatures and pressures.

## "K" Data by the Peng Robinson Equation

As discussed in Chapter 2, these authors also modified the Redlich Kwong Equation
Equation 4-33

$$
P=\frac{R T}{v-b}-\frac{a(T)}{v(v+b)+b(v-b)}
$$

This equation can be used to find "K" accurately over a wide range of temperatures and pressures. It is available as a computer program through the GPSA.

## "K" Data by the Benedict-Webb-Rubin Equation (Starling Modification)

The BWRS equation (Starling's modification of the BWR equation of state) has the same basic form as the BWR equation, but contains two additional adjustable parameters. The BWRS equation has the following form (see also equation 2.5 , with mixing rules given in Table 2.2)

Equation 4-34:

$$
P=R T \rho+\left(B_{0} R T-A-\frac{C_{0}}{T^{2}}+\frac{D_{0}}{T^{3}}-\frac{E_{0}}{T^{4}}\right) \rho^{2}+\left(b R T-a-\frac{d}{T}\right) \rho^{3}+\left(a+\frac{d}{T}\right) \alpha \rho^{6}+\frac{c \rho^{3}}{T^{2}}\left(1+\chi \rho^{2}\right) \exp \left(-\chi \rho^{2}\right)
$$

Where:
$p$ is the absolute pressure
T the absolute temperature
$\rho$ the molar density
$R$ the universal gas constant.
Mixing rules used to obtain mixture parameters for the BWRS equation are as given in Table 4.1.
Table 4.1: Mixing Rules - BWRS Equation

$$
\begin{array}{ll}
B_{0}=\sum_{i} x_{i} B_{0 i} & b^{1 / 3}=\sum_{i} x_{i} b_{i}^{1 / 3} \\
A_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{3} x_{i} x_{j} A_{0 i}^{1 / 3} A_{0 j}^{1 / 2} & a^{1 / 3}=\sum_{i} x_{i} a_{i}^{1 / 3} \\
C_{0}=\sum_{i} \sum_{j}\left(\frac{m_{1 j}}{2}\right)^{3} x_{i} x_{j} C_{0 i}^{1 / 2} C_{0 j}^{1 / 2} & \alpha^{1 / 3}=\sum_{i} x_{i} \alpha_{i}^{1 / 3} \\
\chi^{1 / 2}=\sum_{i} x_{i} \chi_{i}^{1 / 2} & c^{1 / 3}=\sum_{i} x_{i} c_{i}^{1 / 3} \\
D_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{4} x_{i} x_{j} D_{0 i}^{1 / 2} D_{0 j}^{1 / 2} & d^{1 / 3}=\sum_{i} x_{i} d_{i}^{1 / 3}
\end{array}
$$

$$
E_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{5} x_{i} x_{j} E_{0 i}^{1 / 2} E_{0 j}^{1 / 2}
$$

where $x_{i}$ is the mole fraction of the "ith" component for the homogeneous phase under consideration, and parameters with subscript "i" refer to the "ith" pure component. The BWRS mixing rules contain a binary interaction parameter $\left(m_{i j}\right)$ for each pair of components. The interaction parameters have little effect on bulk properties such as density and enthalpy but can greatly improve K-value predictions.
The BWRS equation is a very good overall thermodynamic prediction method available in the gas processing industry. It is applicable to all types of gas processes including cryogenic expander and absorption of oil plants. It may not be accurate for heavy gas reservoir systems such. as gas condensates or volatile oils or for natural gas-heavy crude systems at processing conditions.
The procedure for calculating " $K$ " is as follows:

1. Perform a flash calculation on the mixture using arbitrary "K".
2. From the vapour and liquid composition calculate the vapour and liquid density.
3. Using the BWRS equation above for fugacity calculate the individual fugacities for each component.
4. Now the fugacities of individual components in the vapour phase and liquid must be equal, i.e.

Equation 4-35

$$
f_{i}^{v}=f_{i}^{\ell}
$$

Therefore steps 1, 2, 3 are replaced until this condition is satisfied. This method of course requires computer programs for its use but is generally quite good.

## "K" Data by the Prausnitz-Chueh Correlation

This method uses the same basic equation as the Chao-Seader but uses different methods for finding the fugacity, activity, etc. Prausnitz has allowed for the effect on the presence of other components on the constants for individual components in calculating the fugacities, molar volumes, etc. For example, in the calculation of $\phi_{i}$ of Equation (18) the Redlich Kwong equation is still used by a binary interaction coefficient is added, i.e. the same as used in the BWRS mixing rules as previously discussed. This data is found from experimental data on binary systems. For example.

Equation 4-36

$$
\ln \phi_{i}=\ln \frac{V}{V-b}+\frac{b_{i}}{V-b}-\frac{2 \sum_{i} y_{i} a_{i j}}{R T^{1.5} b} \ln \left(\frac{V+b}{V}\right)+\frac{a b_{i}}{R T^{1.5} b^{2}}\left[\ln \frac{V+b}{V}-\frac{b}{V+b}\right]-\ln z
$$

This equation corresponds to Equation (31) but the interaction coefficient $a_{i j}$ is added and "a" and " $b$ " are evaluated differently and have different mixing rules. The small "a" and "b" are the constants in the Redlich equation.

The other important change is that the requirement of sometimes having a hypothetic liquid state for the development of the term $v_{i}^{0}$ is avoided by the development of an assymetrical standard state. For the details of the method please refer to reference 12 or suggested reading reference 2.

### 4.12 A Comparison of the Methods of Determining "K"

The accuracy of the various equations has been checked under special conditions, i.e. Iow temperatures and high pressure. Some comparative data versus experimental values are given in Tables 4.2 and 4.3. The selection of the appropriate equation of state or method for " $K$ " values is given in references 4 and 5 of the reading list.

Table 4.2: Comparison of Experimental Methane K-Values at $-75^{\circ}$ F Taken from the $\mathrm{C}_{1}-\mathrm{C}_{3}$ Binary Data

| P psia | Experimental | $\mathbf{1 9 7 2} \mathbf{C h a r t s}$ <br> $\mathbf{P K}_{\mathbf{K}} \mathbf{1 0 0 0}$ | $\mathbf{1 9 6 6} \mathbf{C h a r t s}$ <br> $\mathbf{P}_{\mathbf{K}} \mathbf{1 0 0 0}$ | Soave | Prausnitz - <br> Chueh | $\mathbf{P - V - T}$ Mark V | Choa-Seader | K-Value |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 100 | 10.3 | 10.2 | 10.8 | 10.10 | 10.57 | 10.2 | 7.65 | 10.65 |
| 150 | 7.00 | 6.9 | 6.7 | 6.73 | 7.03 | 6.80 | 5.24 | 7.36 |
| 300 | 3.58 | 3.56 | 3.25 | 3.44 | 3.48 | 3.46 | 2.85 | 3.63 |
| 400 | 2.66 | 2.65 | 2.45 | 2.61 | 2.60 | 2.615 | 2.27 | 2.63 |
| 500 | 2.13 | 2.12 | 1.94 | 2.11 | 2.08 | 2.10 | 1.925 | 2.07 |
| 600 | 1.76 | 1.80 | 1.67 | 1.77 | 1.74 | 1.76 | 1.806 | 1.72 |
| 700 | 1.49 | 1.56 | 1.45 | 1.51 | 1.51 | 1.50 | 1.56 | 1.49 |
| 800 | 1.28 | 1.36 | 1.28 | 1.33 | 1.35 | 1.30 | 1.46 | 1.32 |
| 900 | 1.122 | 1.18 | 1.14 | 1.167 |  | 1.134 | 1.39 | 1.12 |

$\mathrm{P}_{\mathrm{c}}=944$

## Table 4.3: Comparison of Natural Gas Condensate K-Values with those Predicated by Several Correlations for $-100^{\circ} \mathrm{F}$ and 400 psia

| Comp. | Experimental | $\mathbf{1 9 7 2} \mathbf{C h a r t s}$ <br> $\mathbf{P}_{\mathbf{K}}=\mathbf{9 0 0} \mathbf{p s i a}$ | $\mathbf{1 9 6 6} \mathbf{C h a r t s}$ <br> $\mathbf{P}_{\mathbf{K}} \mathbf{= 9 0 0} \mathbf{p s i a}$ | Soave | P-V-T Mark V | Choa-Seader | K-Value |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{N}_{2}$ | 12.164 | 8.1 | 8.1 | 11.686 | 13.561 | 12.049 | 12.267 |
| $\mathrm{CO}_{2}$ | .554 | .559 |  | .548 | .516 | .364 | .801 |
| $\mathrm{C}_{1}$ | 2.316 | 2.24 | 1.90 | 2.129 | 2.338 | 1.938 | 2.273 |
| $\mathrm{C}_{2}$ | .159 | .160 | .167 | .147 | .144 | .144 | .1605 |
| $\mathrm{C}_{3}$ | .0221 | .0261 | .0267 | .0211 | .0206 | .0233 | .0256 |
| $\mathrm{iC}_{4}$ | .0068 | .0085 | .0085 | .0054 | .0052 | .0075 | .0073 |
| $\mathrm{nC}_{4}$ | .0044 | .0055 | .0055 | .0031 | .0029 | .0045 | .0045 |
| $\mathrm{iC}_{5}$ | .0014 |  |  | .0008 | .0008 | .0018 | .0016 |
| $\mathrm{nC}_{5}$ | .0009 |  |  | .0005 | .0005 | .0011 | .0010 |

Table 4.4: Recommended Ranges of Application of K-Value Predication Methods

| Item | Chao-Seader | Grayson <br> Stread | Lee-Erbar $^{20}$ | SBWR | Soave RK | K-Val ${ }^{21}$ | Peng <br> Robinson | Mark V |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |


| Temp lower limit | $-100^{\circ} \mathrm{F}$ | $-200^{\circ} \mathrm{F}$ | $-260^{\circ} \mathrm{F}$ | $-260^{\circ} \mathrm{F}$ | $-260^{\circ} \mathrm{F}$ | $-300^{\circ} \mathrm{F}$ | $-260^{\circ} \mathrm{F}$ | $-240^{\circ} \mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Temp upper limit | ${ }^{+500}{ }^{\circ} \mathrm{F}$ | $+900^{\circ} \mathrm{F}$ | $+300^{\circ} \mathrm{F}$ | $+300{ }^{\circ} \mathrm{F}$ | $+600^{\circ} \mathrm{F}$ | $+300^{\circ} \mathrm{F}$ | $+800^{\circ} \mathrm{F}$ | $+200^{\circ} \mathrm{F}$ |
| Pressure, upper limit | $\begin{aligned} & \text { 1500-2000 } \\ & \text { psia } \end{aligned}$ | 2500 psia | 1500 psia | 3000 psia | $\begin{aligned} & 5000 \\ & \text { psia } \end{aligned}$ | Atmos to 1800 | $\begin{aligned} & 5000 \\ & \text { psia } \end{aligned}$ | $\begin{aligned} & 1500 \\ & \text { psia } \end{aligned}$ |
| Pressure:Valu e of Conv. Point | 80\% | 80\% | 85\% | 90-95\% | 90-95\% | Not stated | Up to critical point | Not stated |
| Component limits | - | - | Paraffin hydrocarb ons only, no $\mathrm{C}_{7}{ }^{+}$, $\mathrm{H}_{2} \mathrm{~S}, \mathrm{CO}_{2}$, $\mathrm{N}_{2}$ | $\mathrm{C}_{7}+$ <br> prediction s erratic | No H2 | - | No data for $\mathrm{H}_{2}$ or He | Not accurat e with high $\mathrm{CO}_{2}$ |
| Comments | Excellent Ks below $0^{\circ} \mathrm{F}$ provided pressure below conv.pressure ; methane and ethane K's sensitive to $\mathrm{C}_{7}+$. Liquid not to contain $>30 \% \mathrm{CH}_{4}$ | Best for $\mathrm{H}_{2}$ containing systems, can be used for hydrocarbo ns above CS limits. Methane, ethane K's sensitive to $\mathrm{C}_{7}+$ | Excellent low temperatur e K except close to critical point | Excellent Iow temperatu re K, problems with 10 compone nt mixtures | Probably the best correlatio n for K | Not accurat e when $\mathrm{CH}_{4}$ is $>30 \%$ in liquid |  |  |

### 4.13 Calculations Involving K Factors

## Dewpoint

This is when the first drop of liquid begins to form.
Equation 4-37

$$
\sum_{i=1}^{n} y_{i}=1.0
$$

and

$$
\sum_{i=1}^{n} x_{i}=1.0
$$

$$
x_{i}=\frac{y_{i}}{K_{i}}
$$

Now since we know "y" we calculate the temperature or pressure (the one not given) at which x's add up to 1 or 100\%.

## Bubble Point Calculation

The reverse of a dewpoint calculation is a bubble point calculation. In this case we wish to determine when the first bubble or gas starts to form. Now here we know x , the liquid component. We add up all the y's from the equation:

Equation 4-40

$$
y_{i}=K_{i} x_{i}
$$

so that the sum of $\mathrm{y}=1$ or $100 \%$. i.e.
Equation 4-41

$$
\sum_{i=1}^{n} y_{i}=1.0
$$

Make a table $\mathrm{x}, \mathrm{K}, \mathrm{Y}=\mathrm{Kx}$. Find the proper temp. or press. when:
Equation 4-42
$K x=1.0$
Note: All these calculations are best done using some sort of computer program if it is available. These illustrations are given for example only.

## Example Problem 4.1

Find the dewpoint of the gas given in the table below. The gas is the overhead from an absorber.
The operating pressure is 1000 psia. Set up a table as shown below. Initially assume $P_{K}=2000$ psia

| Comp. | Mole \% | $K_{1000 *}^{0^{\circ} F}$ | $\frac{Y}{K}$ | $\operatorname{Try} K_{1000}^{-20}$ | $\frac{Y}{K}$ | $\operatorname{Try} K_{1000}^{-30}$ | $\frac{Y}{K}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~N}_{2}$ | 0.30 | 7.4 | 0.04 | 6.2 | 0.05 | 5.5 | 0.06 |
| $\mathrm{C}_{1}$ | 91.63 | 2.0 | 45.90 | 1.8 | 50.80 | 1.7 | 54.00 |
| $\mathrm{C}_{2}$ | 5.72 | 0.5 | 11.52 | 0.42 | 13.62 | 0.39 | 14.70 |
| $\mathrm{C}_{3}$ | 1.63 | 0.16 | 10.20 | 0.13 | 12.50 | 0.12 | 13.60 |
| $\mathrm{iC}_{4}$ | 0.29 | 0.084 | 3.47 | 0.07 | 4.16 | 0.06 | 4.81 |
| $\mathrm{nC}_{4}$ | 0.31 | 0.060 | 5.17 | 0.048 | 6.45 | 0.04 | 7.75 |
| $\mathrm{C}_{5}{ }^{+}$ | 0.12 | 0.030 | 4.00 | 0.022 | 5.45 | 0.016 | 7.50 |
| Total | $\mathbf{1 0 0 . 0 0}$ |  | $\mathbf{8 0 . 3 0}$ |  | $\mathbf{9 3 . 0 3}$ |  | $\mathbf{1 0 2 . 4 2}$ |

* 1957 K data see examples further on in book on effect of different "K" data.

By interpolation the dewpoint is $-27^{\circ} \mathrm{F}$.
Now check assumption of $\mathrm{P}_{\mathrm{K}}$; if using curve on P. 172 NGSMA Book
(1957) = 1800 psi; if using curve on P. 222 NGPSA (1966) = 1900 psi.

If using the GPSA (1972) data book $=1800$ psi.

## Example Problem 4.2

At depropanizing tower is operating with all the overhead product condensing. Determine the tower operating pressure. Assume this pressure is 10 psi greater than the accumulator pressure. The condensing temperature is $80^{\circ} \mathrm{F}$.
The overhead product has an analysis of the following:

|  | Mole \% |
| :---: | :---: |
| $\mathrm{C}_{2}$ | 3.0 |
| $\mathrm{C}_{3}$ | 95.0 |
| $\mathrm{iC}_{4}$ | 2.0 |

Assume a $\mathrm{P}_{\mathrm{K}}$ of 800 psi .

## Solution

Find the accumulator pressure by doing a bubble point.

| Comp. | Mole \% | $K_{150}^{80}$ | $\mathbf{K X}$ | $K_{160}^{80}$ | KX |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}_{2}$ | 3.0 | 2.9 | 8.7 | 2.7 | 8.1 |
| $\mathrm{C}_{3}$ | 95.0 | 0.98 | 93.0 | 0.96 | 9.1 |
| $\mathrm{iC}_{4}$ | 2.0 | 0.44 | 0.9 | 0.42 | 0.8 |
| Total |  |  | $\mathbf{1 0 2 . 6}$ |  | $\mathbf{1 0 0 . 0}$ |

Bubble point pressure is 160 psia.
Tower pressure is 170 psia or 155.3 psig.
A comparison of a dew point calculation using different K data is shown below.
Table 4.5: A Comparison of a Dew Point Calculation Using Different K Data

| Comp. | Mole \% | NGSMA <br> $K_{1000}^{0}$ | $Y$ <br> $K$ | NGPSA <br> $K_{1000}^{0}$ | $\frac{Y}{K}$ | NGPSA <br> $K_{1000}^{0}$ | $\frac{Y}{K}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~N}_{2}$ | 0.30 | 7.40 | 0.04 | 3.9 | 0.75 | 3.9 | 0.75 |
| $\mathrm{C}_{1}$ | 91.63 | 2.0 | 45.90 | 1.95 | 47.10 | 2.1 | 43.50 |
| $\mathrm{C}_{2}$ | 5.72 | 0.5 | 11.52 | 0.40 | 14.30 | 0.46 | 12.50 |
| $\mathrm{C}_{3}$ | 1.63 | 0.16 | 10.20 | 0.135 | 12.20 | 0.17 | 9.60 |
| $\mathrm{iC}_{4}$ | 0.29 | 0.084 | 3.47 | 0.088 | 3.30 | 0.084 | 3.47 |
| $\mathrm{nC}_{4}$ | 0.31 | 0.060 | 5.17 | 0.046 | 6.72 | 0.060 | 5.17 |
| $\mathrm{iC}_{5}$ | 0.12 | 0.030 | 4.00 | 0.021 | 5.71 | 0.030 | 4.00 |
| Total | $\mathbf{1 0 0 . 0 0}$ |  | $\mathbf{8 0 . 3 0}$ |  | $\mathbf{8 9 . 9 8}$ |  | $\mathbf{7 8 . 9 9}$ |

## Vapour Liquid Calculations

Another important calculation is determining the amount of liquid and vapour present in a mixture when the pressure and temperature are known. This can happen for inlet separators, low pressure separators, condensate feed tank, overhead accumulators, etc.
where:

$$
F=\text { feed as } 1.00 \text { or } 100 \text { moles }
$$

$V=$ overhead moles in units of feed
$L=$ bottoms moles in units of feed
$z=$ mole $\%$ or mole fraction of feed
$y=$ mole $\%$ or mole fraction component in overhead
$x=$ mole $\%$ or mole fraction component in bottom

$$
F=V+L
$$

or for component i

$$
z_{i} F=y_{i} V+x_{i} L
$$

Now

$$
y_{i}=K_{i} x_{i}
$$

$$
z F=K x V+x L
$$

Equation 4-47

$$
z F=x(V K+L)
$$

Divide both sides by $L$ and transpose
Equation 4-48

$$
x=\frac{\frac{z F}{L}}{K \frac{V}{L}+1}
$$

Now

$$
\sum_{i}^{n} x=1.0
$$

The method actually is as follows:

1. Select "K" for each component at the temperature and pressure of the system.
2. Assume an $L$ and thus a V.
3. Calculate $L$ from

$$
\sum_{i=1}^{n} x=\sum_{i=1}^{n} \frac{z F}{K \frac{V}{L}+1}=L
$$

4. Check this value against assumed value.
5. Repeat calculation until assumed value is equal to calculated value.

## Example Problem 4.3

Rich oil from an absorber is sent to a rich oil flash drum which operates at $100^{\circ} \mathrm{F}$ and 300 psig . It is desired to determine the composition and quantity of gas that comes from the rich oil flash drum. The amount of rich oil is 65,931 moles per day and the composition is given in the following table.

|  |  |  | Assume L = 90.0 moles |  | Assume L = 88.97 moles |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Comp. | Feed Mole \% | ${ }^{\oplus} K_{315}^{100}$ | $\left(K \frac{V}{L}+1\right)$ | $\left(\frac{z}{K \frac{V}{L}+1}\right)$ | $K \frac{V}{L}+1$ | $\frac{z}{K \frac{V}{L}+1}$ | Moles of Liquid | Moles of Vapour | Mole \% Vapour |
| $\mathrm{N}_{2}$ | 00.12 | 48.18 | 6.3 | 0.02 | 6.85 | 0.02 | 0.02 | 0.10 | 0.93 |
| $\mathrm{C}_{1}$ | 16.63 | 10.01 | 2.10 | 7.93 | 2.21 | 7.42 | 7.42 | 9.21 | 83.53 |
| $\mathrm{C}_{2}$ | 4.99 | 1.92 | 1.21 | 4.11 | 1.230 | 4.03 | 4.03 | 0.96 | 8.71 |
| $\mathrm{C}_{3}$ | 6.01 | 0.66 | 1.07 | 5.63 | 1.080 | 5.56 | 5.56 | 0.45 | 4.10 |
| $\mathrm{iC}_{4}$ | 2.04 | 0.31 | 1.034 | 1.97 | 1.038 | 1.96 | 1.96 | 0.08 | 0.68 |
| $\mathrm{nC}_{4}$ | 4.37 | 0.22 | 1.025 | 4.26 | 1.027 | 4.25 | 4.25 | 0.12 | 1.08 |
| $\mathrm{iC}_{5}$ | 1.75 | 0.11 | 1.012 | 1.73 | 1.012 | 1.73 | 1.73 | 0.02 | 0.21 |
| nC 5 | 1.29 | 0.084 | 1.009 | 1.21 | 1.009 | 1.28 | 1.28 | 0.01 | 0.12 |
| $\mathrm{C}_{6}$ | 3.74 | 0.031 | 1.004 | 3.73 | 1.004 | 3.73 | 3.73 | 0.01 | 0.13 |
| ${ }^{1} \mathrm{C}_{10}$ | 59.06 | 0.007 | 1.001 | 59.00 | 1.001 | 59.00 | 59.00 | 0.06 | 0.51 |
| Total |  |  |  | 88.61 |  | 88.98 | 88.98 | 11.02 | 100.00 |

Note: Assume $\mathrm{P}_{\mathrm{K}}=5000$ (Convergence pressures are quite high with absorber oils).
Amount of vapour per day $=\frac{11.02}{100.00}(65,931)(378.9)=2.75$ MMSCFD

### 4.14 "K" Data for Special Compounds or Systems

These are discussed in some detail in the GPSA Data Book and in the literature. For example methyl mercaptan data is given in the literature (see Haddon and Grayson article). It is supposed to have a " K " value of about $10 \%$ greater than isobutane. Also, hydrocarbon systems with hydrogen

[^9]and nitrogen have been discussed in some detail by Lenoir. The presence of $\mathrm{H}_{2}$ particularly modifies the " $K$ " value for methane and other gases considerably.

For determining the "K's" for sour gas the method of Lenoir and White or the Soave method is probably as good as any when using charts.
The Peng Robinson or the Soave methods give reasonable values for sour gas "K's" from the computer programs.

To find the "K" value for heavy components we can either use data in the NGPSA book for various boiling point materials or by plotting of log "K" versus $\frac{1}{T_{b}}$ for various components in the mixture at the system pressure and extropolate to the $\mathrm{T}_{\mathrm{b}}$ of the heavy component. Other methods are given in Campbell.
Also please read Section 25 of the English GPA data book for general discussion on Equilibrium Ratios.

## Example Problem 4.4

An existing tower that has a design operating pressure of 100 psia is available for use in debutanizing a hydrocarbon feed of the following composition:

|  | Mole \% |
| :---: | :---: |
| $\mathrm{C}_{2}$ | 0.8 |
| $\mathrm{C}_{3}$ | 35.4 |
| $\mathrm{iC}_{4}$ | 10.6 |
| $\mathrm{nC}_{4}$ | 21.7 |
| $\mathrm{iC}_{5}$ | 5.0 |
| $\mathrm{nC}_{5}$ | 11.6 |
| $\mathrm{C}_{6}$ | 10.3 |
| $\mathrm{C}_{7^{+}}$ | 4.6 |

The fractionation is such thet the top product is not to contain more than $2.0 \%$ of $\mathrm{iC}_{5}$ and the bottom is not to contain more than $3.0 \%$ of $\mathrm{nC}_{4}$.
Determine the type of cooling medium that has to be used with this tower.
a) Air cooling-product condensing temperature $120^{\circ} \mathrm{F}$.
b) Cooling Tower water; product condensing temperature $95^{\circ} \mathrm{F}$.
c) Once through river water product condensing temperature $70^{\circ} \mathrm{F}$.
d) Propane refrigeration product condensing temperature $40^{\circ} \mathrm{F}$

## Example Problem 4.5

A Heat exchanger in a LNG plant which is chilling natural gas from $+60^{\circ} \mathrm{F}$ to $-20^{\circ} \mathrm{F}$ has as the chilling medium a mixed refrigerant of the composition listed in the table below. The refrigerant enters the exchanger as a liquid and leaves as a vapour. Determine the $\Delta \mathrm{T}$ at each end of the exchanger.

|  | Mole \% |
| :---: | :---: |
| $\mathrm{N}_{2}$ | 1.0 |
| $\mathrm{C}_{1}$ | 83.5 |


| $\mathrm{H}_{2} \mathrm{~S}$ | 6.5 |
| :---: | :---: |
| $\mathrm{CO}_{2}$ | 3.5 |
| $\mathrm{C}_{2}$ | 2.8 |
| $\mathrm{C}_{3}$ | 1.4 |
| $\mathrm{iC}_{4}$ | 0.4 |
| $\mathrm{nC}_{4}$ | 0.5 |
| $\mathrm{iC}_{5}$ | 0.2 |
| $\mathrm{nC}_{5}{ }^{+}$ | 0.2 |
|  | $\mathbf{1 0 0 . 0}$ |

## Example Problem 4.6

You are to recommend to your company what "K" correlation to use for an ethane recovery facility that is to process gas of the following composition:

|  | Mole \% |
| :---: | :---: |
| $\mathrm{C}_{1}$ | 86.01 |
| $\mathrm{C}_{2}$ | 10.35 |
| $\mathrm{C}_{3}$ | 2.55 |
| $\mathrm{iC}_{4}$ | 0.32 |
| $\mathrm{nC}_{4}$ | 0.47 |
| $\mathrm{iC}_{5}$ | 0.08 |
| $\mathrm{nC}_{5}$ | 0.12 |
| $\mathrm{C}_{6}$ | 0.10 |

This gas is received at 700 psia and $60^{\circ} \mathrm{F}$.
The following conditions should be investigated:

1. At the first separator 680 psia and $-90^{\circ} \mathrm{F}$
2. At the second separator after the expander in which the gas from the first separator is expanded to 300 psia and $-135^{\circ} \mathrm{F}$

## Example Problem 4.7

A gas of the composition given below is cooled to $-120^{\circ} \mathrm{F}$ and 350 psia in an expander plant. It has a high methyl mercaptan $\left(\mathrm{CH}_{3} \mathrm{SH}\right)$ content. Some concern has been expressed as to whether most of this material will stay in the gas. Please estimate what fraction of the mercaptan will remain in the gas phase after the above referred to chilling has taken place (within 10\%). Use the following data:

|  | Feed Gas <br> Composition Mole \% |
| :---: | :---: |
| $\mathrm{C}_{1}$ | 93.54 |
| $\mathrm{C}_{2}$ | 4.96 |
| $\mathrm{C}_{3}$ | 1.25 |
| $\mathrm{iC}_{4}$ | 0.10 |
| $\mathrm{nC}_{4}$ | 0.15 |
|  | $\mathbf{1 0 0 . 0 0}$ |

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### 5.0 Water Hydrocarbon Systems

- Water solubility in natural gas and natural gas liquids.
- Effect of chemical composition on solubility.
- Gas hydrates and their nature.
- The probability of forming gas hydrates, and the preventing of their formation.
- Effect of chemical composition on hydrate formation.


### 5.1 Why Do We Consider These Systems?

a) Water is present in most reservoirs and raw gas is usually considered to be saturated in the reservoir. This may not be the case, but no detailed work has been done to show that reservoirs are not saturated.
b) The presence of water can cause the formation of what is called hydrates. These are chemical compounds of 2~ and hydrocarbons. If they form in pipelines they cause serious plugging problems.
c) The presence of water in liquid hydrocarbons can cause freezing of liquid lines and stoppage of fuel flow.
d) Water systems can be corrosive, particularly when acid gases are present.

### 5.2 Typical Water-Hydrocarbon Systems

The systems of water and various hydrocarbons are quite complex. Many liquids, hydrate and solid phases occur. Figure 5.1 shows the temperature composition diagram for propane and water at a fixed pressure of 300 psig ( 2200 kpa ).

To see what happens to a mixture of propane and water, let us consider a $50 \% \mathrm{C}_{3}$ and $50 \% \mathrm{H}_{2} \mathrm{O}$ mixture at about $350^{\circ} \mathrm{F}\left(176^{\circ} \mathrm{C}\right)$ and then cool it. Initially it is a gas (G). Upon cooling, a liquid phase that is essentially water $\left(\mathrm{L}_{1}\right)$ is formed and the gas becomes richer in propane but is still just a gas ( $G, L_{1}$ are present). On further cooling, a propane rich liquid is formed $\left(L_{2}\right)$ and only two liquid phases are present $\left(L_{2}\right.$ and $\left.L_{1}\right)$. Further cooling brings the formation of a propane water hydrate $(\mathrm{H})$ while the propane rich liquid remains. More cooling brings about the formation of solid propane while the hydrate compound remains. The pressure, temperature diagram for $\mathrm{C}_{3}$ and $\mathrm{H}_{2} \mathrm{O}$ is shown in

Figure 5.2. Similar types of diagrams can be developed for other hydrocarbon-water systems. (See Katz, Pages 190 forward).


Figure 5.1: Temperature Composition Diagram Propane Water


Figure 5.2: Pressure Temperature Diagram Propane Water

### 5.3 Water Content of Natural Gas

## Sweet Gas (Hydrocarbons Only)

Natural gas can contain considerable amounts of water vapour, particularly at high temperatures and low pressures. Figure 5.3, wltich is a reproduction of the chart given in the GSPA SI Data Book shows that as the pressure is increased the water content of natural gas is decreased. This chart also can be used to illustrate why the specification of a water content of 4 lbs per MMSCF for pipeline gas is required in Canada.
The dewpoint of a gas at 800 psia ( 5500 kpa ) with a water content of 4 lbs per MMSCF ( 65 mg per $\left.\mathrm{m}^{3}\right\}$ is $14^{\circ} \mathrm{F}\left(-10^{\circ} \mathrm{C}\right)$. Since pipeline gas gets down to a temperature of $+25^{\circ} \mathrm{F}\left(-4^{\circ} \mathrm{C}\right)$ in the winter even when in a buried pipeline three feet under ground, a water content higher than $4 \mathrm{lbs} / \mathrm{MMSCF}$ would result in water condensing in the pipeline which would result in several problems.

## Gas Containing Significant Amounts of Non-Hydrocarbons

In the case where there are significant quantities of non-hydrocarbons such as nitrogen, hydrogen sulphide or carbon dioxide present, the water content of the gases are quite different than compared to that obtained from Figure 5.3. Nitrogen does not hold as much water as natural gas. Katz, on pages 197 and 198, discusses this. The acid gases, $\mathrm{H}_{2} \mathrm{~S}$, and $\mathrm{CO}_{2}$ can hold a much greater amount of water, particularly at high pressures. This is explained by the fact that both water and the acid gases are polar compounds and hydrocarbons are not.
Figures 15-21 and 15-22 in the GPSA Data Book give the water content for pure $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{CO}_{2}$ for calculation purposes.
To find the actual water content of gases containing large amounts of non-hydrocarbons, it is best to consider each non-hydrocarbon component separately, then add the separate fractions of the gas to find the total water content. The equation for this is

Equation 5-1

$$
W_{\text {mixture }}=Y_{H C} W_{\mathrm{HC}}+Y_{\mathrm{H}_{2} \mathrm{~S}} W_{\mathrm{H}_{2} \mathrm{~S}}+Y_{\mathrm{CO}_{2}} W_{\mathrm{CO}_{2}}
$$

Where:
$Y$ is the mole fraction of each component.
An example of this procedure is given in Example Problem 5.1. This method has worked out quite successfully at Pine Creek, Alberta, where it was found that water content of the sour gas that was to be dehydrated was much higher than that obtained from the sweet gas curves. (For a description of the facilities and some special test work for this field see A. Masuda and P. Krachy).

## Method of Wichert

Moore, Heidemann, and Wichert have developed a new method for estimating the water contents of sour natural gas based on extensive field tests of sour gas in Canada. Figure 5.7, 5.8, and 5.9 show this data to sour gas up to $40 \%$ acid gas and from 300 to 10,000 psia (2068 to 68,947 kpa).

Note: The figures are given for $\mathrm{H}_{2} \mathrm{~S}$ as the acid gas component. $\mathrm{CO}_{2}$ is considered to hold about $75 \%$ of what $\mathrm{H}_{2} \mathrm{~S}$ does, thus if you had a mixture of $20 \% \mathrm{H}_{2} \mathrm{~S} 16 \% \mathrm{CO}_{2}$ and the rest hydrocarbons you would use data for $32 \% \mathrm{H}_{2} \mathrm{~S}-68 \% \mathrm{HC}$.

## Example Problem 5.1

Determine the expected water content of gas of the composition given below. The gas is in the reservoir at 3000 psi and $160^{\circ} \mathrm{F}$

|  | Mole \% |
| :---: | :---: |
| $\mathrm{N}_{2}$ | 0.4 |
| $\mathrm{H}_{2} \mathrm{~S}$ | 35.0 |
| $\mathrm{CO}_{2}$ | 10.0 |
| $\mathrm{C}_{1}$ | 53.6 |
| $\mathrm{C}_{2}$ | 1.0 |

## Method 1

Use the partial water content for each major different component. See Figure 15-21 and Figure 15 - 22 from the GPSA Data Book for the $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{~S}$ water content. Then the calculation becomes:

|  | Mole \% | Individual Water Content <br> lbs/MMSCF at 160F | Partial Water <br> Content | Source of Data |  |  |  |  |  |
| :--- | :---: | :---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sweet Gas Comp. | 55.0 | 130 | 71.5 | Fig. 15-14 GPSA Data Book |  |  |  |  |  |
| $\mathrm{H}_{2} \mathrm{~S}$ | 35.0 | 500 | 175.0 | Fig. 15-22 GPSA Data Book |  |  |  |  |  |
| $\mathrm{CO}_{2}$ | 10.0 | 220 | 22.0 | Fig. 15-21 GPSA Data Book |  |  |  |  |  |
| Total |  |  |  |  |  |  |  | $\mathbf{2 6 8 . 5}$ |  |

Method 2 (Wichert's)
$\mathrm{H}_{2} \mathrm{~S} \quad 35.0$
$\mathrm{CO}_{2} \quad 10.0$ equivalent 7.5 Acid Gas 42.5\%
$\mathrm{HC} \quad 57.5$
From Chart 5.8 and by interpolation water content $=.78 \mathrm{BBIs} / \mathrm{MMSCF}=0.223 \mathrm{lbs} \mathrm{H}_{2} \mathrm{O} / \mathrm{MMSCF}$
Note: Experimental data on high acid natural gas of a similar composition give a water content data of just over $300 \mathrm{lbs} / \mathrm{MMSCF}$. Thus, either method can be used for calculating water content at high acid gas concentrations.


Figure 5.3: Water Contents of Natural Gas with Corrections for Salinity and Relative Density


Figure 5.4: Water Contents of Natural Gas Mixtures

### 5.4 Water Content of Liquid Hydrocarbons

Data for the solubility of water in varying hydrocarbons is presented in GPSA Data Book, P. 15-9, as Fig. 15-13. Hydrocarbons from propane through lube oil are given. Generally hydrocarbons that have been in contact with water must be dried before being stored. A salt tower is often satisfactory for the heavier compounds like diesel oils; this removes the free water. For drying liquid propane from storage wells $\mathrm{CaCl}_{2}$ pellets are often used.

### 5.5 The Measuring of The Water Content

Water content can be measured by:
a) The use of a Bureau of Mines Dewpoint detector in which the gas is chilled to the point of condensation of the water. Particular care has to be taken when using this apparatus that a water dewpoint and not a hydrocarbon dewpoint is recorded.
b) The use of chemical tests: Karl Fisher Reagent. This is used for trace water determinations.
c) Using chromatography techniques - as described by Lukacs and Robinson.

### 5.6 Hydrocarbons in Water

The problem of dissolving hydrocarbons by water is primarily that of physical absorption. A Henry's law equation or a modification of it can be used, i.e.

Equation 5-2

$$
\overline{P i}=H X i
$$

where:
$\overline{P i}=$ partial pressure of component i in gas
H = Henry constant for system
$X i=$ mole fraction of $i$
or if fugacities are used, $\overline{f i}=H X i$. Henry's law constant for various gases given in Perry and Katz. These values are a function of temperature only.
Data for the solubility of specific compounds or products, such as natural gas, propane, etc., are giveh in Katz on P. 207.
Special data should be collected for the absorption of natural gas by the various sweetening solvents. Figure 5.5 gives the data for monoethanol amine. Diethanol amine absorbs about twice as much and sulphinol considerably more than this. Actual data needs to be published on these systems.

### 5.7 Hydrates

Gas hydrates are loose chemical compounds of hydrocarbons and water. Some typical formulae are.:

| $\mathrm{CH}_{4}$ | - | $7 \mathrm{H}_{2} \mathrm{O}$ |
| :--- | :--- | :--- |
| $\mathrm{C}_{2} \mathrm{H}_{6}$ | - | $8 \mathrm{H}_{2} \mathrm{O}$ |
| $\mathrm{C}_{3} \mathrm{H}_{8}$ | - | $17 \mathrm{H}_{2} \mathrm{O}$ |



Figure 5.5: $\mathrm{CH}_{4}$ Dissolved in $25 \%$ NEA Solution
Gas hydrates belong to a class of substances called clathrates (see \#4 of the Reading List) - A clathrate compound is one formed by the complete enclosure of one or more species of a molecule in a suitable structure formed by another species. When the host structure is water the clathrate is called a hydrate. Gas hydrates have some properties ascribed to chemical compounds and
sometimes behave as solutions of gases in crystalline solids. They resemble wet snow in appearance. Two types of structural lattice are generally:
a) Structure I a body centre cubic lattice with $7-8 \mathrm{H}_{2} \mathrm{O}$ in framework. This applies for the smaller molecules like $\mathrm{CH}_{4}, \mathrm{C}_{2} \mathrm{H}_{6}, \mathrm{H}_{2} \mathrm{~S}$
b) Structure II a diamond shape lattice with up to $17 \mathrm{H}_{2} \mathrm{O}$ molecules per gas molecule for heavier molecules.

In both cases, water forms the framework and hydrocarbon fills voids in the centre of the framework or in cavities formed by the water molecules. Note that: The maximum diameter of the cavities is 67 Angstroms. A gas having a molecular dimension greater than this diameter cannot form hydrates, thus $\mathrm{C}_{7}$ and heavier do not hydrate. $\mathrm{C}_{5}$ will hydrate at $32^{\circ} \mathrm{F}\left(0^{\circ} \mathrm{C}\right)$ and $\mathrm{C}_{6}$ will hydrate at a lower temperature than this. Gases with a hydrogen from atom in the polar position do not hydrate, i.e. ammonia, alcohols, etc.

Table 5.1 shows the molecular dimension of hydrocarbons.
Table 5.1: Size of Hydrocarbon Molecules

| Hydrocarbon | Molecular Dimension ${ }^{\circ} \mathbf{A}$ |
| :---: | :---: |
| $\mathrm{C}_{1}$ | 3.882 |
| $\mathrm{C}_{2}$ | 4.418 |
| $\mathrm{C}_{3}$ | 5.061 |
| $\mathrm{iC}_{4}$ | 5.341 |
| $\mathrm{nC}_{4}$ | 4.997 |
| $\mathrm{iC}_{5}$ | 5.32 |
| $\mathrm{nC}_{5}$ | 5.769 |
| $\mathrm{nC}_{6}$ | 5.909 |
| $\mathrm{C}_{7}$ | 8.88 |
| $\mathrm{C}_{8}$ | 7.451 |
| $\mathrm{C}_{9}$ | 8.778 |

Note: Hydrate can form with liquid hydrocarbons present but the right conditions of free water present, proper temperatures and pressures have to occur.

### 5.8 Conditions for Hydrates to Form

Hydrates form only when free water is present and the system is at a proper temperature and pressure. It should be noted that hydrocarbons from $\mathrm{C}_{1}$ to $\mathrm{nC}_{4}$ inclusive only form hydrates. Pentanes and heavier do not above $32^{\circ} \mathrm{F}\left(0^{\circ} \mathrm{C}\right)$ - However, $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{CO}_{2}$ do. Here are some examples of hydrate conditions:

Table 5.2: Hydrate Formation Conditions

|  | Min. psia | ${ }^{* *}$ Pres. (kpa) | Max. Temp. | ${ }^{* * *}{ }^{\circ} \mathbf{F}\left({ }^{\circ} \mathbf{C}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{C H}_{4}$ | 400 | $(2790)$ | 33 | $(1)$ |
|  | 600 | $(4185)$ | 40 | $(4)$ |
|  | 1000 | $(6970)$ | 50 | $(10)$ |
| $\mathrm{C}_{2} \mathbf{H}_{6}$ | 80 | $(558)$ | 33 | $(1)$ |


|  | 400 | $(2790)$ | 57 | $(14)$ |
| :--- | :--- | :--- | :--- | :--- |

Note: $\quad$ ** Hydrates will form if pressure above these values and temperature below these values.

### 5.9 Calculation of the Possibility of Hydrates Forming

The possibility of a hydrate forming can be calculated by using the hydration formation graph on Fig. 15-1 of the GPSA Manual. For example, to find the hydrate temperature of a gas with a gravity of 0.62 at 900 psia, one reads off the chart that it is $60^{\circ} \mathrm{F}$. Another method of calculating the hydrate temperature is by the use of the hydrate equilibrium constant " $\mathrm{K}_{\mathrm{v}-\mathrm{s}}$ ". The equation that is used is:

Equation 5-3

$$
K_{v-s}=\frac{y}{x_{s}}
$$

where:
$\mathrm{K}_{\mathrm{v}-\mathrm{s}}=$ equilibrium constant for vapour solid equilibrium
$y=$ mole fraction of HC on a water free basis
$\mathrm{x}_{\mathrm{s}}=$ mole fraction of HC in the solid on a water free basis
Values for $\mathrm{K}_{\mathrm{v} \text {-s }}$ for $\mathrm{C}_{1}, \mathrm{C}_{2}, \mathrm{C}_{3}, \mathrm{iC}_{4}, \mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{~S}$ are given in the GPSA Data Book, Figure 15-7 to p . 15-12. To find the hydrate condition of a gas at given pressure, a calculation similar to a dewpoint one should be done, i.e.

Equation 5-4

$$
\sum \frac{Y}{K}=1.0
$$

Make a table showing given gas composition, then find $\frac{Y}{K}$ for assumed temperature. When $\frac{Y}{K}=1.0$ then this is the temperature at which hydrate will form. For K value not given in the charts use the following:

1. For $n$ butane take $K$ values for ethane.
2. For $\mathrm{N}_{2}$ and hydrocarbon compounds heavier than $\mathrm{nC}_{4}$ take K as infinity. Example Problem No. 2 shows how above calculation is done.

Baillie and Wichert have developed a graphical method for calculating hydrate temperature of sour natural gas. The method is given below and uses Figure 5.11 (metric units) and Figure 5.12 (imperial units).

1. Calculate the relative density (specific gravity) of the gas mixture.
2. Enter the main graph at the pressure on the left side (sloping axis), and move to the right to the $\mathrm{H}_{2} \mathrm{~S}$ concentration line. Interpolate between lines. Drop down to the gas relative density (gas gravity) line, then follow the slope of the guide line to
the temperature scale at the bottom of the graph. Read the temperature in $0^{\circ} \mathrm{C}$ ( $0^{\circ} \mathrm{F}$ ).
3. Obtain the temperature adjustment for the $\mathrm{C}_{3}$ content from the top left side of the page. Enter this graph along the $\mathrm{H}_{2} \mathrm{~S}$ scale, move to the right to the $\mathrm{C}_{3}$ concentration of the mixture and then drop down to the pressure line. Move either right or left to obtain the $\mathrm{C}_{3}$ content adjustment in $0^{\circ} \mathrm{C}\left(0^{\circ} \mathrm{F}\right)$. The values on the left side are negative.
4. Add the $\mathrm{C}_{3}$ adjustment~obtained in Step 3 to the value obtained in Step 2. The result is the estimate of the hydrate temperature at the given pressure for the gas mixture.


Figure 5.6: Hydrate Chart for Sour Natural Gas (SI Units)


Figure 5.7: Hydrate Chart for Sour Natural Gas (Imperial Units)

## Example Problem 5.2

Determine the hydrate point of the gas of the composition given in the table below when the gas is at 1200 psig.

| Comp. | Mole \% | Kvs at 65 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\frac{Y}{K}$ | Kvs at 70 |  |
|  |  |  | $\frac{Y}{K}$ |  |  |
| $\mathrm{~N}_{2}$ | 4.2 | $\infty$ | 0.0 | $\infty$ | 0.0 |
| $\mathrm{H}_{2} \mathrm{~S}$ | 6.4 | 0.25 | 25.6 | 0.37 | 17.3 |
| $\mathrm{CO}_{2}$ | 4.4 | 10.0 | 0.4 | 25.0 | 0.2 |
| $\mathrm{C}_{1}$ | 78.0 | 1.18 | 66.1 | 1.21 | 64.4 |
| $\mathrm{C}_{2}$ | 3.2 | 0.85 | 3.8 | 1.15 | 2.8 |
| $\mathrm{C}_{3}$ | 1.2 | 0.10 | 12.0 | 0.16 | 7.5 |
| ${ }^{*} \mathrm{nC}_{4}$ | 0.5 | 0.85 | 0.6 | 1.15 | 0.4 |
| $\mathrm{iC}_{5}$ | 0.3 | $\infty$ | 0.0 | $\infty$ | 0.0 |
| $\mathrm{nC}_{5}$ | 0.5 | $\infty$ | 0.0 | $\infty$ | 0.0 |
| $\mathrm{C}_{6}$ | 1.3 | $\infty$ | 0.0 | $\infty$ | 0.0 |
| Total |  |  | $\mathbf{1 0 7 . 5}$ |  | $\mathbf{9 2 . 6}$ |

* Use $\mathrm{K}_{\mathrm{vs}}$ value for ethane for n Butane.

By interpolation the hydrate point is $69^{\circ} \mathrm{F}$. If gravity of gas is calculated from composition it is equal to $\frac{20.7}{28.9}=0.71$. Check hydrate temperature using this value. From 15-1, P. 15-2, hydrate temperature is $67^{\circ} \mathrm{F}$. This is a good check (The value by the Wichert chart is 71 .).
Also given in Fig. 15-2 to 15-6 of the GPSA Data Book are graphs showing the permissible expansion of natural gases without hydrate formation. This is quite important, as often when a well is choked at the wellhead, this condition can occur.

### 5.10 The Prevention of Hydrates

Hydrates form under the following conditions:
a) At proper conditions of temperature and pressure.
b) When free water is present.

Also, generally they form in areas of great turbulence.
To prevent hydrates from forming, the following methods can be used:

1. Keep the gas above the hydrate temperature.
2. Remove the water from the gas so that free water will not condense out.
3. Add chemicals to the gas to combine with the water. The chemicals mostly used are methanol, glycols and sometimes ammonia. Glycols are generally used for continuous processes while methanol is used for emergencies.
A well known equation, called the Hanunerschmidt equation, is used to determine the concentration of chemical in the final solution.

$$
d=\frac{K W}{100 M-M W}
$$

where:
$\mathrm{d}=$ number of ${ }^{\circ} \mathrm{F}$ gas hydrate freezing point is lowered.
$\mathrm{W}=\mathrm{wt} \%$ of final glycol concentration.
$M=$ mole wt. of compound used for hydrate suppression.
$\mathrm{K}=\mathrm{a}$ constant $=2335$ for methanol, ethanol, ammonia; $=4000$ for glycols
In metric units i.e. d in ${ }^{\circ} \mathrm{C}$ then $\mathrm{k}=1297$ for methanol, and 2222 for glycols. Thus we can calculate the concentration of final glycol solution and if we know what the initial concentration is (for hydrate inhibition solution strengths used are about $75 \%$ to $80 \%$ ) then the amount to circulate can be calculated.

## Example Problem 5.3

Determine the amount of $67 \%$ by weight mono ethylene glycol to be circulated in a gas gathering unit that has a central glycol concentration unit.

| Gas Pressure | 1000 psig |
| :--- | :--- |
| Gas Temperature from well | $85^{\circ} \mathrm{F}$ |
| Ground Temperature | $40^{\circ} \mathrm{F}$ |
| Gas Specific Gravity | 0.75 |
| Total gas handled per day | 8 MMSCF |

From the hydrate formation curve, it is determined that a saturated gas with a specific gravity of 0.75 at 1000 psig has a hydrate point of 67F. Thus, the hydrate depression required is $67-40$ or 27F. Assuming mono ethylene glycol (mol. wt. 62.1) is utilized, the following substitutions are made in the Hammerschmidt equation and W determined:

$\mathrm{W}=29.5$ \% by wc - EG final concentration.
From Figure 5.3 it is seen that saturated gas at $85^{\circ} \mathrm{F}$ and 1000 psig contains $39.1 \mathrm{lbs} \mathrm{H}_{2} \mathrm{O} / \mathrm{MMSCF}$. When the gas is cooled to $40^{\circ} \mathrm{F}$ it will contain $9 \mathrm{lbs} / \mathrm{MMSCF}$.

With 8 MMSCF of gas being processed daily, this amounts to

$$
\left(\frac{39.1-1}{24 \text { Hours }}\right)(8)=10 l b s / h r
$$

that is condensed and has to be handled by the glycol.
Assuming hydrate depression is to be achieved by injecting $67 \%$ by weight ethylene glycol, the injection rate required to produce a final glycol concentration of $29.5 \%$ is calculated.
Do this by a glycol balance.
Let:

$$
\begin{aligned}
& X=\mathrm{lb} \text { of } 0.67 \mathrm{EG} / \mathrm{Hr} \\
& 0.67 \mathrm{X}=0.295(\mathrm{X}+10) \\
& \mathrm{X}=7.86 \mathrm{lbs} / \mathrm{hr} \text { required }
\end{aligned}
$$

probably should design pumping capacity for about double this amount.

## Example Problem 5.4

Data
Gas pressure 6995 kpa
Gas temperature from Well $=29.4^{\circ} \mathrm{C}$
Ground Temperature $=4.4^{\circ} \mathrm{C}$
Gas flow $=226,564 \mathrm{~m}^{3} /$ day
Solution
Gas Hydrate temperature $=19.4^{\circ} \mathrm{C}$
Ground temperature $=4.4^{\circ} \mathrm{C}$
Depression Required $=15^{\circ} \mathrm{C}$
Hammerschmidt Equation:

$$
15=\frac{2222 W}{100(62.1)-62.1 W}
$$

$\mathrm{W}=29.5 \%$ by wt. total concentration.

## From Figure 5.3:

Water content at $29.4^{\circ} \mathrm{C}=690 \mathrm{mg} / \mathrm{m}^{3}$
Water content at $4.4^{\circ} \mathrm{C}=170 \mathrm{mg} / \mathrm{m}^{3}$
Difference $=520 \mathrm{mg} / \mathrm{m}^{3}$

$$
m g / \mathrm{hr}=\frac{520(226,564)}{24}=4.91 \frac{\mathrm{~kg}}{\mathrm{hr}}
$$

Now solve by glycol balance:

$$
0.67 X=0.295(x+4.91)
$$

$$
\mathrm{X}=3.86 \mathrm{~kg} / \mathrm{hr}
$$

### 5.10.1 More Example Problems

## Example Problem 5.5

It has been decided to use a molecular sieve unit to dehydrate a gas produced from a reservoir. The reservoir pressure is 3000 psia and at $160^{\circ} \mathrm{F}$. The gas has the following composition:

|  | Mole \% |
| :---: | :--- |
| $\mathrm{N}_{2}$ | 0.5 |
| $\mathrm{H}_{2} \mathrm{~S}$ | 26.7 |
| $\mathrm{CO}_{2}$ | 12.3 |
| $\mathrm{C}_{1}$ | 57.3 |
| $\mathrm{C}_{2}$ | 2.3 |
| $\mathrm{C}_{3}$ | 0.8 |
| $\mathrm{iC}_{4}{ }^{+}$ | 0.1 |

The dehydration a 4 hour cycle. on regeneration unit is to be designed to handle 50 MMSCFD of gas on. That is, each bed is on for 4 hours and then 4 hours and cooling.
Determine the length and diameter of the mole sieve vessel. Here is some additional information.
a) The wellhead flowing pressure is 2600 psia and the temperature is $140^{\circ} \mathrm{F}$.
b) The design flow for gas through a mole sieve dessicant bed is 30 feet per minute.
c) Allow 2 feet on either side of the molecular sieve bed for an entrance chamber and for a disengaging space.
d) The bulk density of the molecular sieve is $43 \mathrm{lbs} / \mathrm{cu}$. feet.
e) The design absorptive capacity of the sieve is $10 \%$ adsorption.
f) The gas is to be dried to a dew point of $10^{\circ} \mathrm{F}$ prior to entering the pipeline.
g) The unit's design operating pressure is 1440 psig.

## Example Problem 5.6

A gas well flows at the rate of 20 MMSCFD directly to a gas plant. It is located 2 moles from the plant. The temperature of the gas leaving the well is $100^{\circ} \mathrm{F}$ (after the choke) and it is $80^{\circ} \mathrm{F}$ when it reaches the plant. The gas composition is as follows:

|  | Mole \% |
| :--- | :--- |
| $\mathrm{H}_{2} \mathrm{~S}$ | 27.5 |
| $\mathrm{CO}_{2}$ | 7.5 |
| $\mathrm{C}_{1}$ | 63.0 |
| $\mathrm{C}_{2}$ | 1.7 |
| $\mathrm{C}_{3}$ | 0.3 |

Another gas well is found adjacent to the gathering line 1 mile from the plant. It produces only 5.0 MMSCFD and the temperature of the gas leaving the choke is calculated to be $60^{\circ} \mathrm{F}$ with no heater. Its composition is as follows:

|  | Mole \% |
| :---: | :---: |
| $\mathrm{H}_{2} \mathrm{~S}$ | 5.0 |


| $\mathrm{CO}_{2}$ | 1.0 |
| :--- | :--- |
| $\mathrm{C}_{1}$ | 87.0 |
| $\mathrm{C}_{2}$ | 5.0 |
| $\mathrm{C}_{3}$ | 1.5 |
| $\mathrm{iC}_{4}$ | 0.5 |

The pressure of the gas at each well is 2000 psia. The pipeline pressure at the first well is 1200 psia, at the second well 1100 psia and the plant 1000 psia.
Do you think it is necessary to put a heater at the second well before the choke? If so, how hot would you heat the gas from this well?
Assume temperature drop along the initial gathering line is directly proportional to its length.

## Example Problem 5.7

Assume gas field has been discovered just off the Gulf Islands between Vancouver, B.C. and Vancouver Island. The gas composition is as given below. It is anticipated the flowing wellhead pressure will be 2500 psia and it will be choked at the well to 1400 psia and then transported along the bottom of the ocean to a central processing plant on the B.C. mainland at tidewater. The anticipated maximum flow is 200 MMSCFD. It is planned to control the hydrates in the line by injecting an $80 \%$ ethylene glycol solution at each welihead. The glycol will be recovered at the plant and re-used. Determine the amount of glycol required for this operation. Express as an 80\% glycol solution in Ibs/day.
Data:
Ocean minimum temperature $42^{\circ} \mathrm{F}$
Reservoir Pressure 3000 psia
Reservoir Temperature $160^{\circ} \mathrm{F}$
Wellhead temperature under flowing conditions $\quad 110^{\circ} \mathrm{F}$
Plant entrance pressure 1200 psia
The gas composition is:

|  | Mole \% |
| :--- | :--- |
| $\mathrm{C}_{1}$ | 87.2 |
| $\mathrm{C}_{2}$ | 5.6 |
| $\mathrm{C}_{3}$ | 3.2 |
| $\mathrm{iC}_{4}$ | 1.0 |
| $\mathrm{nC}_{4}$ | 2.4 |
| $\mathrm{iC}_{5}$ | 0.6 |

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### 6.0 Flow of Fluids

- Energy relationship
- Gas flow
- Liquid flow
- Two-phase flow
- Measurement of flow and equipment for making fluids flow.


### 6.1 Introduction

### 6.1.1 What is a Fluid?

A fluid can be defined as a substance which, when a fixed quantity of the substance is taken, this material assumes the shape of the container that holds it as contrasted to a solid which is a fixed shape (liquid takes half of bottom of container if not enough present). A fluid can be either a gas or a liquid.

### 6.1.2 Classes of Fluids

There are two major classes of fluids, Newtonian and non-Newtonian. We are concerned in this course, and in the natural gas industry, primarily with Newtonian fluids. However, we should define the two classes. For example, a non-Newtonian fluid is a material like a plastic or tar, etc. and is often characterized by a minimum force required to cause flow, or the shear stress is not directly proportional to the rate of shear stress. Figure 6.1 shows the difference between the two classes.


Figure 6.1: Newtonian and Non-Newtonian Fluid Properties
Another way to show the difference between Newtonian and non-Newtonian fluids is to plot the viscosity versus the shear rate as shown in Figure 6.2. For Newtonian fluid, the viscosity " $\mu$ " is a constant at a set temperature while for a non-Newtonian, it is not.


Figure 6.2: Newtonian and Non-Newtonian Fluid Viscosities

### 6.1.3 Other Comments

We also wil limit ourselves to systems in which the fluid is a continuous substance, ie. we are not considering systems in which there are only a few molecules present as different laws apply, (high vacuum, etc.).

### 6.1.4 Definitions

Let us define some common physical properties of a fluid:

## Density

$\rho=$ mass of substance per unit volume, normally lbs/cu.ft., $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$.

## Viscosity

$\mu=$ a particular fluid property. It is the internal friction in a fluid that reduces flow. It is defined as:

$$
\mu=\frac{\text { ShearingStress }}{\text { Rate of Shearing Strain }}
$$

Or we can consider the following diagram:


Figure 6.3: Physical Properties of Fluid
The Force (F) per unit area (A) applied to make the top layer move at a velocity (dv) a distance (dy) from the stationary plane can be expressed by the following equation:

$$
\frac{F}{A}=\mu \frac{d v}{d y} \quad \text { or } \quad=\mu \frac{d \gamma}{d t}
$$

where:

$$
\begin{aligned}
& \mu=\text { the viscosity of the fluid } \\
& y=\text { shear stress } \\
& t=\text { time }
\end{aligned}
$$

This property has the dimensions of $\frac{\text { mass }}{\text { length - time }}$ and is normally expressed as centipoise in the metric system. There are many other units that viscosity is expressed in due to the variety of means of measuring it, ie. Saybolt, Kinematic, Engler, etc.

## Reynolds Number

Another well known item concerned with. fluids is the Reynolds number. This is defined as follows.
Equation 6-2

$$
\operatorname{Re}=\frac{(\text { Diameter of Pipe })(\text { Velocity of fluid })(\text { Density of fluid })}{\text { Vis } \cos \text { ity of fluid }}=\frac{D v \rho}{\mu}
$$

The Reynolds Number is important as it defines the fluid in a system, because fluids that have the same Reynolds Number are dynamically similar and when applied to geometrically similar systems, they behave identically. For example, the friction factor " $f$ " is correlated against the Reynolds Number.

### 6.1.5 Symbols

In the course of this section we will be using many symbols. The main ones are as follows, along with the common units:

```
F = Force (lbs normally) [Newton]
\rho= Density (lbs/cu.ft.) [kg/m}\mp@subsup{}{}{3}
\mu= Viscosity ( }\frac{lbs}{ftx\operatorname{sec}}\mathrm{ ) [or in poises or }\frac{kg}{m-\operatorname{sec}}\mathrm{ ]
D = Pipe diameter (ft) [m]
d = pipe diameter (in) [cm or mm]
v = Velocity (ft/sec) [m/sec]
G = Mass velocity (lbs/ft }\mp@subsup{}{}{2}\textrm{sec})[\textrm{kg}/\mp@subsup{\textrm{m}}{}{2}/\textrm{sec}
gc}=\mathrm{ Gravity (32.2 ft/sec}\mp@subsup{}{}{2})[980 cm/\mp@subsup{sec}{}{2}] note: sometimes has unit \frac{ft}{h\mp@subsup{r}{}{2}
w = Work (BTUs or ft. Ibs} [kilojoules]
```

$\mathrm{q}=$ Heat (BTUs or ft. Ibs\} [kilojoules]
$Q=$ Flow (SCFH or SCFD) [ $\mathrm{m}^{3} / \mathrm{Hr}$ or $\mathrm{m}^{3} / \mathrm{day}$ ]
$\mathrm{z}=$ Height or Potential (ft) [m]
Z = Compressibility Factor
$\mathrm{u}=$ Internal Energy (BTUs or ft. Ibs) [kilojoules]
$\mathrm{L}=$ Length of pipe (ft or miles) [ m ]
$\mathrm{W}=$ Mass flow $\frac{l b}{\sec }\left[\frac{\mathrm{~kg}}{\mathrm{se}}\right]$
$\mathrm{A}=$ Cross-sectional area $\left(\mathrm{ft}^{2}\right)\left[\mathrm{m}^{2}\right]$
$\mathrm{V}=$ Volume (normally specific volume, cu.ft./lb) $\left[\mathrm{m}^{3} / \mathrm{kg}\right]$
P = Pressure (normally psi) [kpa]
$\mathrm{T}=$ Temperature (normally in ${ }^{\circ} \mathrm{R}$ ) $\left[{ }^{\circ} \mathrm{K}\right]$
$\mathrm{S}=$ Gas gravity compared to air $=1.0$

### 6.2 Energy Equations

### 6.2.1 The Drag Law

Whenever a fluid flows past a solid object or a solid object passes through a fluid, a force "F" is required to overcome the friction developed. This can be expressed by the equation:

$$
F=\frac{f^{\prime} \rho A v^{2}}{2 g_{c}}
$$

where:
$\mathrm{A}=$ the area of the solid in contact with the fluid.
$f^{\prime}=$ the factor dependent only on Reynolds Number for the system.
$\mathrm{V}=$ the velocity of the fluid.
$g_{c}=$ the gravity.
$\rho=$ the density of the fluid.

### 6.2.2 Energy Equation

Consider the following system for 1 lb . (or 1 kilogram) of material flowing:


Figure 6.4: Material Flowing Through a Heat Exchanger
An energy equation can be written from Point 2 as compared to Point 1.
Equation 6-4

$$
u_{2}+\frac{v_{2}^{2}}{2 g_{c}}+z_{2}+P_{2} V_{2}=u_{1}+\frac{v_{1}^{2}}{2 g_{c}}+z_{1}+P_{1} V_{1}+q+w
$$

or

$$
\Delta u+\Delta\left(\frac{v^{2}}{2 g_{c}}\right)+\Delta z+P V=q+w
$$

Let $\ell w=$ lost work (work to overcome friction or other changes). This would be part of the term " $w$ " in (5) above. However, let us consider the case where no outside work occurs. We will also consider the case in which there is no outside heat. Equation (5) reduces to

Equation 6-6

$$
\int_{1}^{2} V d P+\Delta\left(\frac{v^{2}}{2 g_{c}}\right)+\Delta z+l w
$$

For an incompressible fluid this can be expressed as:
Equation 6-7

$$
\frac{\Delta P}{\rho}+\Delta\left(\frac{v^{2}}{2 g_{c}}\right)+\Delta z=l w
$$

### 6.2.3 Basic Equation for Incompressible Flow

Equation (7) can be used to develop the Fanning Equation or the Darcy Equation for flow in pipes. Let us consider the Drag Equation for flow in pipes where $F$ (force) is required to overcome friction.

$$
F^{\prime}=f^{\prime} \frac{\rho \pi D L v^{2}}{2 g_{c}}
$$

The area is $\pi \mathrm{DL}$.


Assume that the fluid moves a distance dL then the energy lost in ft . Ibs. is FdL. This is equal to the lost work, $\ell w$. Now the mass of fluid moved is equal to:

$$
\frac{\rho \pi D^{2} d L}{4}
$$

or $\ell w$ per unit mass of fluid is expressed as follows:

$$
l w=\frac{F^{\prime} d L}{\rho \pi D^{2} d L / 4}=\frac{4 F^{\prime}}{\rho \pi D^{2}}
$$

Now, replacing F' from (8) we have:
Equation 6-10

$$
l w=\frac{2 f^{\prime} L v^{2}}{D g_{c}}
$$

Now substitute in the energy equation for a non-compressible fluid in which there is no change in elevation or potential energy or change in velocity. (Equation (7) modified).

Equation 6-11

$$
l w=\frac{\Delta P}{\rho}=\frac{2 f^{\prime} L v^{2}}{D g_{c}}
$$

This is a form of the Fanning Equation.
Now let $f=4 f^{\prime} \quad f^{\prime}=\frac{f m}{4}$
We can now express the pressure loss in the familiar Darcy Equation where " f " is the regular friction factor. (Moody Friction factor)

$$
\Delta P=\frac{f m \rho L v^{2}}{2 g_{c} D} \quad \text { in } l b / f t^{2}
$$

or the Darcy Equation in Ibs/in ${ }^{2}$
Equation 6-13

$$
\Delta P=\frac{\rho f m L v^{2}}{144 D\left(2 g_{c}\right)}
$$

Note: The friction factor is sometimes expressed as the Fanning Friction - Factor ff which is $1 / 4$ of fm.

### 6.2.4 Friction Factor

The friction factor has been correlated vs Reynolds Number. In Figure 6.5, this so called Moody diagram gives different values for different types of flow. These types of flow are listed below:

## Laminar Flow

A flow in which fluid flows in straight lines, occurs below Re. $=2000$

## Transition Range

Between Re. $=2000$ to 4000

## Turbulent Flow

Above $\mathrm{Re} .=4000$. We normally have this type of flow.
Note: The roughness of pipe affects the friction factor. (Does not drop very fast with increasing Re. No. in rough pipe). This is the value $\varepsilon / D$ shown in Figure 6.5 and 6.8.


Figure 6.5: Friction Factors for Commercial Pipe

### 6.2.5 Flow Pattern in Pipe

Let us consider flow patterns in pipe. Figure 6.6 shows some typical flow patterns.


Figure 6.6: Flow Patterns in Pipe
This can be contrasted if the ratio of the average velocity " $v$ " divided by $\mathrm{v}_{\text {max }}$ is plotted against Re . Number.


Figure 6.7: Velocity Profile vs Reynolds Number

### 6.3 Liquid Flow

We are concerned primarily with the flow of liquids in pipes and will not discuss flow over weirs or in channels. There are many formulas giving the pressure drop in pipes. In GPSA Data Book on pages 10-10 and 10-11 charts these are giving pressure drops in psi/l00 ft. Also data in kpa/l00 m are given in the SI GPSA Data Book on the same page number.
A good basic formula that can be used is the Darcy-Wiesbach formula (for turbulent flow).

$$
\Delta P=\frac{f W^{2} L}{5715 \rho D^{5}}
$$

where:

$$
\Delta \mathrm{P}=\text { pressure drop psi }
$$

$f=$ friction factor from Colebrook-White chart (Figure 6.8 or Figure 6.5). (fm - Moody Value)
W = Flow, lbs/sec.
$\rho=$ density, lbs/cu.ft.
$\mathrm{D}=$ inside diameter in ft .
$L=$ length in feet.
As can be seen from Figure 6.8, "f" is a function of the Re. No. and the roughness factor "e" and thus e/D.
If we have laminar flow, we can find " f " from the Hagen-Poiseuille Law which is:
Equation 6-15

$$
f=\frac{64}{\operatorname{Re}}
$$

where:

$$
\text { Re }=\text { the Reynolds Number. }
$$

Another way of obtaining the pressure drop is to use the data as given in the Ingersoll Rand's "Cameron Hydraulic Data" in which the pressure drop (head loss) for various sizes of pipe is given for water and HC fluids against a viscosity. This is also reproduced in Ludwig, Vol. I, P.78.

Because of the complexity of elbows, tees, valves, etc., it is not possible or correct to just take the straight length of pipe. All fittings have to be taken into account, thus an equivalent length is calculated. This is straight length plus equivalent length of fittings as determined from Fig. 10-14, GPSA Data Book.

If you do not have the actual number of elbows, tees, etc., use at least $20 \%$ of straight length pipe in process plants and $10 \%$ for pipelines.

We have been concerned with measuring pressure drop. Actually prime concern is to determine the most economic size. This is a balance between pressure drop and power required for pumping, as is shown in Figure 6.9.
This optimum size has been worked out for several conditions. The following table gives some economic velocities. This table applies primarily to pump and compressor discharge piping.

Table 6.1: Recommended Velocities in Pipe

| Fluid Density |  | Optimum Velocity |  |
| :--- | :--- | :--- | :--- |
| Ibs/cu.ft. | $\mathbf{k g} / \mathbf{m}^{\mathbf{3}}$ | $\mathrm{ft} / \mathbf{s e c}$ | $\mathrm{m} / \mathbf{s e c}$ |
| 100 | $(16.018)$ | $5.1-8.0$ | $(1.55-2.43)$ |
| 50 | $(8.009)$ | $6.2-10.0$ | $(1.9-3.05$ |
| 10 | $(1.602)$ | $10-16$ | $(3.05-4.87)$ |


| 1 | $(0.160)$ | $19.5-31$ | $(5.94-9.5)$ |
| :--- | :--- | :--- | :--- |
| 0.1 | $(0.016)$ | $39-59$ | $(11.9-18.0)$ |
| 0.01 | $(0.0016)$ | $78-112$ | $(23.8-34.2)$ |



Figure 6.8: Friction Factor VS Reynolds Number


Figure 6.9: Optimum Pipe Size Determination
This data can also be expressed more specifically for particular services as follows:

## Suggested Allowable Velocities or Pressure Drops in Process Plants

The following data is to be used as a guide. A thorough review of the actual installation should always be made.

Table 6.2: Liquids - Allowable Velocities

|  | $\mathrm{ft} / \mathbf{s e c}$ |  |  |
| :--- | :--- | :--- | :--- |
|  | Boiling Liquids | Light Hydrocarbons and Water | Viscous Oil, Etc. |
| Pump Discharge | $5-8$ | $5-8$ | $3-5$ |
| Pump Suction | 1 (max) | 3 (max) | 1 (max) |
| Gravity Flow | $0.5^{*}$ | $2.5^{*} \quad 1-2$ * |  |
|  | meters/sec |  |  |
|  | Boiling Liquids | Light Hydrocarbons and Water | Viscous Oil, Etc. |
| Pump Discharge | $1.5-2.4$ | $1.5-2.4$ | $0.9-1.5$ |
| Pump Suction | 0.3 (max) | 1 (max) | 0.3 (max) |
| Gravity Flow | $0.15^{*}$ | $0.8^{*}$ | $0.3-0.6$ * |

* Should check on the pressure drop available basis also.


## Table 6.3: Gases - Allowable Velocities

|  | $\mathrm{ft} / \mathbf{s e c}$ | $\mathrm{m} / \mathbf{s e c}$ |
| :--- | :--- | :--- |
| Pressure (atmospheric) | $80-100$ | $24.4-30.4$ |
| $\mathbf{1 0 0} \mathbf{~ p s i g}$ | $60-80$ | $18.3-24.4$ |
| $\mathbf{2 0 0} \mathbf{~ p s i g}$ | $50-60$ | $15.2-18.3$ |
| $\mathbf{3 0 0} \mathbf{~ p s i g}$ | $40-50$ | $12.2-15.2$ |
| $\mathbf{5 0 0} \mathbf{~ p s i g}$ | $30-40$ | $9.1-12.2$ |
| $\mathbf{1 0 0 0} \mathbf{~ p s i g}$ | $10-20$ | $3.05-6.1$ |
| Compressor Suction | 30 | 9.1 |
| Compressor Discharge | 70 | 21.3 |

Table 6.4: Vacuum Systems - Allowable Pressure Drop

| Vacuum | psi/100 ft |
| :--- | :--- |
| $28^{\prime \prime}$ of Mercury | 0.05 |
| $25^{\prime \prime}$ of Mercury | 0.10 |
| $15^{\prime \prime}$ of Mercury | 0.15 |

Table 6.5: Steam Systems - Allowable Pressure Drop

| Steam Pressure PSIG | PSI/100 ft |
| :--- | :--- |
| $10-50$ | 0.5 |
| $50-500$ | 1.0 |
| 500 and greater | 1.5 |

The problem of long transmission lines is slightly different. Since the cost of pump stations is higher than pumps alone, higher velocities probably can be used. However, an economic balance equation should be developed. For rough sizing about 6 to 10 psi per mile can be used. Also, pump stations are usually located every 100 miles or less. However, this is a balance. Pump discharge pressure is normal maximum for pipe, i.e. $1440 \mathrm{psig}(10,024 \mathrm{KPa})$ or 720 psig ( 5065 KPa ) depending on the flange rating of the valves in the system.

## Example Problem 6.1

You are to size the butane splitter feed and bottoms piping from the feed drum to the tower as shown by the sketch below.


## Solution

| Line No. | Flow (Usgpm) | Service | Allowable Velocity (ft/sec) | Size (inches) | Pressure Drop (Psi/100 ft) | Velocity (ft/sec) | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 234 | Pump Suction | 1 | 10 | 0.02 | 0.9 |  |
| 2 | 234 | Pump Discharge | 5-8 | 4 | 0.75 | 6 |  |
| 3 | 146 | Rundown to Storage | 5-8 | 3 | 1.2 | 6 | * |

* Should check length of line and available pressure drop. It may be that 4 inches is best.

| Line No. | Flow (m ${ }^{\mathbf{3} / \mathrm{hr})}$ | Service | Allowable Velocity <br> $(\mathbf{m} / \mathbf{s e c})$ | Size (mm) | Pressure Drop <br> $(\mathbf{k p a / 1 0 0} \mathbf{~ m})$ |
| :---: | :---: | :--- | :---: | :---: | :---: |
| $\mathbf{1}$ | 53.14 | Pump Suction | 0.3 | 254 | 2 |
| $\mathbf{2}$ | 53.14 | Pump Discharge | $1.5-2.4$ | 101.2 | 30 |
| $\mathbf{3}$ | 33.16 | Rundown to Storage | $1.5-2.4$ | 75 | 45 |

## Control Valves

Another item to consider is control valve sizing. Generally it is best to let a process control valve take about one third of the available pressure drop in the system.

### 6.4 Gas Flow

The flow of gas is complicated because it is compressible and the pV in the flow equation cannot be reduced to Vdp but the term pdV has to be considered also. This pdV term is, however, cancelled out in the general equation by a change in internal energy due to a change in pressure. We have to consider two types of flow:

## Adiabatic Flow

Flow is an insulated pipe in which no heat is transferred. The gas law equation for this is:
Equation 6-16

$$
P V^{k}=\text { Constant }
$$

or

$$
\left(\frac{P_{2}}{P_{1}}\right)=\left(\frac{V_{1}}{V_{2}}\right)^{k}
$$

where

$$
k=\frac{C_{P}}{C_{V}}
$$

## Isothermal flow

The gas is kept at a constant temperature. The gas law equation for this condition is such that

$$
\frac{P_{2}}{P_{1}}=\frac{V_{1}}{V_{2}}
$$

Isothermal flow is usually taken for flow in long pipelines and formulas developed for flow in pipelines are usually based on isothermal flow. For flow through nozzles at high speeds, etc. adiabatic flow is considered.

### 6.4.1 Adiabatic Flow

Let us firsts consider adiabatic flow $\mathrm{q}=0$. Assume work $=0$ and potential is zero, then

$$
P_{1} V_{1}=U_{2}-U_{1}+\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}+P_{2} V_{2}
$$

Now

$$
C_{V}\left(T_{2}-T_{1}\right)=U_{2}-U_{1}
$$

and

$$
P V=R T
$$

also

$$
C_{V}=\frac{R}{k-1}
$$

where:
$k$ is the ratio of specific heats.
Therefore

$$
\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=P_{1} V_{1}-P_{2} V_{2}+C_{V}\left(T_{1}-T_{2}\right)
$$

$$
\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=P_{1} V_{1}-P_{2} V_{2}+\frac{P_{1} V_{1}}{k-1}-\frac{P_{2} V_{2}}{k-1}
$$

or

$$
\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=\frac{k}{k-1}\left(P_{1} V_{1}-P_{2} V_{2}\right)
$$

Now, for adiabatic reversible flow

$$
\frac{P_{2}}{P_{1}}=\left(\frac{V_{1}}{V_{2}}\right)^{k}=\left(\frac{\rho_{2}}{\rho_{1}}\right)^{k}
$$

Equation (24) becomes

$$
\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=\left(\frac{k}{k-1}\right)\left(\frac{P_{1}}{\rho_{1}}\right)\left[1-\left(\frac{P_{2}}{P_{1}}\right)^{\frac{k-1}{k}}\right]
$$

We can use this equation for gas flow through nozzles, orifices, flow meters. For example, if W is the weight of gas passing through a nozzle, $W$ at the throat of a nozzle

$$
W=\frac{A_{2} v_{2}}{V_{2}}
$$

and assuming $v_{1}^{2}$ is small, we obtain

$$
W=A \sqrt{\left(\frac{2 k g_{c}}{k-1}\right)\left(\frac{P_{1}}{V_{1}}\right)\left(\frac{P_{2}}{P_{1}}\right)^{\frac{2}{k}}-\left(\frac{P_{2}}{P_{1}}\right)^{\frac{k-1}{k}}}
$$

If plot of W versus $\frac{P_{2}}{P_{1}}$ is made we will get a plot as is shown in Figure 6.10.


Figure 6.10: Maximum Flow of Compressible Fluid
The maximum rate of flow can be found by differentiating $W$ with respect to $P_{2}$ and settling result to 0 . Call $\mathrm{P}_{2}$ at this condition $\mathrm{P}_{\mathrm{c}}$.

$$
\frac{P_{c}}{P_{1}}=\left(\frac{2}{k+1}\right)^{\frac{1}{k-1}}
$$

The velocity at this point can be shown to be:
Equation 6-30

$$
v_{c}=\sqrt{\frac{2 g_{c}}{k+1} k\left(P_{1} V_{1}\right)}=\sqrt{\frac{k P_{c}}{\rho_{c}}}
$$

or, in English units

$$
v_{c}=\sqrt{k g_{c} T_{c} \frac{z_{c} R}{M}}
$$

which is the velocity of sound at the critical pressure.
where:
$\mathrm{v}_{\mathrm{c}}=$ velocity of sound, $\mathrm{ft} / \mathrm{sec}$
$\mathrm{g}_{\mathrm{c}}=$ gravity, $32.2 \mathrm{ft} / \mathrm{sec}^{2}$
R = $1541 \mathrm{ft} . \mathrm{lbs} /$ mole
$\mathrm{M}=$ mole weight of gas in lbs
$Z_{c}=$ compressibility factor at outlet conditions or when velocity reaches that of sound.
$T_{c}=$ Temperature when gas is at velocity of sound or at pressure $P_{c}$ in ${ }^{\circ} R$.
Note: The velocity of sound is the maximum velocity that can occur in gas pipes. This occurs at end of pipe. A reduction of the pressure below the value of $P_{c}$ or when $P_{2}<0.5 P_{1}$ will not increase the flow.

Field flare stacks are sometimes sized for close to sonic velocities when the maximum amount of gases are being flared. (Usually 0.8 of sonic velocity). Plant flare stacks are sized at lower sonic velocities, about 0.2 of sonic velocities. This lower value is necessary as higher than 0.2 can often cause blow out of a flame.

### 6.4.2 Isothermal Flow

Next let us consider isothermal flow which, is the normal flow in most gas gathering lines, pipelines, etc. If we assume:

1. No mechanical work in system
2. Have horizontal flow.
we can write the general energy equation in the following form:

$$
V d P+\frac{d\left(v^{2}\right)}{2 g_{c}}+d R=0
$$

Change in pressure + Change in velocity + Lost work to overcome friction $=0$
Now

$$
d R=\frac{f v^{2} d l}{2 g_{c} D}
$$

(This is the drag law)
where:

$$
\ell=\text { length of line. }
$$

Equation becomes:

$$
V d P+\frac{v d V}{g_{c}}+\frac{f v^{2} d l}{2 g_{c} D}=0
$$

or

$$
\frac{2 g_{c} V d P}{v^{2}}+\frac{2 d v}{v}+\frac{f d l}{D}=0
$$

Integrating this equation between points 1 and 2 we obtain:

$$
P_{1}^{2}-P_{2}^{2}=\frac{v_{1}^{2} P_{1}}{g_{c} V_{1}}\left[2 \ln \frac{v_{2}}{v_{1}}+\frac{f l}{D}\right]
$$

or if we neglect the acceleration or kinetic energy change we can obtain the equation for long pipes

$$
\frac{f l}{D} \gg 2 \ln \frac{v_{2}}{v_{1}}
$$

$$
\frac{P_{1}^{2}-P_{2}^{2}}{P_{1}^{2}}=\frac{f l v_{1}^{2}}{g_{c} D_{1} P_{1} V_{1}}
$$

or

$$
P_{1}-P_{2}=P_{1}\left[1-\sqrt{1-\frac{f l v_{1}^{2}}{g_{c} D P_{1} V_{1}}}\right]
$$

### 6.4.3 Common Formula for Gas Flow

We can change the above equation to units in which we have a friction factor and common units. A typical equation that covers all cases for horizontal flow:

$$
Q=K \frac{T_{s}}{P_{s}}\left[\frac{\left(P_{1}^{2}-P_{2}^{2}\right) d^{5}}{f L S T Z_{a}}\right]^{\frac{1}{2}}
$$

where:

|  | English Units | Metric Units |
| :---: | :---: | :---: |
| Q - Flow in | SCFD | $\mathrm{m}^{3} / \mathrm{D}$ |
| P - Pressure in | psia | bars $=\frac{k P a}{100}$ |
| $P_{s}$ - Pressure base in | psia | $\text { bars }=\frac{k P a}{100}$ |
| $\mathrm{T}_{\mathrm{s}}$ - Temperature base in | ${ }^{\circ} \mathrm{R}$ | ${ }^{\circ} \mathrm{K}$ |
| T- Operating temperature in | ${ }^{\circ} \mathrm{R}$ | ${ }^{\circ} \mathrm{K}$ |
| d - Pipe diameter in | inches | cm |
| L - Pipe length in | miles | km |
| S - gas specific gravity | ---- | ---- |
| Za - average compressibility between that at $P_{1}$ and $P_{2}$ | ---- | ---- |
| f - Friction factor | See Figure 6.11 | ---- |
| k | 38.77 | 0.1842 |



Figure 6.11: Recommended Friction Factors for Gas Flow

A short discussion of finding $\frac{1}{f}$ is desirable. The factor is correlated against the Re. No. and $\frac{\varepsilon}{D}$, the roughness factor. $\varepsilon$ is the height of the roughness in inches and $D$ is the diameter in inches (Or these could be in cm ). Here are some roughness data.

Table 6.6: Roughness Data

| Low Pressure | Pipe Size | $\boldsymbol{\varepsilon}$ |
| :--- | :--- | :--- |
| $\left(4{ }^{\prime \prime}-10\right.$ " of $\mathrm{H}_{9}$ Vacuum $)$ | $2-8$ | $0.01^{\prime \prime}$ |
| $\left(100-250\right.$ mm of $\left.\mathrm{H}_{9}\right)$ | $8-30$ | $0.007^{\prime \prime}$ |
| Med. Pressure |  |  |
| $(2-10$ psig $)$ | All | $0.0025^{\prime \prime}$ |
| $(15-170$ kpa $)$ | All | $0.0025^{\prime \prime}$ |
| High Pressure |  |  |
| $(>10$ psig $)$ | All | $0.0025^{\prime \prime}$ |
| $(170$ kpa $)$ | All | $0.0025^{\prime \prime}$ |
| New Pipe | All | $0.0007^{\prime \prime}$ |
| 5 yrs old | All | $0.002^{\prime \prime}$ |
| 10 yrs old | All | 0.0025 |
| 15 yrs old | $0.003^{\prime \prime}$ |  |

There are some other well known empirical formulas. In these the friction factor is expressed as a function of either the Diameter (Weymouth) or the Re. No. (Panhandle).
The Weymouth formula which is often used assumes that $\frac{1}{f}$ is a function of the diameter "d".
That is:

$$
f=\frac{0.032}{d^{\frac{1}{3}}}
$$

The formula is:

$$
Q=433.5 \frac{T_{b}}{P_{b}}\left[\frac{P_{1}^{2}-P_{2}^{2}}{S T L Z_{a}}\right]^{\frac{1}{2}} d^{2.667}
$$

or S.I.

$$
Q=0.0037 \frac{T_{b}}{P_{b}}\left[\frac{P_{1}^{2}-P_{2}^{2}}{S T L Z_{a}}\right]^{\frac{1}{2}} d^{2.667}
$$

where:
$\mathrm{d}=$ pipe diameter in inches (mm)
$L=$ line length in miles (If $L$ in feet constant is (km) 30,490 instead of 433.5)
$P_{1}, P_{2}=$ pressure in psia at points 1 and 2
$Q=$ SCFD at $T_{b}$ and $P_{b}\left(\mathrm{~m}^{3} / \mathrm{d}\right)$
$S=$ specific gravity
$\mathrm{T}={ }^{\circ} \mathrm{R}\left({ }^{\circ} \mathrm{K}\right)$
$\mathrm{T}_{\mathrm{b}}=$ base temp ${ }^{\circ} \mathrm{R}\left({ }^{\circ} \mathrm{K}\right)$
$\mathrm{P}_{\mathrm{b}}=$ base pressure, psia (Kpa)
Charts in the GPSA Data Book plot (Page 10-3) plot flows vs $P_{1}^{2}-P_{2}^{2} / \mathrm{km}$ and pipe sizes for the formula. The Weymouth formula is usually used for sizing gathering lines.
Another common formula is the Panhandle. Here the friction factor is taken as:

$$
\frac{1}{f}=\theta(\operatorname{Re})^{0.73}
$$

This formula is given on the following pages. Please note that $E$ is the pipeline efficiency 0.92 for clean transmission lines and 0.88 for gathering lines.
Note: $\quad E$ is the pipeline efficiency usually it is taken as 0.92 , but can vary from 0.85 to 0.95 depending on operating conditions.

### 6.4.3.1 Summary of Equations for Single Phase Gas Pipelines Using One-Step Calculation Procedure

## Capacity

## General Equation

$$
Q=K E\left(\frac{T_{b}}{P_{b}}\right)^{\alpha}\left(\frac{P_{1}^{2}-P_{2}^{2}}{T_{a} L Z_{a}}\right)^{\beta} \frac{D^{\chi}}{S^{v}}
$$

| Equation | System of Units | K | $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{\gamma}$ | $\boldsymbol{v}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Panhandle | Field | 435.87 | 1.0788 | 0.5394 | 2.6182 | 0.4606 |
| Panhandle | SI | $4.596 \times 10^{-3}$ | 1.0788 | 0.5394 | 2.6182 | 0.4606 |
| Panhandle <br> Eastern | Field | 737 | 1.02 | 0.510 | 2.530 | 0.490 |
| Panhandle <br> Eastern | SI | $10.02 \times 10^{-3}$ | 1.02 | 0.510 | 2.530 | 0.490 |

## Upstream and Downstream Pressures

General Equations

$$
\begin{aligned}
& P_{1}=\left\{P_{2}^{2}+K\left(\frac{Q}{E}\right)^{\alpha}\left(\frac{P_{b}}{T_{b}}\right)^{\beta} \frac{S^{\chi}}{D^{v}} T_{a} L Z_{a}\right\}^{1 / 2} \\
& P_{2}=\left\{P_{1}^{2}-K\left(\frac{Q}{E}\right)^{\alpha}\left(\frac{P_{b}}{T_{b}}\right)^{\beta} \frac{S^{\chi}}{D^{v}} T_{a} L Z_{a}\right\}^{1 / 2}
\end{aligned}
$$

| Equation | System of Units | $\mathbf{K}$ | $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{\gamma}$ | $\boldsymbol{v}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Panhandle | Field | $1.279 \times 10^{-5}$ | 1.8539 | 2 | 0.8539 | 4.8539 |
| Panhandle | SI | $2.157 \times 10^{4}$ | 1.8539 | 2 | 0.8539 | 4.8539 |
| Panhandle <br> Eastern | Field | $2.385 \times 10^{-6}$ | 1.9608 | 2 | 0.9608 | 4.9608 |
| Panhandle <br> Eastern | SI | $8.315 \times 10^{3}$ | 1.9608 | 2 | 0.9608 | 4.9608 |

## Diameter

## General Equation

$$
D=K\left(\frac{Q}{E}\right)^{\alpha}\left(\frac{P_{b}}{T_{b}}\right)^{\beta}\left(\frac{T_{a} L Z_{a}}{P_{1}^{2}-P_{2}^{2}}\right)^{\chi} \frac{S}{1}
$$

| Equation | System of Units | K | $\boldsymbol{\alpha}$ | $\boldsymbol{\beta}$ | $\boldsymbol{\gamma}$ | $\boldsymbol{v}$ |
| :--- | :--- | :--- | ---: | ---: | ---: | ---: |
| Panhandle | Field | 0.0982 | 0.3819 | 0.4120 | 0.2060 | 0.1759 |
| Panhandle | SI | 7.8133 | 0.3819 | 0.4120 | 0.2060 | 0.1759 |
| Panhandle <br> Eastern | Field | 0.0736 | 0.3953 | 0.4032 | 0.2016 | 0.1937 |
| Panhandle <br> Eastern | SI | 6.1684 | 0.3953 | 0.4032 | 0.2016 | 0.1937 |

## Definition of Parameters and Units

| Parameter | Definition | Units |  |
| :---: | :---: | :---: | :---: |
|  |  | Field | SI |
| D | Inside diameter of pipe. | inch | mm |
| E | Pipeline efficiency factor, expressed as a fraction | -- | ---- |
| S | gas gravity relative to air = 1 | ---- | ---- |
| L | total length of pipeline | mile | km |
| $\mathrm{P}_{\mathrm{b}}$ | reference pressure for standard conditions | psia | kPa |
| $\mathrm{P}_{1}$ | upstream pressure | psia | kPa |
| $\mathrm{P}_{2}$ | downstream pressure | psia | kPa |
| Q | gas flow rate at standard conditions | $\mathrm{ft}^{3} /$ day at $\mathrm{T}_{\mathrm{b}}, \mathrm{P}_{\mathrm{b}}$ | $\mathrm{m}^{3} /$ day at $\mathrm{T}_{\mathrm{b}}, \mathrm{P}_{\mathrm{b}}$ |
| $\mathrm{T}_{\mathrm{b}}$ | reference temperature for standard conditions | ${ }^{\circ} \mathrm{R}$ | ${ }^{\circ} \mathrm{K}$ |
| $\mathrm{T}_{\mathrm{a}}$ | average temperature of the flowing gas | ${ }^{\circ} \mathrm{R}$ | ${ }^{\circ} \mathrm{K}$ |


| $Z_{a}$ | average compressibility factor of the flowing gas | $----\quad---$ |
| :---: | :--- | :---: | :---: |

When there is a significant difference in head between the start and finish of a transmission loss the change of potential energy $\Delta \mathrm{z}$ must be taken into account. This can be done by the use of the following equation:

$$
\frac{\Delta z S}{A T_{a} Z_{a}}=\frac{\ln P_{1}}{P_{2}}
$$

where:

English Units
Metric Units
$\Delta z=$ head difference
ft
m
$S=$ gas gravity
$\mathrm{T}_{\mathrm{a}}=$ ave temperature
${ }^{\circ} \mathrm{R}$
${ }^{\circ} \mathrm{K}$
$\mathrm{Z}_{\mathrm{a}}=$ ave compressibility
$P_{1}=$ Pressure at 1
psia $\quad \frac{k p a}{100}$
$P_{2}=$ Pressure at 2
psia
$\frac{k p a}{100}$
A = Constant
54.34
29.28

When sizing short process lines in vapour service the following formula can be used:
$\Delta P_{100}=\frac{W^{2}}{e}\left(\frac{0.000336 f_{f}}{d^{5}}\right)$
where:
$\Delta \mathrm{P}_{100}=$ Pressure drop/I00 ft
$\mathrm{f}_{\mathrm{f}}=$ Fanning friction factor
$\mathrm{W}=$ Flow lbs/hr
$\rho=$ density lbs/cu.ft.
$d=$ diameter in inches
See GPSA Data book page 10-5 and 10-6 for solving this formula, or in metric units:

$$
\frac{\Delta P}{100 M}=\frac{W^{2}}{\rho}\left(\frac{62530 \times 10^{2} f}{d^{5}}\right)
$$

where:

$$
\begin{aligned}
& \Delta \mathrm{P}=\mathrm{kpa} \\
& \mathrm{f}=\text { Fanning Friction Factor } \\
& \mathrm{W}=\text { Flow } \mathrm{kg} / \mathrm{hr} \\
& \mathrm{~d}=\text { inside diameter in } \mathrm{mm} \\
& \rho=\text { density } \frac{\mathrm{kg}}{\mathrm{~m}^{3}}
\end{aligned}
$$

### 6.4.4 Line Sizing

The prime problem is to determine what size to make pipe for carrying gas. This again is an economic balance. The general data given in the table on optimum velocity can be given or the more detailed data given previously in Table 6.3: Gases - Allowable Velocities can be used.

### 6.4.5 Gathering Pipelines

For gathering lines from wells to a processing facility, etc. we have a different problem. The well initially can be at a very high pressure - 3000 to $5000 \mathrm{psig}(20,684$ to $34,473 \mathrm{kpa}$ ) depending on depth. It is necessary to do a study of the maximum pressure in the pipeline vs well deliverability vs wall thickness, etc. Usually the maximum pressure allowable in the line is 1440 psig, (about 10024 kpa) which is the maximum pressure rating for 600 ANSI raised face and ring joint flanges. There are, of course varying other pressures used depending on special circumstances, such as recycling, etc. For pressure drops varying values are used. They are affected by the length of the line, etc. About 10-50 psi/mile is sometimes used.
Also, if wellhead pressure is set by pipe flange considerations and the processing facility outlet condition is set by the transmission company (usually 900 psig ) then the allowable and available pressure drop is set. Example Problem 2 in Chapter 14 shows how a gathering system is sized.

### 6.4.6 Gas Transmission

To size gas transmission lines a different set of conditions have to be reviewed. A detailed study of pipe diameter versus compressor HP has to be made after the design volumes for both initial and future conditions have been determined. Some of the factors considered and the rules of thumb for initial design are:

1. Design pressure limitation - either 600 ANSI rating or 400 ANSI rating valves, flanges, etc., are used, usually 400.
2. The optimum compression ratio of generally taken as:

- for reciprocating machines -1.3 to 1.5 .
- centrifugal machines - 1.2 to 1.3.

3. The spacing of compressor stations is:

- reciprocating machines - 80-100 miles apart.
- centrifugal machines - 40-50 miles apart.

4. The pressure drop used is 5-15 psi per mile.
5. The ease of installing the pipe.
6. The place where looping will be done.
7. The storage of gas required.

### 6.4.7 Steam

Another fluid to be considered is steam flow. This is also a compressible fluid and the general flow equations could be used. However, a specific formula for saturated and superheated steam has been developed along with nomographs. Generally it is desirable to keep the pressure drop in steam lines low so as to prevent condensation. (See Fig. 10-10 in the GPSA Data Book for determining pressure drop in steam lines). For steam lines the following allowable pressure drops are often used:

- $1 \mathrm{lb} / 100 \mathrm{ft}$ for 50 to 500 psig systems.
- About 0.5 psig for 50 psig systems or lower pressures.
- For pressures above 500 psig, use $1.5 \mathrm{lbs} / 100 \mathrm{ft}$.

In terms of velocities, the following are often used:

- $20 \mathrm{psig}-100 \mathrm{ft} / \mathrm{sec}$
- $150 \mathrm{psig}-130 \mathrm{ft} / \mathrm{sec}$

In steam condensate systems, make sure the pressure drop is low, ie. about 0.5 psi per 100 ft .

### 6.5 Two Phase Flow

### 6.5.1 General

The next consideration is two phase flow. We are concerned with the flow of gas and liquids only. Flows of gases and solids such as occur in cat crackers or slurry flows do not concern us.

Two phase flow occurs quite commonly in gathering lines from wells to a processing facility. It is possible to separate at the wellhead and have a gas line and liquid line. However, even this does not solve the problem as retrograde condensation can cause liquid to form in the gas line and lowering of pressure can cause the liquid to vaporize.
What are some of the problems with two phase flow?

1. Gas and liquid tend to separate in the pipe and gas flows are 2 to 10 times faster than the liquid and thus leaves the liquid behind. There is a drag on the interface between the phases and roughness on surface. This consumes energy and causes increased pressure drop.
2. Liquid accumulates in valleys and thus increases pressure required to flow fluid.
3. Two phase lines are very unstable and have widely varying pressure drops. A change in flow rate causes a line to unload liquid or to accumulate it, thus the phenomenon of
slugging. A two phase line is actually a pipeline system that is an extremely long storage tank.

The total pressure drop in a two phase flow system is often expressed by the equation:
Equation 6-43

$$
\Delta P_{\text {total }}=\Delta P_{\text {two phase flow }}+\Delta P_{\text {elevation change }}+\Delta P_{\text {acceleration change }}
$$

The most important pressure drop considerations are the $\Delta P_{\text {two phase flow }}$ and the $\Delta P_{\text {elevation difference }}$. The pressure drop due to an acceleration change is usually neglected as was discussed when considering the equation for isothermal gas flow (See equation (35)).

### 6.5.2 Types of Flow

Let us review the various types of flow. Figure 6.12 shows several of the types of flow to be expected. For horizontal flow we can have:

1. Bubble Flow - In this, gas bubbles move along the upper section of the pipe at about the same velocity as the liquid. This is the same as froth flow in which the entire pipe is filled with a froth.
2. Plug Flow - In this flow there are alternating plugs of gas and liquid which move along the upper section of the pipe. The lower section is liquid.
3. Stratified Flow - Flow in which liquid flows along the bottom and gas along the top of the pipe.
4. Wave Flow - This is similar to stratified flow except that gas flows at high velocities and disturbs the interface so that waves are formed which travel in the direction of flow.
5. Slug Flow - A slug of liquid is formed from a wave and moves at much greater than normal velocity.
6. Annular Flow - Liquid forms a film around the pipe wall and gas flows at a higher velocity down the centre.
7. Spray or Dispersed Flow - In this flow, the liquid is entrained in minute drops and is dispersed throughout the gas.

A good review of two phase flow is an article by R. Kern. 1

### 6.5.3 Formulas for Various Types of Flow

The types of flow obtained under various conditions have been correlated as a function of the mass velocity "G" of the gas, the mass velocity of the liquid "L", the gas and liquid densities, the surface tension of the liquid and the viscosity of the liquid. Two parameters are used. They are:

Equation 6-44

$$
\lambda=\left[\left(\frac{\rho_{g}}{0.075}\right)\left(\frac{\rho_{L}}{62.3}\right)\right]^{1 / 2}
$$

and

$$
\Psi=\frac{73}{\chi}\left[u_{L}\left(\frac{62.3}{\rho_{L}}\right)^{2}\right]^{1 / 3}
$$

where:
$\gamma=$ the surface tension of the liquid.


Figure 6.12: Two Phase Flow Pattern Sketches
Figure 6.14 correlates the type of flow versus functions relative to the above referred to parameter, i.e. $\frac{G}{\lambda}$ and $\frac{L \lambda \psi}{G}$. It will be noted that in increasing the gas flow, generally the type of flow goes from stratified flow to dispersed flow. When increasing liquid flow we go from stratified flow through slug or plug flow to bubble or froth flow.
Baker gives equations for each type of flow. These equations are formulas for the function $\theta^{2}{ }_{G T T}$ where $\theta_{G T T}$ is the correction factor in the equation:

Equation 6-46

$$
\Delta P_{T P}=\Delta P_{G} \phi_{G T T}^{2}
$$

where:
$\Delta \mathrm{P}_{\mathrm{TP}}=$ pressure drop for two phases
$\Delta \mathrm{P}_{\mathrm{G}}=$ pressure drop for gas alone in total pipe
$\Delta P_{\mathrm{L}}=$ pressure drop for liquid alone in total pipe

The pressure drop, when both phases are in the turbulent range for two phase flow, is equal to the pressure drop due to gas alone multiplied by the correction factor $\theta^{2}{ }_{G T T}$.
All the equations are based on a factor $x$ which equals $\left(\frac{\Delta P_{L}}{\Delta P_{G}}\right)^{\frac{1}{2}}$.

## Froth or Bubble Flow

Equation 6-47

$$
\phi_{G T T}=\frac{14.2 x^{0.75}}{L^{0.1}}
$$

## Plug Flow

$$
\phi_{G T T}=\frac{27.315 x^{0.855}}{L^{0.17}}
$$

## Stratified Flow

$$
\phi_{G T T}=\frac{15400 x}{L^{0.8}}
$$

## Slug Flow

$$
\phi_{G T T}=\frac{1190 x^{0.815}}{L^{0.5}}
$$

## Annular Flow

Equation 6-51

$$
\phi_{G T T}=(4.8-0.3125 d)(X)^{0.343-0.021 d}
$$

Note: For Annular Flow only for up to 10" lines; above this, negative values are obtained, so use 10 " for sizes larger than 10 " as far as " $d$ " is concerned.
For dispersed flow use data from Figure 6.13 based on the Lockhart-Martinelli correlation for two phase flow. $x^{2}$ is found and then the two phase flow pressure drop is found by going over to the curve and then up to the gas phase pressure drop.
For wave flow use graph of work of Schnieder, White and Huntington shown in Figure 6.15, where:
"L" is the liquid mass flow, lb/hr/sq.ft. of total pipe cross sectional area.
" G " is the gas mass flow, lb/hr/sq.ft. of total pipe cross sectional area.
The term $x$ can be found quite simply by considering the general liquid and gas flow equations and deleting the appropriate constants and symbols.

Equation 6-52

$$
x^{2}=\left(\frac{\Delta P_{\text {liquid }}}{\Delta P_{g a s}}\right)=\left(\frac{L}{G}\right)^{1.8}\left(\frac{\rho_{g}}{\rho_{l}}\right)\left(\frac{\mu_{l}}{\mu_{g}}\right)^{0.2}
$$

and for hydrocarbon-liquid vapour mixtures flowing at equilibrium
Equation 6-53

$$
\begin{aligned}
& \left(\frac{\mu_{l}}{\mu_{g}}\right)^{0.2} \approx 1.6 \\
& x^{2}=1.6\left(\frac{L}{G}\right)^{1.8}\left(\frac{\rho_{g}}{\rho_{l}}\right)
\end{aligned}
$$

Another simplification that can often be made is to calculate the term $\frac{G}{\lambda}$ and if it is greater than 80,000 then the flow is dispersed (spray) and figure 6.13 can be used to find the two phase pressure drop. Figures 6.19 and 6.20 give a simple way of finding the two phase pressure drop for annular and bubble flow respectively. The method is the same as for dispersed flow. That is, find $x$, enter the nomograph against the appropriate line, go up to the appropriate $\Delta P$ for the vapour and read off the $\Delta P_{\text {two }}$ phase .


Figure 6.13: Two phase flow unit losses for dispersed flow


Figure 6.14: Flow Pattern Regions


Figure 6.15: Two-Phase Wave Flow


Figure 6.16: Liquid Holdup in Pipelines


Figure 6.17: Elevation Factor Correction Chart from Flanigan, Oil \& Gas Journal, March 1958


Figure 6.18: Flanigan Efficiency Factor

Flanigan Efficiency Factor for Metric Units



Figure 6.19: Annular Flow Unit Loss


Figure 6.20: Bubble Flow Unit Loss

### 6.5.4 Liquid Holdup

Before we consider pipeline design, we should mention liquid holdup. The percent volume of pipe occupied by liquid is correlated by the factor x . We can have up to $80 \%$ by volume liquid. Figure 6.16 shows this data. This figure also can be used to illustrate the instability of two phase lines as a slight change in $x$ can cause a considerable volume of liquid to come out of a line. For example, if the factor $x$ changes from 0.8 to 1.0 , the amount of liquid that will drop out is $5 \%$ of the total volume of the gathering system, which can be quite substantial. This explains the slugging that often occurs when increases in flows to a plant are required.

### 6.5.5 Pressure Drop Due to Elevation Change

In two phase flow liquid can accumulate in valleys, therefore it is necessary to allow for this in calculating the two phase pressure drop. This is done by the formula:

Equation 6-54

$$
\Delta P_{H}=\frac{\sum h F_{e} \rho_{L}}{144}
$$

where:

$$
\sum h=\text { height of the hills which the line covers }
$$

$$
F_{e}=\text { elevation factor }
$$

$$
\rho_{\mathrm{L}}=\text { liquid density }
$$

Note: $\quad F_{e}$ is obtained from data developed by Flanigan as a function of gas velocity and given in Figure 6.17.

### 6.5.6 Method of Flanigan ${ }^{5}$ for Two Phase

This is quite a simple method for calculating $\Delta P_{T P}$. It was developed for natural gas and condensate systems and probably is not applicable to other systems because physical properties of fluid are not taken into account. The method consists of finding a new efficiency factor "E" for the Panhandle formula. " $E$ " is a function of the liquid content and the gas velocity.

### 6.5.6.1 The Flanigan Procedure

a) Find superficial gas velocity (velocity with no liquid present) "U"
b) Find " $R$ ", the bbls of liquid per MMSCF of gas
c) Calculate $\frac{U}{R^{0.32}}$
d) Read off pipeline efficiency from Figure 6.18
e) Calculate pressure drop from the Panhandle formula, inserting proper pipeline efficiency.

Note: GE Time Sharing has this as a program. It is called FLANIS.

### 6.5.7 Method of Gregory, Mandhane and Aziz ${ }^{10}$

Recently Gregory and Aziz ${ }^{13}$, co-workers at The University of Calgary, developed a more sophisticated method for finding the pressure drop in two phase flow situations. They developed a slightly different flow diagram which is shown as Figure 6.21. This plots the superficial liquid velocity versus the superficial gas velocity. The various types of flow to be expected are shown on the diagram. Then after the type of flow is determined, a correlation for calculating the liquid holdup and pressure is selected according to the next table.

## Table 6.7: Suggested Methods for Pressure Drop and Hold Up Calculations

| Flow Regime | Holdup Prediction Method | Pressure Drop Prediction Method |
| :--- | :--- | :--- |
| Bubble, Elongated Bubble | Hughmark | Chenoweth and Martin |
| Stratified | Agrawal, Gregory and Govier | Agrawal, Gregory, and Govier |
| Wave | Chawla | Dukler, Wicks, and Cleveland |
| Annular, Annular Mist | Lockhart and Martinelli | Chenoweth and Martin |
| Dispersed | Beggs and Brill | Modified Lockhart and Martinelli |

Note: Computer programs for each of the available at the University of Calgary.
In particular, their method is as follows:

1. For the given transportation problem, the superficial gas and liquid velocities, $V_{S G}$ and $V_{S L}$ respectively, are calculated for the conditions existing at the inlet of the pipeline.
2. Using Figure 6.21 and the values of $V_{S G}$ and $V_{S L}$ calculated above, the expected flow pattern is determined.
3. Knowing the predicted flow pattern, one then selects the particular methods recommended for predicting the liquid holdup, $E_{L}$, and the friction pressure drop, $\Delta P_{f}$, from the table above.
4. The friction pressure drop, $\Delta P_{f}$, and liquid holdup, $E_{L}$, are calculated for an increment of pipe length using the methods selected above. The total pressure drop over the increment of pipe length is then determined from the relation,

Equation 6-55
$(\Delta P)_{\text {increment }}=\Delta P_{f}+\left(\Delta Z^{+}\right) \rho_{M}$
where
Equation 6-56
$\rho_{M}=\rho_{L} E_{L}+\rho_{G}\left(1-E_{L}\right)$
and $\Delta Z^{+}$is the change in elevation for which the flow is uphill. $\Delta Z^{+}$is zero for horizontal or downhill flow.
$\mathrm{E}_{L}$ is calculated from a holdup prediction method.
5. The procedure is then repeated for a new increment of pipe length, using the conditions at the downstream end of the previous increment as the basis of the calculation of new values of $V_{S G}$ and $V_{S L}$.
In practice, a rather involved computer program is required to properly follow this procedure. Determining the superficial velocities of the gas and liquid generally requires a phase behavior calculation; provision for this must be built into the program. As the conditions change along the pipeline, some provision must be made to account for changes in the physical properties of the gas and liquid phases. Since the amount of gas flowing in the pipeline generally increases with decreasing pressure, an iterative calculation is required over the incremental length to match the downstream pressure to the flowing phase volumes. This can be further complicated by the existence of a temperature gradient in the direction of flow. The pipeline profile must be available as input data; changes in the slope of the pipeline at irregular intervals require that a variable length increment be possible. This is also the case where the flow is predicted to pass through a flow pattern transition. For completeness, Equation (55) should also be modified to include pressure loss due to kinetic energy effects.
In short, the proposed design strategy is not well suited to hand calculations. However, in view of the general accessability of computers, this is not believed to be a serious limitation.

## Example Problem 6.2

Determine the size of a gas gathering line to handle 60 MMSCFD of a gas with an expected liquid content of 12 BBLs per MMSCF. The length of the line is 10.0 miles and the sum of the elevation difference is 500 ft . The gas is to be delivered to a processing plant at 950 psig . The maximum delivery pressure at the wellsite is 1200 psig. The average temperature in the pipeline is $70^{\circ} \mathrm{F}$.
Some of the properties of the gas are:
SG $=0.65$
$Z$ at average conditions $=0.800$
Actual density at average conditions $=7.100 \mathrm{lbs} / \mathrm{cu} . \mathrm{ft}$.
Some of the properties of the liquid are:

$$
\text { Density = } 44.0 \mathrm{lbs} / \mathrm{cu} . \mathrm{ft} \text {. }
$$

## Solution

Pressure drop available for flow $=250$ psi
Let us use the method of Flanigan. Assume 8 in. diameter pipe. Calculate U, superficial gas velocity, via Flanigan Formula.
where:

$$
\begin{aligned}
& U=\frac{31,194 Z Q}{P d^{2}} \text { in } \mathrm{ft} / \mathrm{sec} \\
& \mathrm{Q}=\text { Flow MMSCFD } \\
& \mathrm{P}=\text { Press psia }
\end{aligned}
$$

$d=$ diameter inches
$Z=$ compressibility factor


Figure 6.21: Two Phase Flow Types

$$
U=\frac{31194(60)(0.800)}{(8)^{2}(1100)}=21.3 \mathrm{ft} / \mathrm{sec}
$$

From chart, $\mathrm{F}_{\mathrm{e}}=0.12$
Pressure drop due to elevation difference

$$
\Delta P_{H}=\frac{\rho_{L} F_{e} \sum h}{144}=\frac{44(0.12)(500)}{144}=18.3 \mathrm{psi}
$$

Next calculate the pressure drop due to friction:
Find

$$
\frac{U}{R^{0.32}}=\frac{21.3}{(12)^{0.32}}=9.7
$$

From graph, line efficiency is equal to $86 \%$.
We put this efficiency in the Panhandle Equation (Equation (40)).

$$
Q=435.87 E\left(\frac{T_{0}}{P_{0}}\right)^{1.078}\left(\frac{P_{1}^{2}-P_{2}^{2}}{L}\right)^{0.5394}\left(\frac{1}{T}\right)^{0.5394}\left(\frac{1}{G}\right)^{0.4606}\left(\frac{1}{Z}\right)^{0.5} d^{2.6182}
$$

Solve for $\mathrm{P}_{2}$

$$
60 \times 10^{6}=435.87(0.86)\left(\frac{520}{14.65}\right)^{1.078}\left(\frac{1215^{2}-P_{2}^{2}}{L}\right)^{0.5394}\left(\frac{1}{530}\right)^{0.5394}\left(\frac{1}{0.65}\right)^{0.4606}\left(\frac{1}{0.8}\right)^{0.5} 8^{2.6182}
$$

$P_{2}=1020$
The total pressure drop is $18.3+195=213$ psi. This is probably okay for size but let us try a 10 in . diameter line. The superficial gas velocity is U .

$$
U=\frac{31194(60)(0.80)}{(10)^{2}(1100)}=13.6 \mathrm{ft} / \mathrm{sec}
$$

$F_{\text {e }}$ from chart $=0.18$

$$
\Delta P_{H}=\frac{44(0.18)(500)}{144}=27.5 \mathrm{psi}
$$

Note how this rises as diameter increases, the pressure drops for hills, increases as velocity is slowed down. Find pressure drop due to friction.

$$
\frac{U}{R^{0.32}}=\frac{13.6}{2.17}=6.25
$$

From the graph the line efficiency is equal to $77 \%$. Now put this efficiency into the. Panhandle Equation and solve for $\mathrm{P}_{2}$ :

$$
60 \times 10^{6}=435.87(0.77)\left(\frac{520}{14.65}\right)^{1.0781}\left(\frac{1215^{2}-P_{2}^{2}}{10}\right)^{0.5394}\left(\frac{1}{530}\right)^{0.5394}\left(\frac{1}{0.65}\right)^{0.4606}\left(\frac{1}{0.80}\right)^{0.5} 10^{2.6182}
$$

$$
P_{2}=1138 p s i
$$

The total pressure drop is $27.4+77=104$

Unless there was a method of continuing to keep the wellhead pressure up, it would probably be better to make the line 10" instead of 8 " - although 8 " would do.
This problem could also be solved by the Baker Method. The procedure is to find the type of flow, from the graph that correlates

$$
\frac{G}{\lambda} v s . \frac{L \lambda \Psi}{G}
$$

then find the value of $\theta_{G T T}$ for the type of flow. The pressure drop due to friction is then found from the formula:

$$
\Delta P_{\text {two phase }}=\phi_{G T T}^{2} \Delta P_{G}
$$

The elevation pressure drop is found as previously illustrated. This is shown below.
Solution using the Method of Baker (Modified by Kern)
First find $\lambda$

$$
\lambda=\left[\left(\frac{\rho_{G}}{0.075}\right)\left(\frac{\rho_{L}}{62.3}\right)\right]^{1 / 2}=\left[\left(\frac{7.10}{0.075}\right)\left(\frac{44}{62.3}\right)\right]^{1 / 2}=8.1
$$

Find G assuming a 10 " line

$$
\begin{aligned}
& \text { Gas Flow }(\mathrm{lb} / \mathrm{day})=\frac{60 \times 10^{2}}{384}(0.69)(29)=2.96 \times 10^{6} \mathrm{lb} / \mathrm{day} \\
& G=\frac{2.96 \times 10^{6}}{24\left(\frac{\pi}{4} \frac{10^{2}}{144}\right)}=226000 \frac{\mathrm{lb} / \mathrm{hr}}{\text { sq.ft. }} \\
& \frac{G}{\lambda}=\frac{226000}{8.1}=28000
\end{aligned}
$$

Must find $\Psi$ since $\frac{G}{\lambda}<80,000$, to find type of flow.

$$
\begin{aligned}
& \Psi=\frac{73}{\chi}\left[u_{L}\left(\frac{62.3}{\rho_{L}}\right)^{2}\right]^{1 / 3} \\
& \chi=22 \text { dynes } / \mathrm{cm} ; \quad u_{L}=0.5
\end{aligned}
$$

$$
\Psi=\frac{73}{22}\left[0.5\left(\frac{62.3}{44}\right)^{2}\right]^{1 / 3}=3.3
$$

Also find L

$$
L=\frac{12(60)(350)(0.7)(144)}{78.9(24)}=13200
$$

Find ordinate on Figure $6.14 \frac{L \lambda \psi}{G}$

$$
=\frac{13200}{226000}(8.1)(3.3)=1.56
$$

Type of flow from Figure 6.14 is annular. Find pressure drop for gas alone $\Delta \mathrm{P}_{100}$ (from GPSA Data Book).

$$
=0.2 \mathrm{psi} / 100 \mathrm{ft} .
$$

Use Figure 6.19 for finding $\Delta \mathrm{P}_{\text {two phase }}$
First find $X$

$$
x^{2}=\left(\frac{13200}{226000}\right)^{1.8}\left(\frac{7.10}{44}\right)(1.6)=(0.058)^{1.8}(0.16)(1.6)=0.00152
$$

From Figure 6.19

$$
\begin{aligned}
& \phi^{2}=\frac{\Delta P_{T P}}{\Delta P_{G}}=1.2 \quad \Delta P_{T P}=0.2(1.2)=0.24 \\
& \Delta P_{\text {two phase }}=0.24 \mathrm{psi} / 100 \text { foot of pipe }
\end{aligned}
$$

or read directly off of Figure 6.19.
Total drop exclusive of elevation change
$=0.24 \frac{5280}{100}(10)=127$ psi
which is relatively close to the Flanigan Method. i.e. total drop would be $27.4+127=154.4 \mathrm{psi}$.

### 6.6 Measurement of Fluids

Section 1 of the GPSA Data Book should be reviewed in connection with this section.

### 6.6.1 Units of Measurement

1. Gas - primarily as standard cubic feet per day at varying pressure, bases, but one temperature, $60^{\circ} \mathrm{F}$. The pressure bases are:
15.025 psia
14.900 psia
14.730 psia
14.650 psia
14.400 psia

In metric units it is generally $\mathrm{m}^{3} /$ day at $15^{\circ} \mathrm{C}$ and 101.325 kPa
Liquids - normally Barrels Per Day for crude oil.
For LPG's - Imperial or U.S. Gallons per day.
For gasoline or other finished products -thousands of Imperial Gallons per Day.
For plant process streams, pumps, discharge, etc. - U.S. gpm. In metric units generally $\mathrm{m}^{3} / \mathrm{hr}$ or $\mathrm{m}^{3} /$ day.

For accounting purposes, considerable interest is now being shown in mass measurement in lbs/hr or Kg/hr.
Steam - lbs/hr or Kg/hr.

### 6.6.2 Measuring Instruments

2. Orifice Meter Equations - The prime measuring instrument is the differential pressure meter, primarily the orifice plate. In this device a restriction is placed in the pipeline to induce a pressure drop as shown in Figure 6.22


Figure 6.22: Orifice Plate Representation
The pressure drop that occurs is shown in the graph below


Figure 6.23: Pressure Drop in Orifice Plate
The general equation for an orifice meter is:

$$
W=C_{0} A_{0} \sqrt{\frac{2 g_{c} \rho(\Delta P)}{1-\left(\frac{A_{0}}{A_{1}}\right)^{2}}}
$$

where:

$$
\begin{aligned}
& C_{o}=\text { constant } \approx 0.62 \\
& A_{o}=\text { area of orifice opening } \\
& \rho=\text { density of fluid } \\
& \mathrm{gc}=\text { force of gravity } \\
& \Delta \mathrm{P}=\text { pressure drop } \\
& \mathrm{A}_{1}=\text { area of pipe } \\
& \mathrm{W}=\text { mass flow }
\end{aligned}
$$

This general equation has been changed into the following specific equation for gas by the American Gas Association in their report No. 3 reference. (Now ANSI/API 2500)

$$
Q=C \sqrt{h_{w} P_{f}}
$$

where:
Q = rate of flow in cu.ft./hr at the base conditions
$\mathrm{h}_{\mathrm{w}}=$ measured pressure drop in inches of water
$P_{f}=$ static pressure in psia (upstream value)
C = constant determined from the following data, all of which are available in the GPSA Data Book or AGA Report No. 3

$$
=\left(F_{B}\right)\left(F_{P B}\right)\left(F_{T B}\right)(Y)\left(F_{\mathrm{tf}}\right)\left(F_{\mathrm{pv}}\right)\left(F_{\mathrm{R}}\right)\left(F_{\mathrm{g}}\right)\left(\mathrm{F}_{\mathrm{L}}\right)
$$

These are:
$F_{B}=$ Basic orifice factor which depends on where the differential pressure is measured and the ratios of orifice diameter to pipe diameter ( $\beta$ ratio).
$\mathrm{F}_{\mathrm{PB}}=$ Pressure base factor
$\mathrm{F}_{\mathrm{TB}}=$ Temperature base factor
Y = Expansion factor
$F_{g}=$ Gravity of the gas
$\mathrm{F}_{\mathrm{tf}}=$ Flowing temperature correction
$\mathrm{F}_{\mathrm{pv}}=$ Super compressibility factor $=\frac{1}{\sqrt{Z}}$. The sour gas correction as developed by Wichert and Aziz as given in chapter 2, should be included in this factor if sour gas is being measured.
$F_{R}=$ The Reynolds number factor
$F_{L}=$ Correction for location other than $45^{\circ}$ Latitude
For steam, the same equation, i.e. (58) is used by a different set of factors make up the constant C'. (See page 1-11 in the GPSA Data Book.)
For liquids, the static pressure is not a factor and the equation is
Equation 6-59

$$
Q_{h}=C^{\prime} \sqrt{h_{w}}
$$

where:
$\mathrm{Q}_{\mathrm{h}}=$ flow, US gallons per hour
$C^{\prime}=$ the orifice constant determined from a set of factors for liquids as given in the GPSA Data Book.

### 6.6.3 Two Phase Flow Measurement

E. Wichert of Canadian Fina has developed a reasonably accurate method. This method consists of measuring the two phase flow with a standard orifice using the gas properties and the measured differential, then correcting the measuring flow by means of the equation below:

Equation 6-60

$$
Q_{T W E}=Q_{M P}\left(\frac{1+R_{H L} E}{1+R_{T L} S}\right)
$$

where:
$Q_{\text {TWE }}=$ Total hydrocarbon well effluent MMSCFD
$Q_{M P}=$ The rate of flow obtained by using the properties of the gas phase with the multiphase meter readings for flow calculations.
$\mathrm{R}_{H}{ }^{\mathrm{L}}=$ liquid to gas ratio BBIs/MMSCF
$E=$ equivalent volume of liquid as a vapour at standard conditions MMSCF/BBI
$R_{T L}=R_{H L}+R_{W}$
$R_{w}=$ water/gas ratio BBIs/MMSCF
$S=$ function of gas molar density (from Figure 6.24) at above $700 \mathrm{psia} S=0.0024 \rho^{2}$


Figure 6.24: Function of Gas Molar Density

## Orifice Meter Installations

The installation of orifices requires special care, particularly the presence of a close course of turbulence upstream has to be avoided. Some typical meter run installations are given in the GPSA Data Book (Page 1-8). These give the upstream and downstream requirements of straight pipe.

The measuring accuracy of an orifice meter is considered to be about $2 \%$. Some companies claim $1 \%$ with extra long runs, no turbulent sections upstream, etc.

## Venturi Meters

These operate on the same principle as an orifice (a differential pressure). However, the loss of pressure in the meter is much less. The coefficient of discharge is 0.92 to 0.98 compared to 0.62 with an orifice. As we know, it has a smoothly contoured throat rather than a sharp edge.


Figure 6.25: Venturi Meter
The Venturi is used primarily in large water lines, not gas lines. Use the general equation given previously with $\mathrm{C}_{\mathrm{o}}-.92$ to .98 , .98 above 100,000 Re.

## Flow Tube



Figure 6.26: Flow Tube
This is smaller than Venturi, measures small differences in pressure. It is sometimes used in large gas lines.

## Area Meters

These are taper tubes with plugs in some. The pressure drop remains the same but area is allowed to vary by the motion of the meter.

## Volume Meters

For low pressure, volume meters, such as the wet test meter, are used. The meter, half filled with liquid, has rotating blades which measure flow.

## Turbine Meters

In this velocity of rotation is proportional to flow rate. API Standard 2534 covers turbine meters.

## Liquid Meters

All the above referred to meters can be and are used for liquids. However, often positive displacement meters such as rotating lobes, wobbling discs, pistons, etc., are used for measuring liquids, particularly for finished products.

Both turbine and positive displacement liquid meters require periodic prooving to check counter registration versus gross volume. There are several types of liquid meter provers. These are discussed in the GPSA Data Book. Another instrument that is coming into prominence is the vortex meter which measures the number of vortices produced.

There is now a move to mass flow measurement. This is discussed on Pages 1-12 and 1-13 of the GPSA Metric Data Book.

A very good summary of measurement calculation is shown on Fig. 3-2 and Fig. 3-3 on the new English GPSA Data Book which are reproduced here.


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| :---: | :---: | :---: | :---: | :---: | :---: |

### 6.7 MOVING OF FLUIDS

The two main pieces of fluid moving equipment are pumps and compressors. We are not going to touch on all various types of pumps, such as centrifugal, turbine, reciprocating, gear, etc., or discuss the advantages or disadvantages of reciprocating or centrifugal compressors, or discuss the type of compressor to use. However, we would like to review some of the problems in selecting the proper pieces of equipment to do the job.

### 6.7.1 Specification of Pumps

There are several process items to be selected by an engineer specifying a pump.
These are:

1. Fluid being pumped.
2. Specific gravity of fluid at its operating temperature and $60^{\circ} \mathrm{F}$.
3. Viscosity at operating temperature.
4. Operating temperature.
5. Capacity (use about $10 \%$ above process flow sheet for ordinary services and $25 \%$ for reflux services).
6. Head.
7. Net positive suction head available (NPSH).

The first five are obtained from flow diagrams or physical property tables. This leaves three classifications.

## Capacity

For the capacity an allowance of $10 \%$ above material balance figures should be used.

## Head

For determining the head, first make a sketch of the system as shown in the sketch accompanying the example problem. To find the pump head required, list pressure drop pump has to overcome, i.e.

1. Terminal pressure in tower - from process flow sheet.
2. Pressure drop in discharge piping - calculate.
3. Heat exchange pressure drop - 10 psi (normally, or actual value, if available).
4. Control valve \& controller pressure - 10 psi (or take about $1 / 3$ of total available system drop).
5. Determine the difference in elevation.
6. Add $5 \%$ over plus. This gives the head required.

## NPSH

This determines whether a pump will cavitate or not.
The NPSH is found from the formula:
$N P S H=P_{1}-V P+H_{1}-H_{2}-F$
where:
$P_{1}=$ actual pressure in suction drum
VP = vapour pressure of liquid being pumped
$\mathrm{H}_{1}=$ minimum level in suction tank
$\mathrm{H}_{2}=$ height of impeller eye above grade
$\mathrm{F}=$ friction loss in the suction line to the pump in feet
The reason that NPSH is so important is that it is a measure of cavitation or vapourization possibilities in a pump. Cavitation causes pits, etc. in pump impeller.
Refer to the article by A.H. Younger and J.L. Reuter, for further discussion on the calculation of heads and NPSH.

An example problem will illustrate this sizing of pumps.

## Example Problem 6.3

Calculate the head and NPSH required for pumping 60 US gpm of mixed butanes from a feed tank that operates at 50 psig and $80^{\circ} \mathrm{F}$ into a fractionating tower that operates at 200 psig . The following sketch illustrates the system.


Figure 6.27: Mixed Butanes from a Feed Tank

| Head Calculations | Head in Feet $\mathbf{1} \mathbf{~ p s i}=\mathbf{4}$ ' for $\mathbf{C}_{4}$ |
| :--- | :---: |
| Terminal Pressure (200 psig) |  |
| Suction Pressure (50 psig) |  |
| Net Pressure Difference (150 psi) | 600 |
| Elevation Difference (50 - 2) | 48 |
| Control Valve (10 psi) | 40 |
| Heat Exchangers (.10 psi ea.) | 80 |


| Piping (400 equivalent feet) |  | 48 |
| :--- | :--- | :---: |
| Sub Total | 816 |  |
| Add 5\% for safety factor |  | 42 |
|  | Total | 858 |

NPSH Calculations
Use formula NPSH $\left.=(\mathrm{Pi}-\mathrm{VP})+\mathrm{H}_{1}-\mathrm{H}_{2}-\mathrm{F}\right)$

| Feet |
| :--- |
| 200 |
| 200 |
| 6 |
| 2 |
| 1 |
| 3 |

### 6.7.2 Compressor Specifying

In this case it is necessary to specify the following:
3. Gas to be compressed and its properties, i.e., mole weight and ratio of specific heat.

$$
\frac{C_{P}}{C_{V}}=K
$$

Gas temperature at suction end of compressor.
Gas pressure at suction end of compressor.
Flow in SCFM or SCFD, etc. use process flow sheet flow plus $5 \%$ to $10 \%$.
Discharge pressure. Calculate in the same manner as for pumps. Specify discharge pressure with the following additional margin:

|  | Comp. Patio |
| :--- | :---: | Pressure Drop

See example problem 1 in Section 10.

### 6.8 Example Problems

## Example Problem 6.4

You are to size the pipeline to carry waste water fran a settling basin in a plant to a river. The design flow rate is 200 US gpm and the profile and length of line is as follows:


Note: Make the line the same size throughout.

## Example Problem 6.5

You are to size a gathering system for the field shown in the sketch below. The plant is to receive the gas at a minimum pressure of 600 psia. The gas gravity is 0.65 . The well deliverability pressure is 705 psia.
$1 X$

## SCALE $1^{\prime \prime}=1$ mile

$X^{4} \quad x$ Wells
P Plant
$2 x$
$x$
3
The wells have the following deliverability.

|  | MMSCFD |
| :--- | :---: |
| \#1 | 8 |
| \#2 | 15 |
| \#3 | 20 |
| \#4 | 12 |
| \#5 | 30 |

The cost of installation of a pipeline is $\$ 6000 /$ inch diameter mile.
Calculate the cost of your gathering system and show it on a sketch.
Assume that the reservoir has a water drive and the deliverability pressure will never decrease.

## Example Problem 6.6

A large gas gathering line is pigged every day. This line goes through a river valley 1000 feet deep. Approximately how much greater is the pressure at the upstream side of the pig when the pig is in
the bottom of the valley as compared to the pressure at the top of the valley on the downstream side of the valley? The line size is 20 ( 19.250 " ID) and the flow is 140 MMSCFD. The gas contains 30 BBIs per MMSCFD of liquid. The operating pressure is 1100 psig and the operating temperature is $70^{\circ} \mathrm{F}$. The gas gravity is 0.70 and the liquid's density is $45 \mathrm{lbs} / \mathrm{cu} . \mathrm{ft}$.

## Example Problem 6.7

Determine the line size for a gas gathering line delivering gas to a heater located as shown in the sketch.

Well


Length of line from well to dehydration is 1 mile. The best line is one with the lowest pressure drop. The gas flow is 15 MMSCFD. At the wellhead pressure is 800 psi. It contains liquid of 50 BBIs/MMSCF with a density of 40 lbs per cubic foot. The gas gravity is 0.7 and the $Z$ factor is 0.9 . Data on pressure drop for various line sizes are shown in the following table. Make your choices from these line sizes.

| Size | $\mathbf{\Delta P}$ Gas Only psi | $\mathbf{\Delta P}$ Liquid Only psi |
| :---: | :---: | :---: |
| $8^{\prime \prime}$ | 10 | 1 |
| $6 "$ | 20 | 1.5 |
| $4 "$ | 60 | 4 |
| $3^{\prime \prime}$ | 140 | 8 |

## Example Problem 6.8

You are to specify the head required for pumping propane from storage bullets that operate in a plant in which the local temperature goes down to $-20^{\circ} \mathrm{F}$ through a 8 " pipeline approximately 12 miles long and into a salt storage cavern that has brine specific gravity 1.2 as the means that holds pressure in the cavern. The cavern is 2000 feet deep. Also in the 12 mile pipeline there is a section of 6 " pipe that is used to cross a lake. It is 2 miles long.
Note: Express your answer in feet of head.
Also estimate the NPSH required for the pump if the pump suction is at 2 ft . above grade and the minimum liquid tank level is 10 ft . The suction line is only 20 ft long and is 12 inches in size. The flow in the lines is to be 40,000 BPD.

## Example Problem 6.9

Propane is kept in a refrigerated storage vessel at $+20^{\circ} \mathrm{F}$ which has 120,000 BBls capacity. It is being pumped out of this vessel into a pipeline at a rate of 200,000 BPD. The pipeline pump station is one mile farther down the line from the injection point. The pump station suction pressure is to be 25 psia above the vapour pressure of the propane at the maximum pipeline temperature.
A vapourizer is put in to keep the pressure on the when pumping is in progress.
a) Determine the heat duty required by the vapourizer.
b) Determine head and capacity of the propane pump in and US gpm.

The sketch below shows the proposed system.


- The maximum temperature in the pipeline at any time is $65^{\circ} \mathrm{F}$.
- Assume pure propane for your calculations.
- Assume a 5 psi pressure drop across the FRC valve and orifice meter in propane injection line.
- Assume that the 100,000 barrels is moved at one time.


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### 7.0 Mass Transfer

- The principles of mass transfer and a review of unit operations based on mass transfer, distillation, absorption and adsorption


### 7.1 Introduction

### 7.1.1 What is a Mass Transfer?

It is the movement of one or more compounds between phases. We are primarily interested in transfer between liquid and gas but we do encounter in natural gas processing the transfer of mass between two liquid phases which are immiscible. You can, of course, have mass transfer between miscible phases, particularly when there is a permeable or semipermeable membrane, i.e. gas diffusion, osmosis, etc. Also if there is no membrane present we have a form of mass transfer in thermal diffusion.

### 7.1.2 Types of Processes Considered

Mass transfer operations we wish to consider are:

- Gas - Liquid
> Distillation of Fractionation
> Absorption
> Stripping
- Liquid-Liquid
> Liquid-Liquid Extraction
- Gas - Solid
> Adsorption
$>$ Desorption


### 7.1.3 Primary Concepts

There are three primary concepts in mass transfer. These are:

1. Stages and the Ideal Stages
2. Continuous Transfer
3. Batch Transfer

## Stages and the Ideal Stages

If two insoluble phases come together so that the various components can distribute themselves between the phases and the phases are mechanically separated, then this operation is called a stage. If enough time is allowed for complete equilibrium to occur such that additional time will not change the composition, then an ideal stage has been reached.

Let us consider a distillation tray as shown.


Figure 7.1: Distillation Tray
Let us consider the equilibrium relationships around this tray. The liquid leaving tray n is in equilibrium with the vapour leaving it. Thus, if we have a component such as $\mathrm{C}_{3}$ we can write the equation for tray n :

Equation 7-1

$$
Y_{C_{3}}=K x_{C_{3}}
$$

where:
$Y_{C_{3}}=$ mole fraction of $\mathrm{C}_{3}$ in vapour.
$x_{C_{3}}=$ mole fraction of $\mathrm{C}_{3}$ in liquid.
$\mathrm{K}=$ equilibrium constant.
If we know the temperature and pressure on the tray we can calculate the composition of one phase if we know the other. We also have a mass balance and generally a molar balance as follows:

Equation 7-2

$$
L_{n+1}+V_{n-1}=V_{n}+L_{n}
$$

where:
$L_{n}=$ Moles of liquid from tray $n$.
$V_{n}=$ Moles of vapour from tray $n$.
$V_{n-1}=$ Moles of vapour to tray $n$.
$\mathrm{L}_{\mathrm{n}+1}=$ Moles of liquid to tray n .
In the ideal stage concept the rate of mass transfer is only considered by the approach to equilibrium that the actual stage obtains as compared to that theorectically possible. This is normally expressed as efficiency.
We also have stages in such apparatus as leaching tanks, etc., in the mining industry.

## Continuous Transfer

This occurs in packed towers, etc. Rate Equation - the general rate equation of:

$$
\text { Rate }=\frac{\text { Driving Force }}{\text { Resis } \tan c e}
$$

In general the driving forces are concentration differences while the resistances are normally film thicknesses. A difference of concentration exists only when a system is not at equilibrium. For example, consider a system of ammonia and water, i.e. pure ammonia and pure water brought together. Since ammonia dissolves in water, there is a driving force of a difference in concentration between the ammonia in the vapour and in the water. This is a very quick action.


Figure 7.2: Mass Transfer System
Let us also consider a slow action, that of water in a pan outside on a dry day. Water evaporates because there is a driving force from pure water to the amount of water that the air can hold. This is, again, mass transfer.

## Batch Transfer

In both previously discussed cases we have a continuous process in which the transfer is from the main bulk of one fluid through the interphase between the two fluids to the main bulk of the other fluid. In adsorption we have a slightly different case. The components are transferred from the main fluid to the surface of the other fluid, not to the main body.
The process continues until surface is saturated and then break-through occurs, i.e. concentration difference between passing gas and surface no longer great enough for transfer to completely take place.

### 7.2 Types of Diffusion

Two types of diffusion from one phase to the other are:

### 7.2.1 Molecular Diffusion

This is movement from one phase to the other or, in a single phase, by means of the molecules' thermal energy, i.e. have a beaker of water and add ink slowly or the evaporation of water in air.

### 7.2.2 Eddy Diffusion

By means of agitation you can increase diffusion rate extensively, i.e. stir beaker above, equilibrium comes much quicker. Of course, within each eddy, uniformity of concentration is achieved by molecular diffusion which is the ultimate process. One can see, therefore, that molecular diffusion is the mechanism of mass transfer in stagnant fluids, or in fluids that are moving in laminar motion although it is, nevertheless, always present in highly developed turbulent flow.

### 7.3 Rate of Diffusion

We have seen from the simple demonstration that as long as there is non-uniformity (of concentration) in a given solution, the solution is spontaneously brought to uniformity by diffusion, the solute molecules moving from a place of high concentration to one of low concentration. The rate at which the solute molecules move at any point, in any direction, must, therefore, depend on the concentration gradient at that point. This rate can be conveniently described in terms of a molar flux or:

```
moles/(time) (area)
```

the area being measured in a direction normal to the diffusion. For non-reacting systems of two components $A$ and $B$, the molar fluxes of $A$ and $B$ are described by Fick's Law of Diffusion, which may be written for steady one dimensional transfer as:

Equation 7-3

$$
J_{A}=-D_{A B} \frac{d C_{A}}{d Z}
$$

Equation 7-4

$$
J_{B}=-D_{B A} \frac{d C_{B}}{d Z}
$$

where:
$J_{A}$ and $J_{B}=$ molar fluxes of $A$ and $B$ relative to the molar average velocity of the mixture.
$Z=$ distance in the direction of diffusion
$C_{A} \& C_{B}=$ molar concentrations of $A$ and $B$
$D_{A B}$ and $D_{B A}=$ molecular diffusivities of $A$ in $B$ and $B$ in $A$ respectively.
Now for a perfect gas:

$$
C_{A}=\frac{P_{A}}{R T} \quad \text { and } \quad C_{B}=\frac{P_{B}}{R T}
$$

where:

$$
P_{A} \text { and } P_{B}=\text { partial pressures of } A \text { and } B
$$

$R=$ gas constant
$\mathrm{T}=$ absolute temperature
So that equations (3) and (4) become
Equation 7-5

$$
J_{A}=-\frac{D_{A B}}{R T} \frac{d P_{A}}{d Z}
$$

Equation 7-6

$$
J_{B}=-\frac{D_{B A}}{R T} \frac{d P_{B}}{d Z}
$$

where:
$J=$ flux relative to average mole velocity of mixture.
The negative sign in equations (3) to (6) emphasizes that diffusion occurs in the direction of a drop in concentration. Molecular diffusivity ( $D_{A B}$ or $D_{B A}$ ) is a characteristic of a constituent and its environment (i.e. temperature, pressure, concentration, state of aggregation, etc.). The kinetic theory yields several theoretical expressions of the following form, for the binary gas systems.
The following equation is recommended for estimating diffusion coefficients in binary gas systems at pressures less than 500 psia:

Equation 7-7

$$
D_{1,2}=\frac{0.04381 T^{1.5}\left(\frac{1}{M_{1}}+\frac{1}{M_{2}}\right)^{0.5}}{p\left(\sigma_{1,2}\right)^{2} \Omega_{D}}
$$

where:
$D_{1,2}=$ diffusion coefficient of component 1 in component 2 in square feet per hour.
T = temperature, in degress Rankine.
$M_{1}, M_{2}=$ molecular weights of components 1 and 2 , respectively.
$p=$ pressure, in pounds per square inch absolute.
$\sigma_{1,2}=$ arithmetic average of the collision diameters for 1,2 components 1 and 2, in angstrom units.
$\Omega_{D}=$ collision integral for diffusion.

## Procedure to find "D"

1. Obtain the Lennard-Jones force constants $(\varepsilon / k$ and $\sigma$ ) for both components of the mixture from the Table in API data book.

If the compounds of interest are not listed, use equations 8 and 9 in the API data book with the critical temperature and volume listed in Chapter 1 and the critical compressibility factor in Chapter 2 of the API data book:
$\frac{\varepsilon}{k}=65.3 T_{C} Z_{C}{ }^{3.6}$
where:
$\varepsilon / \mathrm{k}=$ Lennard-Jones potential parameter, in degrees Rankine.
$\mathrm{k}=$ Boltzmann constant.
$\mathrm{T}_{\mathrm{c}}=$ critical temperature, in degrees Rankine.
$Z_{c}=$ critical compressibility factor.
Equation 7-9

$$
\sigma=0.7402 \frac{\left(M V_{C}\right)^{0.333}}{z_{C}^{1.2}}
$$

where:
$\sigma=$ Lennard-Jones collision diameter, in angstrom units.
$\mathrm{M}=$ molecular weight.
$V_{c}=$ critical volume, in cubic feet per pound. c
2. Calculate the Lennard-Jones force constants for the mixture with equations (10) and (11):
$\sigma_{1,2}=\frac{1}{2}\left(\sigma_{1}+\sigma_{2}\right)$
where:
subscripts 1 and 2 refer to the components and 1,2 refer to the mixture.
Equation 7-11
$\frac{\varepsilon_{1,2}}{k}=\left[\left(\frac{\varepsilon_{1}}{k}\right)\left(\frac{\varepsilon_{2}}{k}\right)\right]^{0.5}$
3. Calculate the dimensionless group, $k T / \varepsilon_{1,2}$ using the $\varepsilon_{1,2} / k$ result from equation 11 and the temperature of interest in degrees Rankine. Using this value, interpolate the collision integral, $\Omega_{D}$ from Table in API data book.
4. Calculate the diffusion coefficient using equation (7).

Note: The following equation is recommended for estimating diffusion coefficients in dilute liquid binary solutions. The equation may be used directly or approximated conveniently with a nomograph, Fig. 13A1.2 in the API data book.
$D_{1,2}=\frac{1.59 \times 10^{-7}\left(\Psi_{2} M_{2}\right)^{0.5 T}}{\mu\left(\frac{M_{1}}{\rho_{1}}\right)^{0.6}}$
where:
$D_{1,2}=$ diffusion coefficient of solute (component 1 ) in solvent (component 2 ), in square feet per hour
$\Psi_{2}=$ association parameter for the solvent
$\mathrm{M}_{2}=$ molecular weight of the solvent
$M_{1}=$ molecular weight of the solute
$\mathrm{T}=$ temperature, in degrees Rankine
$\mu=$ viscosity of the solution, in centipoises
$\rho_{1}=$ saturated liquid density of the solute at the normal boiling point, in grams per milliliter

## Procedure

1. Obtain $M_{1}$ and $M_{2}$ from Chap. 1, and obtain $\rho_{1}$ using the methods or figures in Chap. 6. In the absence of experimental data, estimate $\mu$ using chap. 11 procedures. (All chapters refer to API Data Book).
2. Determine the association parameter for the solvent, $\Psi_{2}=1$. For other associated solvents not listed in the following table, estimate a value between 1.0 and 2.6 based on the relative associative tendency of the solvent:

| Solvent | $\boldsymbol{\Psi}_{\mathbf{2}}$ |
| :--- | :---: |
| Nonassociated solvents | 1.0 |
| Ethyl alcohol | 1.5 |
| Methyl alcohol | 1.9 |
| Water | 2.6 |

3. Obtain $D_{1,2}$ directly from equation 12 or with the nomograph, Fig. 13A1.2 in the API data book.

Going back to equations (5) and (6), we can consider first the general case in which a steady bulk flow is imposed upon the fluid mixture in the direction in which component $A$ is diffusing. The magnitude of this molar flux of the mixture relative to stationary coordinates will be:

$$
N_{A}+N_{B}
$$

The flux of components $A$ and $B$ relative to stationary coordinates are now the resultant of two quantities (vectors):

1. The flux caused by the bulk flow.
2. The flux caused by molecular diffusion.

Whereas these vectors are in the same direction for component $A$, they are clearly in the opposite direction for component $B$. The total flux of A relative to stationary coordinates, then, is the sum of that resulting from the bulk flow and that due to molecular diffusion (i.e. for a gaseous mixture).

$$
N_{A}=\left(N_{A}+N_{B}\right) \frac{P_{A}}{P}-\frac{D_{A B}}{R T} \frac{d P_{A}}{d Z}
$$

Two special cases of molecular diffusion are customarily considered:

1. Equimolal Counterdiffusion.
2. Unimolal Unidirectional Diffusion.

In the case of equimolal counter diffusion (process often approximated in the distillation of binary systems) the total molal flux with respect to stationary coordinates is zero ( A and B diffusing in the opposite direction and at the same molal rate) so that:

$$
N_{A}=-N_{B}
$$

then from equations (5), (6) and (7)
Equation 7-14

$$
N_{A}=J_{A}=-N_{B}=-J_{B}
$$

but $P_{A}+P_{B}=P=$ constant
therefore
Equation 7-15

$$
\frac{d P_{A}}{d Z}=-\frac{d P_{B}}{d Z}
$$

and from equations (5), (6) and (14)

$$
D_{A B}=D_{B A}=D
$$

At steady state $N_{A}$ and $N_{B}$ are constants, so that equations (5), (16) and (13) may be combined and integrated for constant $D$ to give:

$$
N_{A}=\frac{D}{R T Z}\left(P_{A_{1}}-P_{A_{2}}\right)
$$

(steady stage equimolal counterdiffusion)
also for liquids:

$$
N_{A}=\frac{D_{A B}}{Z}\left(C_{A_{1}}-C_{A_{2}}\right)
$$

where:

$$
\mathrm{Z}=\mathrm{Z}_{1}-\mathrm{Z}_{2}
$$

$P_{A_{1}}$ and $P_{A_{2}}=$ partial pressures of A at $\mathrm{Z}_{1}$ and $\mathrm{Z}_{2}$ respectively.
$C_{A_{1}}$ and $C_{A_{2}}$ are in concentration at $\mathrm{Z}_{1}$ and $\mathrm{Z}_{2}$.
For the case of steady state unimolal, unidirectional diffusion in gases, the flux of component $B$ in one direction, because of the bulk flow, is equal to the flux of $B$ in the opposite direction because of the molecular diffusion. Component B is therefore motionless in relation to stationary coordinates and $N_{B}=0$. In such as case:

Equation 7-18

$$
N_{A}=\frac{D P}{R T Z} \ln \left(\frac{P_{B_{2}}}{P_{B_{1}}}\right)
$$

which may be written as:
Equation 7-19

$$
N_{A}=\frac{D P}{R T Z}\left(\frac{P_{B_{2}}-P_{B_{1}}}{P_{B} \log \text { mean }}\right)
$$

or

$$
N_{A}=\frac{D}{R T Z}\left(\frac{P}{P_{B} \log \text { mean }}\right)\left(P_{A_{1}}-P_{A_{2}}\right)
$$

(unimolal, unidirectional diffusion)
where

$$
P_{B} \log \text { mean }=\frac{P_{B_{2}}-P_{B_{1}}}{\ln \frac{P_{B_{2}}}{P_{B_{1}}}}
$$

### 7.4 Mass Transfer Coefficients

Consider the distribution of a solute (A) between two immiscible phases in contact with each other, as represented by the figure below:


Figure 7.3: Mass Transfer Curve
The first phase may be gaseous and the second phase liquid. $\mathrm{Y}_{\mathrm{A}}$ will then denote the composition of the gas phase and $X_{A}$ the composition of the liquid phase.
A point on the equilibrium curve gives the equilibrium compositions of the two phases. A point located above the curve indicates that component $A$ is being transferred from the gas to the liquid and a point below the curve indicates that component $A$ is being transferred from the liquid to the gas.

It is assumed that local equilibrium prevails at the interface where the compositions are $Y_{A}^{*}$ and $X_{A}^{*}$. If transfer takes place from the gas to the liquid, the individual mass transfer coefficients $\mathrm{k}_{\mathrm{g}}$ and $\mathrm{k}_{\mathrm{L}}$, for the gas and liquid phases respectively, can be defined as follows:

$$
N_{A}=k_{g}\left(Y_{A}-Y_{A}^{*}\right)
$$

where

$$
k_{g}=\frac{D_{A B}}{R T Z}
$$

Equation 7-23

$$
N_{A}=k_{L}\left(X_{A}^{*}-X_{A}\right)
$$

where

$$
k_{L}=\frac{D_{A B}}{Z}
$$

where:
$Y_{A}$ and $X_{A}$ are the concentrations of component $A$ in the bulk of gas and liquid phases.

Let us consider what happens in the above transfer as shown in Figures 7.4 and 7.5. Equations (21) and (23) show that

$$
\frac{Y_{A}-Y_{A}^{*}}{X_{A}-X_{A}^{*}}=-\frac{k_{L}}{k_{g}}
$$

Interfacial concentrations $X_{A}^{*}$ and $Y_{A}^{*}$ are often unknown and frequently impossible to determine at a given location at the interface and it is then more convenient to use overall coefficients $\mathrm{K}_{\mathrm{g}}$ and $\mathrm{K}_{\mathrm{L}}$, defined in terms of overall concentration differences as shown below:

Equation 7-26

$$
N_{A}=K_{g}\left(Y_{A}-Y_{A L}\right)
$$

$$
N_{A}=K_{L}\left(X_{A G}-X_{A}\right)
$$

The locations of $Y_{A L}$ and $X_{A G}$ are shown in the figures. There are respectively $Y_{A L}$ the equivalent of $X_{A}$ in terms of $Y$ and $X_{A G}$ the equivalent of $Y_{A}$ in terms of $X$.


Figure 7.4: Mass Transfer Across Film


Conc. A in Liquid
Figure 7.5: Mass Transfer Curve
The relationships between the individual coefficients of equations (21) and (23) and the overall coefficients of equations (26) and (27) are shown in the following equations:

Equation 7-28

$$
\frac{1}{K_{g}}=\frac{1}{k_{g}}+\frac{m}{k_{L}}
$$

$$
\frac{1}{K_{L}}=\frac{1}{k_{L}}+\frac{1}{m k_{g}}
$$

and

$$
\frac{1}{K_{g}}=\frac{1}{m K_{L}}
$$

where:
$\mathrm{m}=$ the slope of the equilibrium curve.
when:
$\frac{1}{k_{g}}=\frac{m}{k_{L}}$ gas phase is controlling
when:

$$
\frac{1}{k_{L}}=\frac{1}{m k_{g}} \text { liquid phase is controlling }
$$

The total interfacial area (A) for mass transfer in a column is usually not known and in such cases mass transfer rates are frequently based on unit volume of the equipment instead of the unit interfacial area. The rate equations are then modified to the following form:

$$
N_{A} A=k_{g} a\left(Y_{A}-Y_{A}^{*}\right) V_{0}=k_{L} a\left(X_{A}^{*}-X_{A}\right) V_{0}=K_{g} a\left(Y_{A G}-Y_{A L}\right) V_{0}=K_{L} a\left(X_{A G}-X_{A L}\right) V_{0}
$$

where:
$\mathrm{V}_{\mathrm{O}}=$ the volume of the tower
a = interfacial area per unit volume (assumed value)

### 7.5 Review of Processes Depending on Ideal Stages

Now let's consider three mass transfer operations that depend primarilty for analysis on the ideal stages.

### 7.5.1 Distillation

In this process different compounds are separated by the application of heat to transfer the more volatile components from the liquid to the gas. A continuing process of vapourization and condensation takes place in distillation until relatively pure top and bottom products are obtained.
The difficulty in separation can be roughly measured by the difference in boiling points of compounds at atmospheric pressure, i.e.

Table 7.1: Boiling Points for Light Hydrocarbons

| propane | $-43.7^{\circ} \mathrm{F}$ | $\left(-42^{\circ} \mathrm{C}\right)$ |
| :--- | :--- | :--- |
| isobutane | $+10^{\circ} \mathrm{F}$ | $\left(-12.2^{\circ} \mathrm{C}\right)$ |
| n butane | $31.1^{\circ} \mathrm{F}$ | $\left(-0.5^{\circ} \mathrm{C}\right)$ |
| isopentane | $82.1^{\circ} \mathrm{F}$ | $\left(27.8^{\circ} \mathrm{C}\right)$ |
| n pentane | $96.9^{\circ} \mathrm{F}$ | $\left(36.0^{\circ} \mathrm{C}\right)$ |
| n hexane | $155.7^{\circ} \mathrm{F}$ | $\left(68.6^{\circ} \mathrm{C}\right)$ |

This shows that the separation between $\mathrm{C}_{3}$ and $\mathrm{iC}_{4}$ is easier than between $\mathrm{iC}_{5}$ and $\mathrm{nC}_{5}$. A more accurate measure of the difficulty of separation is the relative volatility which is expressed as $\alpha$

Equation 7-32

$$
\alpha=\frac{K_{l}}{K_{n}}
$$

where:
$K_{\ell}=$ equilibrium constant of the light key component and K
$\mathrm{K}_{\mathrm{n}}=$ equilibrium constant for the heavy key component concerned in the separation, both at the same temperature and pressure.
The key components in multicomponent separation are those components that are being separated. The components appear in both the top and bottom of a column, the light key appears mostly in the top and slightly in the bottom, i.e. it is the lightest component in the bottom. The converse is true of the heavy key. It appears primarily in the bottom and is the heaviest component in the top.

### 7.5.2 Absorption

In this operation a soluble component in the gas phase is dissolved in the liquid phase. This is done by either physical absorption or by chemical reaction.

### 7.5.3 Stripping

This is the opposite of absorption. That is, it is the removal by the application of heating or by the application of a lean gas of the soluble liquid components. It is actually distillation when heat is applied to generate the stripping medium.

### 7.5.4 Terms Used

Let's review some terms involved in distillation, absorption and stripping.


Figure 7.6: Typical Distillation System

### 7.6 Equipment

Let us now consider the type of equipment used for these operations. Primarily these operations are conducted in tall towers filled with trays or plates or packing. The oil industry relies more on trays rather than packing for large diameter towers and packing for small diameter towers (24" or less) $[60 \mathrm{~cm}$ or less]. The chemical industry uses packed towers of much greater diameter. Packed towers are coming more into use in the oil industry.

### 7.6.1 Tray Types

Let us consider the operation of a tray in a tower.


Figure 7.7: Flow Across a Tray
The object of the tray is to make sure liquid and gas come in intimate contact and have the opportunity to reach as close as possible to equilibrium. The prime example of obtaining this contact is with the bubble cap.

Liquid


Figure 7.8: Bubble Cap Tray
Another common tray is the valve tray


Figure 7.9: Valve Tray
Sieve trays are a series of perforated holes in which both gas and liquid can pass through or just have the gas going up and the liquid going down a downcomer as in the previous type of trays.


Figure 7.10: Sieve Tray
There are also such trays as turbo girds which are similar to sieves; side to side pans; disc and doughnut trays; uniflux trays; ripple trays; Linde trays. The chief object is to get good contact. The operation of various types of contacting devices on trays and the limits on tray operation are shown on Page 21a which are reproduced from the new English GPSA Data Book.

### 7.6.2 Tray Selection

Type of tray depends on service. The sieve tray normally has the greatest capacity with least flexibility in service. The operating range is limited because of weeping. Also there can be serious problems in corrosive or fouling services. The floating valve cap tray has the next greatest capacity and a wider range of operation. It can be designed so that it cannot shut in fouling service.

The bubble cap tray is the old standby but is being replaced with other higher capacity trays. It is still quite widely used, however. A summary of trays used in gas processing is as follows:

MEA, DEA and other sweetening solvents
All new towers, valve trays. *
Condensate Stabilization
All new towers, valve trays
LPG Fract.

Sieves quite often

* Sieve trays used for hot pot in one case and intalox saddles in another. Sieve trays used in Old Plants.


### 7.6.3 Detailed Tray Diagrams

Flow Through Vapor Passages


Limits of Satisfactory Tray Operation for a Specific Set of Tray Fluid Properties


Valve Trays


Top Two Trays of a Bubble-cap Column


Table 7.2: Comparison of Tray Types

| Type | Capacity | Turndown | Efficiency | Cost |
| :--- | :--- | :--- | :--- | :--- |
| Bubble | Third | $1^{\text {st }} \& 2^{\text {nd }}$ | Third | Third |
| Valve | Second | $1^{\text {st }} \& 2^{\text {nd }}$ | Second | Second |
| Sieve | First | Third | First | First |

Revised from Kitterman \& Ross ${ }^{2}$

### 7.6.4 Packing

The other type of contacting device widely used is packing. Packing provides extensive surface for liquid and gas contact. Packing is usually made of ceramic, metal or carbon shapes to give extensive surfaces. The names of the common shapes are:

1. Raschig ring
2. Intalox saddle
3. Berl saddle
4. Pall rings (Flexi rings are like pall rings)

The pall ring is considered to be the most efficient packing at present. Eckert ${ }^{19}$ gives a good review of different packings. Figure 7.7a shows a typical packed tower and packing shapes.

### 7.7 Tower Sizing - Trayed Towers

### 7.7.1 General

There are two problems process wise in tower sizing. These are the tower diameter and the tower height. The tower height is dependent on the actual number of stages required for a separation and the distance apart these stages are. The number of stages depends on whether distillation or absorption is to be practised. The determining of these number of stages will be discussed shortly. However, the tower diameter is not particularly a function of the transfer process but primarily a function of the gas and liquid load and the tower internals.

### 7.7.2 Diameter Determinations

### 7.7.2.1 Entrainment

This is the carryover of liquid particles from one stage to another. Entrainment is caused by high gas velocity and towers that are gas loaded are generally limited by entrainment.

### 7.7.2.2 Flooding

This occurs primarily whenever the downcomers fill up with liquid and any change of liquid or gas flow causes very erratic performance, high pressure drops and packing of the tower. This occurs primarily with liquid loaded towers, however the flooding point is a function of both liquid and gas rates.

### 7.7.2.3 Gas Loaded Towers

Towers are generally either gas or liquid loaded. For gas loaded towers the old Brown \& Souders ${ }^{3}$ equation can be used:

$$
v=K \sqrt{\frac{\rho_{L}-\rho_{V}}{\rho_{V}}}
$$

where:
$v=$ the allowable superficial velocity (empty tower) ft/sec
$\rho_{\mathrm{L}}=$ density of liquid at tower conditions
$\rho_{V}=$ density of vapour at tower conditions
$\mathrm{K}=\mathrm{a}$ constant
Or
Equation 7-34

$$
G_{\max }=C \sqrt{\rho_{V}\left(\rho_{L}-\rho_{V}\right)}
$$

where:
$\mathrm{G}_{\text {max }}=$ allowable mass superficial velocity $\mathrm{lb} / \mathrm{ft}^{2} / \mathrm{hr}$
$\mathrm{C}=\mathrm{a}$ constant, given in Figure 7.11,
which depends on the surface tension of the liquid in the tower and the distance between the plates. Values for K are given in Perry. For a 24 inch tray spacing the value of K varies from 0.15 to 0.18 . For example a test on a 6 ft diameter absorber with bubble caps was conducted. Here are the data obtained:

Brown \& Souders allowable gas velocity was 69.6 MMSCD
Bubble cap allowable velocity per article by Zenz was 85.3 MMSCFD
Actual Test (based on when significant entrained occurred) was 84.2 MMSCD
Use the previously given equations and data to give approximate diameter. For exact size the present practice is to specify the vapour and liquid loading, both maximum and minimum, the process and operating conditions, etc., and allow the tray manufacturer to select the tray size and tower diameter for you.

Koch, Clitsch, and Nutter (tray manufacturers) have prepared design manuals for tower sizing for English and metric calculations.
To use the data given here it is probably easiest to calculate vand G in English units and then convert to $\mathrm{m} / \mathrm{sec}$ or $\mathrm{kg} / \mathrm{hr} \mathrm{m}^{3}$ respectively. This applies through tower diameter determination.
Section 19 of the most recent English GPSA Data book gives a good review on tower capacities and calculations of same.

## Typical Packed Tower Layout and Common Packing Types




Figure 7.11: Tray Capacities

### 7.7.2.4 Liquid Loaded Towers

In liquid loading the prime consideration is the liquid backup in downcovers, that is the height of liquid in a downcomer.

Old recommended values have been 50\% of downcomer full of liquid for ordinary services and 35\% for foaming service. However, many towers have been operated at $60 \%$ without instability so it is recommended $50 \%$ be used all the time. The height of the liquid in a downcomer can be calculated as outlined below and is related to all the other pressure drops on a tray. This is a simplification but is generally accurate. In general the height of liquid in the downcomer can be calculated from the following equation:

Equation 7-35

$$
h=2\left(h_{w}+h_{o w}\right)+h_{v}+h_{D}
$$

where:
$h=$ the height of clear liquid in downcomer.
$h_{w}=$ height of weir.
$h_{\text {ow }}=$ height of liquid over weir.
$h_{v}=$ pressure drop due to vapour flow through tray.
$h_{D}=$ pressure drop due to liquid flow under down spout.
Downcomer maximum design liquid load is about $200 \mathrm{bbls} / \mathrm{ft}^{2} / \mathrm{hr}$ or $0.3 \mathrm{ft} / \mathrm{sec}$ velocity. Downcomer should not normally take up more than $15 \%$ of tower cross-sectional area.


Figure 7.12: Hold Up on Tray


Figure 7.13: Packed Tower Correlation

### 7.8 Tower Sizing Packed Columns

For the design of packed columns the generalized pressure drop correlation can be used. It is a plot of the gas flow multiplied by several factors pertaining to the type of packing and the fluids being fractionated against a liquid to gas ratio. This plot is given in Figure 7.13. This plot is shown in Perry, The U.S. Stoneware Book. This correlation shows pressure drop lines. The design procedure is to size the tower to operate at about $80 \%$ of flooding which is about 0.25 to 0.5 inch of $\mathrm{H}_{2} \mathrm{O} / \mathrm{ft}$. For foaming solutions use 0.1 inch of $\mathrm{H}_{2} \mathrm{O} / \mathrm{ft}$ of packing.
Figure 7.13 is a plot of:
Equation 7-36

$$
\left(\frac{L_{p}}{G_{p}}\right)\left(\frac{\rho_{V}}{\rho_{L}}\right)^{1 / 2} \quad \text { versus } \frac{G_{p}^{2} \mu_{L}^{0.1} F_{p}\left(\frac{\rho_{W}}{\rho_{L}}\right)}{32.17 \rho_{V}\left(\rho_{L}-\rho_{V}\right)}
$$

where:
$\mathrm{L}=$ liquid mass flow lb/hr/ft ${ }^{2}$
$\mathrm{G}=$ gas flow mass velocity $\mathrm{lb} / \mathrm{hr} / \mathrm{ft}^{2}$
$\rho_{\mathrm{v}}=$ gas density lb/ft ${ }^{3}$
$\rho_{\mathrm{L}}=$ liquid density $\mathrm{lb} / \mathrm{ft}^{3}$
$\rho_{w}=$ density of water
$\mu_{\mathrm{L}}=$ liquid viscosity in centipoise
$F_{p}=$ packing factor as given in the following table

## Table 7.3: Packing Characteristics

Packing Factors ( $F_{p}$ ) - (DUMPED PACKING)

| Packing Type | Material | Nominal Packing Size (inches) |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | $\mathbf{1 / 4}$ | $\mathbf{3 / 8}$ | $\mathbf{1 / 2}$ | $\mathbf{5 / 8}$ | $\mathbf{3 / 4}$ | $\mathbf{1}$ | $\mathbf{1 . 2 5}$ | $\mathbf{1 . 5 0}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{3 . 5}$ |
| IMTP $^{\circledR}$ | Metal |  |  |  | 51 |  | 40 |  | 24 | 18 | 12 |  |
| Hy-Pak $^{\text {TM }}$ | Metal |  |  |  |  |  | 45 |  | 29 | 26 |  | 16 |
| Super Intalox <br> Saddles |  |  |  |  |  |  |  |  |  |  |  |  |
| Super Intalox <br> Saddles |  |  |  |  |  |  |  |  |  |  |  |  |
| Pall Rings | Ceramic |  |  |  |  |  | 60 |  |  | 30 |  |  |
| Pall Rings | Plastic |  |  |  |  |  | 40 |  |  | 28 |  | 18 |
| Intalox Saddles ${ }^{\circledR}$ | Ceramic | 725 | 330 | 200 |  | 145 | 92 |  | 52 | 40 | 22 |  |
| Raschig Rings | Ceramic | 1600 | 1000 | 580 | 380 | 255 | 155 | 125 | 95 | 65 | 37 |  |
| Raschig Rings | $1 / 32 "$ Metal | 700 | 390 | 300 | 170 | 155 | 115 |  |  |  |  |  |
| Raschig Rings | $1 / 16^{\prime \prime}$ Metal |  |  | 410 | 300 | 220 | 144 | 110 | 93 | 62 | 32 |  |
| Berl Saddles | Ceramic | 900 |  | 240 |  | 170 | 110 |  | 65 | 45 |  |  |

Here are some very approximate inch height of equivalent theoretical plate (HETP) for Pall Rings.

| Packing Size | HETP |
| :---: | :---: |
| $5 / 8^{\prime \prime}$ | $6 "$ to $12^{\prime \prime}$ |
| $3 / 4 "$ | $12^{\prime \prime}$ to $18^{\prime \prime}$ |
| $1 "$ | 18 " to $24 "$ |
| $1112^{\prime \prime}$ | 24 " to $30 "$ |
| $2 "$ | $30 " ~-$ |

### 7.9 Tower Height - Distillation

### 7.9.1 General

In this case we are trying to separate the more volatile component from a less volatile component. To find the height of the equipment we wish to find the number of trays or the height of packing.
Let us first review some phase diagrams for two component systems. The temperature
composition diagram for a two component ideal system at constant pressure can be shown as follows:


Figure 7.14: Temperature Composition Diagram for Two Components
Consider a system of composition 1 at temperature 't'. Two-phase exists, ie.vapour and liquid. The vapour would have a composition at 2, i.e. smaller amount of A than at 1 and greater amount of B than at 1. The liquid would have a composition of 3, i.e. more of $A$ and less than B. This is how we can separate two components. Let us now see what a diagram of the relation between the composition of the gas phase and the liquid phase looks like. This, of course, is at constant pressure.


Figure 7.15: Vapour Liquid Composition Diagram
If the system is an ideal solution than Raoult's law applies, that:

$$
P P_{a}=x_{a} V P_{a}
$$

where:

$$
\begin{aligned}
& \mathrm{PP}_{\mathrm{a}}=\text { partial pressure of } \mathrm{A} \\
& \mathrm{VP}_{\mathrm{a}}=\text { vapour pressure of } \mathrm{A}
\end{aligned}
$$

and an ideal gas in vapour phase, Dalton's law applies, i.e.

$$
y_{A}=\frac{P P_{a}}{P T}
$$

where:
PT = total pressure
then the vapour liquid line is expressed by

$$
y_{a}=x_{a} \frac{V P_{a}}{P T}
$$

or if we have K data

$$
y_{a}=K_{a} x_{a}
$$

### 7.9.2 Two Component Distillation

Let us consider the distillation of two components a and b. First of all let us consider a tower and its auxiliary components.


Figure 7.16: Typical Distillation System for Two Components

## Consider:

$y=$ vapour composition of a (mole fraction)
$x=$ liquid composition of a (mole fraction)
$z=$ feed composition of a (mole fraction)

### 7.9.3 McCabe Thiele ${ }^{7}$ Method of Finding Number of Ideal Stages for a Two Component System

We make the following assumptions:

- Constant molal liquid flow down the tower to feed tray and then constant molal liquid below feed (but a different value).
- Similarly constant molal vapour flow in the two sections of the tower (but different in each section).
- There is not a significant heat of solution or a significant change in $H_{V}-H_{L}$ throughout the tower.

The method is as follows:

1. First we take a vapour liquid diagram for component A (See Figure 7.14 and 7.19).
2. Assume vapour leaving tray n is in equilibrium with liquid leaving tray n .

For whole column for component:
Equation 7-41
$F=D+W$
where:
F = Feed in moles
D = Overhead product
W = Bottoms product
For a single tray:
Equation 7-42
$V_{n+1}+L_{n-1}=V_{n}+L_{n}$
or a component
Equation 7-43
$V_{n+1}\left(y_{n+1}\right)+L_{n-1}\left(x_{n-1}\right)=V_{n} y_{n}+L_{n} x_{n}$
And since we have constant molal vapour flow and liquid flow:
Equation 7-44
$y_{n+1}+x_{n-1}=y_{n}+x_{n}$
$V=L+D=D(R+1)$
we know composition of $X_{D}$ and $X_{w}$ (products we wish).
3. We know that vapour from top tray $y_{1}=X_{D}$. Plot on diagram, Fig. 7.19. First let us take a molal material balance around enriching section (top section).


Figure 7.17: Tower Enriching Section

$$
R=\frac{L}{D}
$$

For component A :

$$
V y_{n+1}=L x_{n}+D x_{D}
$$

Divide by V:

$$
y_{n+1}=\frac{L}{V} x_{n}+\frac{D}{V} x_{D}
$$

$$
y_{n+1}=\frac{L}{D(R+1)} x_{n}+\frac{D}{D(R+1)} x_{D}
$$

Or we can say:

$$
y_{n+1}=\frac{R}{R+1} x_{n}+\frac{x_{D}}{R+1}
$$

This gives a line with a slope of $\frac{L}{V}=\frac{R}{R+1}$ which intersects the point $X_{D} y_{1}$. We draw this line on the plot, Figure 7.19. We can also do a material balance around the bottoms section.


Figure 7.18: Tower Fractionation Section
We find that the operating line will be a line with a slope of

$$
\frac{\bar{L}}{\bar{V}}=\frac{\bar{L}}{\bar{L}-W}
$$

which passes through $X_{w}$ which is on the $45^{\circ}$ line of $y=x$. As yet, however, we have not determined the value of $\bar{L}$. This depends on the condition of the feed.

The condition of the feed sets the $\bar{L}$ so we work on feed instead. First of all we know the composition of the feed $Z_{F}$. We set this value on the $45^{\circ}$ line (where $y=Z_{F}$, when $x=Z_{F}$ ).
Next we determine a factor " $q$ ". "q" is defined by the equation:
Equation 7-51

$$
q=\frac{\bar{L}-L}{F}=\frac{H_{V}-H_{F}}{H_{V}-H_{L}}
$$

This is proved by enthalpy balance on the feed plate where $H_{V}$ is the heat content of a saturated vapour of the composition of the feed. $H_{L}$ is the heat content of a saturated liquid of the composition of the feed. $\mathrm{H}_{\mathrm{F}}$ is the actual heat content of feed.

Now a q line for the feed can be established in which the slope is:

Equation 7-52

$$
\frac{q}{q-1}
$$

and it starts at $\mathrm{z}_{\mathrm{F}}$.
Actually on the feed tray it can be shown that
Equation 7-53

$$
y=\frac{q x}{q-1}-\frac{z_{F}}{q-1}
$$

where:
$Z_{F}=$ composition of the feed.
Now if we have a saturated vapour feed then the line is horizontal:
Equation 7-54

$$
\frac{q}{q-1}=0
$$

or if a saturated liquid, the line is vertical:
Equation 7-55

$$
\frac{q}{q-1}=\infty=\frac{1}{0}
$$

We can determine q from the properties of the components and thus draw the q line.
From the intersection of the $q$ line and the rectifying operating line we can join a line to $X_{w}$. This has the slope

$$
\frac{\bar{L}}{\bar{L}-W}
$$

and is the stripping section operating line. These two lines are drawn on Figure 7.19. We are now ready to find the number of theoretical plates.


Figure 7.19: McCabe Thiele Diagram
From a known $X_{D} y_{1}$ we find $x_{1}$ on the equilibrium curve by going horizontally to the equilibriums curve, we find $x_{1}$ in equilibrium with $y_{1}$. We then drop down to the operating line to find the point $\mathrm{x}_{1} \mathrm{y}_{2}$ and continue this way until $\mathrm{x}_{\mathrm{w}}$ is reached. Then the number of theoretical trays is found by counting the number of horizontal lines.

There are some refinements, like feed tray location, that can be worked out. See Page 539 in $K^{2} z^{5}$ for this method.

### 7.9.4 Ponchon $^{8}$ - Savarit ${ }^{9}$ Method for Number of Ideal Stages Use of H - X Diagram

The assumption of constant molal latent heat and constant molal overflow in the analysis of fractionating columns is not true for most practical cases. This limitation, and also the simplifying assumption of zero heat of solution of liquids and vapours, may be removed if the analysis is based on enthalpy balances as well as material balance and equilibrium considerations. The method was first proposed by Ponchon and Savaritt.
Binary vapour-liquid equilibrium can be plotted on coordinates of enthalpy vs concentration (at constant $P$ ). The liquid solution enthalpies include both sensible heat and the heat of mixing of components:

Equation 7-56

$$
H_{L}=C_{P L}\left(t_{L}-t_{0}\right) M_{a v}+D_{S}
$$

where:
$H_{L}$ is liquid enthalpy
$\mathrm{C}_{\text {PL }}$ is specific heat
$t_{L}$ is liquid temperature
$\mathrm{t}_{0}$ is reference temperature
$\mathrm{M}_{\mathrm{av}}$ is average mole weight
$\mathrm{DH}_{\mathrm{S}}$ is heat of mixing.
A typical H-xy diagram is shown in Figure 7.20. The Ponchon - Savarit method represents a graphical solution of the equations of SOREL (material and energy balance equations for each plate). The method of analysis is based on the graphical addition and subtraction of the properties of streams of liquid and vapour streams by the LEVER - ARM rule.

A typical H-xy diagram is shown below where xy are the concentration of the liquid and vapour phases respectively.


Figure 7.20: Ponchon - Savarit Diagrams
A brief description of the LEVER - ARM rule is given below.
Consider a system as shown in Figure 7.21 in which a binary mixture is fed into a column under such condition that it forms an equilibrium mixture of vapour and liquid. The flow rates will be designated as F (feed), D (distillate) and W (bottoms).


Figure 7.21: Vapour Liquid Program
An overall material balance and a component material balance (for the more volatile component) can be written as follows:

$$
F=D+W
$$

$$
F z_{F}=D y_{D}+W x_{w}
$$

Substituting for $F$ from equation (57) and rearranging (58) we obtain:
Equation 7-59

$$
\frac{D}{W}=\frac{z_{F}-x_{w}}{y_{D}-z_{F}}
$$

which provides a relationship between the rates of D and W and the composition of the streams.
We can also write an enthalpy balance for the column:

$$
F H_{F}=D H_{D}+W H_{W}
$$

and again, substituting for F from Equation 57 and rearranging to get

$$
\frac{D}{W}=\frac{H_{F}-H_{W}}{H_{D}-H_{F}}
$$

By combining equations (59) and (60) we can obtain a relationship between rates, compositions and enthalpies of the streams:

$$
\frac{D}{W}=\frac{z_{F}-x_{w}}{y_{D}-z_{F}}=\frac{H_{F}-H_{W}}{H_{D}-H_{F}}
$$

The proportionality between enthalpies and compositions expressed in this equation (60) can also be rearranged to give:

Equation 7-63

$$
\frac{1}{\text { slope }}=\frac{y_{D}-z_{F}}{H_{D}-H_{F}}=\frac{z_{F}-x_{w}}{H_{F}-H_{W}} \quad \text { with a common point } T
$$

which indicates that joints W, F and D, on the enthalpy-composition diagram representing feed, distillate and bottom streams must be on a straight line.
Streams $D$ and $W$ are in equilibrium and must be at the ends of a tie line through $F$.


Figure 7.22: More Ponchon - Savarit Diagrams

$$
\frac{\text { Distillate }}{\text { Bottoms }}=\frac{\overline{W F}}{F D}
$$

$$
\frac{\text { Bottoms }}{\text { Feed }}=\frac{\overline{F D}}{W D}
$$

and

$$
\frac{\text { Distillate }}{\text { Feed }}=\frac{\bar{F} \bar{W}}{W D}
$$

### 7.9.4.1 Analysis of a Fractionating Column

For a column, operating under steady state conditions (shown in Figure7.23), we can write the overall balance, as follows:
From equation $57, F=D+W$, and
Equation 7-67

$$
F z_{F}=D x_{D}+W x_{w}
$$

$$
F H_{F}+q_{r}=D H_{D}+W H_{W}+q_{c}
$$

where:
$q_{r}$ and $q_{c}$ are the total heats put into and removed from the reboiler and condenser, respectively.
To represent $q_{r}$ and $q_{c}$ on the $H-X$ diagram we can convert them into BTU/lb by noting that
Equation 7-69

$$
Q_{D}=\frac{q_{c}}{D} \quad B T U / l b \text { of } D
$$

$$
Q_{W}=\frac{q_{r}}{W} \quad B T U / l b \text { of } W
$$

The overall enthalpy balance can now be written as:
Equation 7-71

$$
F H_{F}=D\left(h_{D}+Q_{D}\right)+W\left(h_{B}-Q_{W}\right)
$$

or
Equation 7-72

$$
F H_{F}=\Delta_{D}+\Delta_{W}
$$

where the stream $\Delta_{D}$ has the coordinates $\left(X_{D}, h_{D}+Q_{D}\right)$ and the stream $\Delta_{W}$ has the coordinates $\left(X_{W}\right.$, $h_{w}-Q_{w}$ ) Equations (71) and (72) can be represented as a straight line (after the method just described) and this is done in Figure 7.24.

All pairs of passing streams within the column can be related to the points which represent $\Delta_{D}$ and $\Delta_{\mathrm{w}}$. The enthalpy balance for the top of the column, for example, is

$$
V_{n} H_{n}=L_{n+1} H_{n+1}+D h_{D}+q_{c}
$$

$$
V_{n} H_{n}-L_{n+1} H_{n+1}=D\left(h_{D}+Q_{D}\right)=\Delta_{D}
$$

$$
\frac{V_{n+1}}{D} H_{D}-\frac{L_{0}}{D} h_{0}=h_{0}+Q_{D}
$$

$$
V_{n+1}=L_{0}+D
$$

$$
\frac{L_{0}}{D}=\frac{h_{0}+Q_{D}-H_{D}}{H_{D}-h_{0}}
$$



Figure 7.23: PS Tower Analysis Diagram


Figure 7.24: Further PS Diagrams


Figure 7.25: Calculation of Number of Theoretical Stages in Rectifying Section


Figure 7.26: Calculation of Number of Trays in Stripping Section


Figure 7.27: Overall Tray Calculation


Figure 7.28: Minimum Reflux

Extrapolate the tie line which passes through the feed point $F$ until it intersects the vertical line at $X_{D}$.


Figure 7.29: Total Reflux
$\Delta_{\mathrm{D}}$ is at infinity. Therefore the operating lines are vertical.

### 7.9.5 Multicomponent Mixtures

The next problem is determining the number of trays for a multicomponent mixture. This is done by quite complex methods. There are a few short cut methods and also some general plate calculations using primary computers. One short cut method is based on the following:

1. Calculate minimum reflux ratio (when we have an infinite number of plates).
2. Calculate minimum number of equilibrium stages (when we have an infinite reflux).
3. Calculate actual number of equilibrium stages from minimum reflux ratio and minimum equilibrium stages using actual reflux.
To determine the minimum reflux and the minimum number of plates one method is to follow that outlined in Maxwell, Page 230.
This is the so-called Fenske Underwood Method. Let us define some quantities.
Key Component - The components that appear in both the top and bottom of fraction tower.
Light Key Component (LK) - The light component; appear primarily in the overhead.
Heavy Key Component (HK) - The heavy component; appear primarily in the bottoms.
$\boldsymbol{\alpha}$ - The relative volatility is the ratio of the K at a specific condition ot temperature and pressure for a component to the K value for the heavy key component.
Subscript LK and HK - mean light and heavy key components.
D - distillate or overhead product as a subscript (mols. dist./100 moles feed)
W - refers to bottom product as subscript and moles/bottom prod./100 moles feed
X - moles of any product/100 moles in distillate or bottoms of feed
$\mathbf{x}$ - mole fraction of any component in liquid
L - means any light component
H - means any heavy component exclusive of LK and HK
O-moles reflux/100 moles feed
Now to find the minimum number of plates the Fenske Equation can be used.
Let SM be minimum number of plates:
Equation 7-77

$$
\alpha_{L K}^{S M}=\frac{\left(X_{L K D}\right)\left(X_{H K W}\right)}{\left(X_{L K W}\right)\left(X_{H K D}\right)}
$$

Since we have assumed the final product's composition we can find SM. To evaluate $\alpha$ should find $\alpha$ at the top of the tower at dew point of distillate, $\alpha$ at bottom of tower at bubble point of bottoms, take the average tower temperature and pressure, and find $\alpha$, then multiply all three $\alpha$ 's together and take $1 / 3$ of this value. For ease take just arithmetic average of temperature and pressure at top and bottom and use this for finding $\alpha$.

The next problem is to calculate the minimum reflux. A method of doing this is the Underwood correlation. This is done by the use of two equations:

Equation 7-78

$$
\frac{\alpha_{1} x_{1 F}}{\alpha_{1}-\theta}+\frac{\alpha_{2} x_{2 F}}{\alpha_{2}-\theta}+\ldots \ldots+\frac{\alpha_{n} x_{n F}}{\alpha_{n}-\theta}=1-q
$$

Equation 7-79

$$
\frac{\alpha_{1} x_{1 D}}{\alpha_{1}-\theta}+\frac{\alpha_{2} x_{2 D}}{\alpha_{2}-\theta}+\ldots \ldots+\frac{\alpha_{n} x_{n D}}{\alpha_{n}-\theta}=R_{\min }+1
$$

where
$q=$ heat ratio of feed used in McCabe Thiele Method

$$
=\frac{H_{V}-H_{F}}{H_{V}-H_{L}}
$$

$\mathrm{X}_{\mathrm{F}}=$ composition in feed (mole fraction)
$x_{D}=$ composition in overhead product (mole fraction)
$\mathrm{R}_{\text {min }}=$ minimum reflux
$\theta=$ a mathematical term but can be estimated from knowing $\alpha_{L K}>\theta>\alpha_{H K}$
The method in general is to find $\theta$. Then knowing $\theta$ find $R_{\text {min }}$.
Van Winkle and Todd $^{18}$ have developed a graph giving approximate values of $\theta$. Figure 7.30 shows this data.


Figure 7.30: Underwood $\theta$ Values

Now to find the actual number of plates a graph has been prepared by Gilland ${ }^{12}$ giving the ratio of Actual Number of theoretical of plates to minimum versus actual reflux to minimum. This is shown as a nomograph and is given as Figure 7.32. It is based on the equation:

Equation 7-81

$$
\frac{S-S_{\min }}{S+1}=f \frac{R-R_{\min }}{R+1}
$$

Mapstone, in Hydrocarbon Processing, Page 169, May 1968, developed this nomograph.
The next item in the method is to pick an actual reflux. An actual reflux is an economic balance between tower height (low reflux compared to minimum, thus giving a high number of trays), and the tower diameter (high reflux and thus high through-put). Here are some values that are commonly used:

Table 7.4: Common Reflux Values

|  | O/D Reflux Overhead Product | Reflux to Feed |
| :--- | :---: | :---: |
| Deethanizer | ---- | $0.5-1.0$ |
| Depropanizers | $4-6$ | $1.0-2.0$ |
| Debutanizer | $2-3$ | $0.6-2.0$ |
| Butane Splitters | $10-12$ | $4.0-5.0$ |
| Stabilizer | $2-3$ | $0.5-2.0$ |
| Pentane Splitters | $10-12$ | $4.0-5.0$ |

Note: Typical application is $1.2 \times$ minimum for an economic reflux rate.
For special columns an actual economic analysis should be run. The figure below shows the type of results that will be obtained:



Figure 7.31: Economics of Number of Trays


Figure 7.32: Gilliland's Calculation for the Number of Theoretical Plates

## Example Problem 7.1

Determine the number of theoretical trays required for depropanizing a feed of the composition given below. The tower is to operate at 300 psig. The top temperature is $100^{\circ} \mathrm{F}$ and the bottom temperature is $310^{\circ} \mathrm{F}$. The anticipated separation is also given in the table below. The minimum reflux ratio for the separation is $2.0(\mathrm{O} / \mathrm{D})$ and the operating reflux ratio is expected to be approximately twice the minimum.

| Comp. | Feed Composition Mole \% | Overhead Product Moles/100 <br> moles feed | Bottoms Product Moles/100 <br> moles feed |
| :--- | :---: | :---: | :---: |
| $\mathrm{C}_{1}$ | 5.1 | 5.1 |  |
| $\mathrm{C}_{2}$ | 8.8 | 8.8 | 0.5 |
| $\mathrm{C}_{3}$ | 21.0 | 20.5 | 6.7 |
| $\mathrm{iC}_{4}$ | 7.0 | 0.3 | 13.0 |
| $\mathrm{nC}_{4}$ | 13.0 |  | 7.2 |
| $\mathrm{iC}_{5}$ | 7.2 |  | 12.4 |
| $\mathrm{nC}_{5}$ | 12.4 |  | 25.5 |
| $\mathrm{C}_{6}$ | 25.5 |  |  |

The method of Fenske will be used.
Find $\alpha_{L K}-$ For simplification, we will take it at 300 psig and $205^{\circ} \mathrm{F}$.

$$
\alpha_{L K}=\frac{K C_{3}}{K i C_{4}}
$$

Use NGPSA "K" data and assume $P_{K}=2000$
Equation 7-83

$$
\alpha_{L K}=\frac{1.6}{0.92}=1.74
$$

Now the Fenske equation:

$$
\alpha_{L K}^{S M}=\frac{\left(X_{L K D}\right)\left(X_{H K W}\right)}{\left(X_{L K W}\right)\left(X_{H K D}\right)}
$$

Equation 7-85

$$
(1.74)^{S M}=\frac{(20.5)(6.7)}{(0.5)(0.3)}=925 \quad \text { so } S M=12.3
$$

Now from Figure 7.32, since we know minimum number of trays, minimum reflux and actual reflux, the theoretical number of trays $=18$. The actual required number of trays is determined by
subtracting 1 from the ideal number of trays to take care of the reboiler and dividing the remaining number by the tray efficiency.

The location of the feed plate is also quite a detailed calculation. Here is a well known formula for locating the feed tray:

Equation 7-86

$$
\log _{10}\left(\frac{\text { Plates above feed }}{\text { Plates below feed }}\right)=0.206 \log _{10}\left[\left(\frac{W}{D}\right)\left(\frac{Z_{H K}}{Z_{L K}}\right)\left(\frac{X_{L K W}}{X_{H L D}}\right)^{2}\right]
$$

It should be noted that most actual towers have 3 feed nozzles.

### 7.9.6 Efficiency

We have determined the number of theoretical plates or equilibrium required for a separation. The next problem is the number or actual plates required. This is determined by dividing the tray efficiency into the theoretical number of trays.

$$
E(\text { overall efficiency })=\frac{n^{*}(\text { number of theoretical trays })}{n(\text { number of actual trays })}
$$

The tray efficiency can be correlated against $\alpha$ of key comp. $X \mu$, viscosity of feed.
Another method is to use the correlation of density and of flood as developed by Koch Engineering and shown as Figure 7.33. This also applies only to Fractionators.

| For a rough guide use $E$ for fractionator | $\sim 75 \%$ |
| :--- | :--- |
| absorbers | $35 \%$ for $C_{5}$ as key components. |
|  | $30 \%$ for $C_{4}$ as key components. |
|  | $25 \%$ for $C_{3}$ as key components. |



Figure 7.33: Efficiency Correlation

### 7.10 Tower Height Absorption

### 7.10.1 General

Let us consider what happens in a tower when absorption takes place. Consider first a two component system in both gas and liquid phases. In gas, assume pure gas with solute and in liquid assume pure solvent and solute. If we allow gas phase and liquid to come together they will eventually reach equilibrium. Thus we can, for fixed temperature and pressure conditions, get an equilibrium curve showing the relation between the concentration of the solute in the gas phase and in the liquid phase.

For example, here are some curves for $\mathrm{NH}_{3}$ in air and water:
Solute - material being absorbed
Solvent - carrier fluid


Figure 7.34: Absorption Curves
These curves can sometimes be expressed by:
4. Raoult's Law (when have ideal solution and gas)

$$
P_{v}=P_{v p} x
$$

where:
$P_{v}=$ partial pressure of solute in the gas
$x=$ mole fraction of the solute in solvent.
$\mathrm{P}_{\mathrm{vp}}=$ vapour press.
5. Henry's Law. This law is more often applicable.

$$
P_{v}=m^{\prime} x
$$

where:
$\mathrm{m}^{\prime}=$ Henry's Law constant.
Note: Henry's Law constant is determined experimentally. It is generally applied to dilute solutions.

### 7.10.2 Absorption of a Single Component

As in distillation we can apply a graphical method for solving the number of theoretical plates required in an absorber absorbing one component from an inert carrier gas and with a non-volatile solvent. We plot an equilibrium curve with ordinates of:

$$
Y=\frac{\text { moles solute }}{\text { moles inert carrier gas }} \quad \text { and } \quad X=\frac{\text { moles solute }}{\text { moles inert solvent in liquid }}
$$



Figure 7.35: More Absorption Curves
Figure 7.36 shows the tower to which Figure 7.35 refers. Let us consider a counter current absorber.


Figure 7.36: Counter Current Absorber
where:
$\mathrm{G}=\mathrm{moles} / \mathrm{hr} / \mathrm{sq} . \mathrm{ft}$. of insoluble carrier gas.
$\mathrm{L}=\mathrm{moles} / \mathrm{hr} / \mathrm{sq} . \mathrm{ft}$. of inert liquid.
A material balance can be written to show that the operating curve of slope $\frac{L}{G}$ passes through $X_{1}, Y_{1}$ and $X_{2}, Y_{2}$. Thus the number of trays can be stepped off. A stripper operates with operating curve below equilibrium line.

### 7.10.3 Multicomponent Absorption

For multicomponent absorption problems we need to introduce the absorption factor concept. This was developed by Kremser and modified by Brown and others. Consider the material balance around an abosrber plate " i " as shown in Figure 7.37 in a " n " number trays absorber.
Note: The absorption calculations as contrasted to some distillation calculations, the trays are numbered from top to bottom.

Equation 7-89

$$
L_{0}\left(X_{i}-X_{i-1}\right)=V_{n+1}\left(Y_{i+1}-Y_{i}\right)
$$

where:
$L_{o}=$ moles of lean oil entering the absorber.
$V_{n+1}=$ moles rich gas entering absorber.
$X_{i}=$ mole of single comp. in liquid leaving plate i.
$X_{i-1}=$ moles of single comp. in liquid to plate i per mole of lean oil.
$Y_{i}=$ moles of single comp. in gas from plate i per mole of rich gas.
$Y_{i+1}=$ moles of single comp. in gas to plate i per mole of rich gas.
Note: $X$ is mole ratio and $x$ is mole fraction.


Figure 7.37: Tray Numbering in Absorption
The actual mole fractions of vapour and liquid are

$$
y_{i}=\frac{Y_{i}\left(V_{n+1}\right)}{V_{i}}
$$

$$
x_{i}=\frac{X_{i} L_{0}}{L_{i}}
$$

where:
$V_{i}=$ mole of gas leaving plate "i".
$\mathrm{L}_{\mathrm{i}}=$ moles of liquid leaving plate "i".
$y_{i}=$ mole fraction of comp. in gas leaving "i'.
$x_{i}=$ mole fraction of comp. in liquid leaving "i".

$$
y_{i}=K_{i} x_{i}
$$

and

$$
Y_{i-1}=K_{i-1} x_{i-1}
$$

$\mathrm{K}_{\mathrm{i}}$ and $\mathrm{K}_{\mathrm{i}-1}$ are the equilibrium constants for a single component or tray i and $\mathrm{i}-1$ respectively.

## Substitute

$$
Y_{i}=K_{i} \frac{L_{0}}{L_{i}} \frac{V_{i}}{V_{n+1}} X_{i}
$$

also

$$
Y_{i-1}=K_{i-1} \frac{L_{0}}{L_{i-1}} \frac{V_{i}}{V_{n+1}} X_{i-1}
$$

Now substitute in (89) for $X_{i}$ and for $X_{i-1}$ in terms of $Y$ and find $Y_{i}$.

$$
Y_{i}=\frac{Y_{i+1}+\frac{L_{i-1}}{K_{i-1} V_{i-1}} Y_{i-1}}{L+\frac{L_{i}}{K_{i} V_{i}}}
$$

$$
\text { Let } \quad A=\frac{L}{K V} \text { or } A_{i}=\frac{L_{i}}{K_{i} V_{i}} \text { or } A_{i-1}=\frac{L_{i-1}}{K_{i-1} V_{i-1}}
$$

We have

$$
Y_{i}=\frac{Y_{i+1}+A_{i-1} Y_{i-1}}{L+A_{i}}
$$

We can eventually expand this equation to the following if we assume $A$ is constant through tower.
Equation 7-99

$$
\text { Absorption } \%=\frac{Y_{n+1}-Y_{1}}{Y_{n+1}-Y_{0}}=\frac{A^{n+1}-A_{0}}{A^{n+1}-1}
$$

Note: The left hand of the equation above is the amount of a single component absorbed. where:
$\mathrm{n}=$ the number of theoretical stages.
$Y_{O}=$ moles of a single comp. in gas in equilibrium with lean oil per mole of entering gas, i.e. with $100 \%$ stripped lean oil, " $\mathrm{Y}_{\mathrm{O}}$ " $=0$.
$Y_{n+1}=$ moles of single comp. in rich gas entering column/mole of rich gas.
$Y_{1}=$ moles of a single comp. in gas leaving top plate/mole of rich gas.
A chart of absorption factors " A " where " A " versus
Equation 7-100

$$
\frac{Y_{n+1}-Y_{1}}{Y_{n+1}-Y_{0}}
$$

versus number of plates is given on Figure 15-51 of GPSA Data Book.
This assumes that " A " is constant through the tower which is not necessarily so because $\frac{L}{V}$ changes and the temperature affects K .
Let us next consider a stripping column as shown.


Figure 7.38: Stripper Operation
We can also write a similar equation for stripping:
Equation 7-101

$$
\frac{X_{m+1}-X_{1}}{X_{m+1}-X_{0}}=\frac{S^{m+1}-S}{S^{m+1}-1}
$$

where:
$X_{1}=$ moles of comp. in stripped lean oil leaving stripper per mole of rich oil.
$X_{m+1}=$ moles of comp. in rich oil entering stripper per mole of rich oil.
$X_{0}=$ moles of comp. in liquid in equilibrium with stripping medium per mole of rich oil.
$\mathrm{m}=$ number of theoretical stripping trays.
$\mathrm{S}=$ stripping factor $\frac{K V}{L}$.
Same chart as used for the absorption factor can be used for stripping.

### 7.10.4 Simplified Method for Finding the Number of Trays for Absorption (Short Cut Method)

Given the gas rate, the oil rate and the \% absorption of the key component

1. Calculate from rich gas rate and lean oil rate.
2. From operating temperature and pressure find K for key component and thus calculate $\frac{L}{V K}$.
3. Go to chart Figure 15-50 in GPSA Data book and read the number of theoretical trays required for the desired key component recovery.
4. This gives a very conservative value (a larger number of trays than probably required), thus it is probably better to use one of the methods discussed further on.

### 7.10.5 Kremser Brown Method of Finding the Number of Trays for Absorption

Let us consider the Kremser Brown method of finding the number of trays for a specific absorption. Given the gas rate, the oil rate and \% absorption of the key component.

1. Calculate $\frac{L}{V}$ from rich oil rate (have to estimate amount of liquid absorbed) and rich gas rate.
2. From operating temperature and pressure find K for the key component and thus calculate $A=\frac{L}{K V}$ (Key comp. one being absorbed).
3. Go to chart Figure $15-51$ in GPSA Data Book and read the number of theoretical trays required for the desired key component recovery.
4. Calculate \% recovery of other components for this number of trays and the same $\frac{L}{V}$ ratio but a different K value because of a different component.
5. Check to see that $L$ assumed is OK - as long as it is not too much lower than that assume that it is probably OK to use.

### 7.10.6 More exact methods for finding absorption factors

### 7.10.6.1 Horton \& Franklin Method

Find effective plate and use conditions there. Find effective plate "i" from value of A for key absorption component, i.e. one that is being absorbed 50 to $80 \%$ (mostly $\mathrm{C}_{3}$ ).

| Value of "A" | Ratio $\frac{i}{n}$ |
| :---: | :---: |
| $0.0-0.1$ | 1.0 |
| $0.1-0.4$ | 0.9 |
| $0.4-1.0$ | 0.8 |
| $1.0-4.0$ | 0.7 |
| $4.0---$ | 0.6 |

Find $V_{i}$ from equation

$$
V_{i}=V_{1} \frac{n+1-i}{n}
$$

$$
\frac{V_{i}}{V_{i+1}}=\frac{V_{1}^{1 / n}}{V_{n+1}}
$$

By material balance find

$$
L_{i}=L_{0}+V_{i+1}-V_{1}
$$

We find the temperature by use of the following equation

$$
\frac{T_{n}-T_{i}}{T_{n}-T_{0}}=\frac{V_{n+1}-V_{i+1}}{V_{n+1}-V_{1}}
$$

Thus we have $V_{i}, L_{i}$ and Temperature, and thus find " $A$ ".

### 7.10.6.2 Edmister Method

The Edmister ${ }^{17}$ method uses an absorption factor based primarily equation

$$
A_{e}=\sqrt{A_{n}\left(A_{1}+1\right)+0.25}-0.5
$$

where:
$A_{e}=$ effective absorption factor.
$\mathrm{n}=$ leaving $\mathrm{n}^{\text {th }}$ plate (bottom of tower conditions).
$1=$ entering $1^{\text {st }}$ plate (top of tower conditions).

### 7.10.7 Encountered Problems

Let us consider some of the problems in using a constant "A" or "S". A graph is given in Katz telling the maximum temperature rise against lbs. of gas absorbed/lb. solvent, on page 519.

### 7.10.7.1 Temperature Effects

A typical temperature profile in an absorber is shown in Figure 7.39. As can be seen the temperature in the tower varies a great deal.


Figure 7.39: Temperature of Absorption

### 7.10.7.2 Changes Throughout the Tower

$\frac{L}{V}$ changes throughout the tower. The moles of liquid increase as material is absorbed throughout the tower and the moles of rich gas obviously decrease.

## Example Problem 7.2

Calculate the number of theoretical plates required to absorb $80 \%$ of the propane in the gas of the composition given in the table below. The gas flow is 50 MMSCFD to the tower and the lean oil rate is 200 US gpm of a 140 mole wt. oil with a gravity of $50^{\circ} \mathrm{API}$. The tower operates at 900 psig and $0^{\circ} \mathrm{F}$.
f) Simplified or Shortcut method.

Find:

$$
\begin{aligned}
& A=\frac{L}{V K} \\
& \mathrm{~V}=\text { Rich }=\frac{50 \times 10^{6}}{379}=132,000 \text { moles } / \text { day } \\
& \mathrm{L}=\text { Lean Oil }=\frac{200(8.33)(.7796)(60)(24)}{140}=13,400 \text { moles } / \text { day } \\
& K_{C_{3}} \text { at } 900 \text { psig and } 0^{\circ} \mathrm{F}=0.13
\end{aligned}
$$

$$
A=\frac{L}{V K}=\frac{13.400}{132,000(.13)}=.78
$$

Number of trays required $=9$
g) Use Edmister's Method.

Gas Analysis:

| Comp. | Mole \% | $K_{900}^{0}$ psig * | Estimate of \% <br> Absorption $\mathbf{~}$ | Moles/100 moles Feed <br> Absorber |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{N}_{2}$ | 0.30 | 9.4 | nil | 0.00 |
| $\mathrm{C}_{1}$ | 91.63 | 2.6 | 3.9 | 3.57 |
| $\mathrm{C}_{2}$ | 5.72 | 0.48 | 21.1 | 1.21 |
| $\mathrm{C}_{3}$ | 1.63 | 0.13 | 80 (given) | 1.30 |
| $\mathrm{iC}_{4}$ | 0.29 | 0.052 | 97 | 0.28 |
| $\mathrm{nC}_{4}$ | 0.31 | 0.037 | 100 | 0.31 |
| $\mathrm{C}_{5}$ | 0.12 | 0.016 | 100 | 0.12 |
|  |  | Total | 6.79 |  |

*     - Using $\mathrm{P}_{\mathrm{K}}=5000$ and NGSMA (1957) K's
- Estimated by calculating $\frac{L}{V K}$ for each component and using 9 theoretical trays.

Find $\mathrm{A}_{1}$ and $\mathrm{A}_{\mathrm{n}}$
$V$ for $A_{n}=V_{\text {Rich Gas }} 132,000$ moles/day
$L_{n}=L_{\text {Rich Liquid }}=L_{\text {Lean oil }}+L_{\text {Liquids Absorbed }}$
$L_{\text {Liquids Absorbed }}=0679(132,000)=8963$ moles/day
$L_{n}=13,400+8963=22,363$ moles $/$ day
$: A_{n}=\frac{22,363}{132,000(.13)}=1.30$
V and $\mathrm{A}_{1}=\mathrm{V}_{\text {Lean Gas }}=132,000-8,963=123,067 \mathrm{moles} /$ day
$L_{1}=L_{\text {Lean oil }}=13,400$
$: A_{1}=\frac{13,400}{123,067(.13)}=0.84$
Find $\mathrm{A}_{\mathrm{e}}$
$=\sqrt{\mathrm{A}_{\mathrm{n}}\left(\mathrm{A}_{1}+1\right)+.25}-0.5$
$=\sqrt{\mathrm{A}_{\mathrm{n}}\left(\mathrm{A}_{1}+1\right)+.25}-0.5=1.13$
No. of trays for $80 \% \mathrm{C}_{3}$ absorption $=3.1$

### 7.11 Adsorption

This is the phenomena of mass transfer from a gas to solid (or liquid to solid). Such operations as drying or leaching are the reverse of this.
We will consider only gas adsorption. There are two types.

### 7.11.1 Physical Adsorption (van der Waal's Adsorption)

In this there is inter-molecular attraction between the molecules of the adsorbent (material which is adsorbing) and absorbate (material which is being adsorbed). Quite often the inter-molecular force is greater than the force between the gas itself and it condenses on the adsorbent even though the vapour pressure of the condensate is greater than pressure of the substance in the gas at this temperature. Heats of adsorption in this case are similar to heats of sublimation. This phenomena is reversible.
This type of adsorption can be described by the so-called Freundlich Equation
Equation 7-106

$$
w_{i}=\alpha\left(p_{i}\right)^{n}
$$

where:

$$
\begin{aligned}
& \mathrm{w}=\text { the concentration of adsorbate on adsorbent } \mathrm{lb} / \mathrm{lb} \\
& \rho_{\mathrm{i}}=\text { partial pressure of adsorbate } \\
& \alpha=\text { constant } \\
& \mathrm{n}=\text { constant }
\end{aligned}
$$

### 7.11.2 Chemical Adsorption

In this case a chemical reaction takes place and if chemical bond is strong the process is not easily reversible.

### 7.11.2.1 Equilibrium Data

As in other mass transfer operations we have experimental equilibrium data. We actually obtain equilibrium of material in a gas phase versus percent adsorbed on bed. A typical adsorption equilibrium curve is shown below

lbs. absorbed 100 lb . dessicant
Figure 7.40: Adsorption Curve

### 7.11.3 Nature of Adsorbents

These are usually granular in form. In particular they are characterized by having an extensive internal surface, i.e. a lot of internal pores. For example, gas mask charcoal has 1,000,000 sp. meters of surface per Kilogram of substance.

### 7.11.4 How Adsorption Proceeds

We are mostly concerned with the adsorption of $\mathrm{H}_{2} \mathrm{O}$ and HC and how facilities for doing this job are designed. Let us consider how the adsorption of $\mathrm{C}_{3}, \mathrm{C}_{4}, \mathrm{C}_{5}{ }^{+}$proceeds. Figure 7.42 shows this. First of all, water is adsorbed with the heavier hydrocarbons and finally the light ones.

### 7.11.5 Sizing of Beds

To determine length of bed, need to know volume of adsorbent to use. This can be obtained from dynamic equilibrium curves as shown in Figure 7.41 which shows data for $\mathrm{C}_{4}, \mathrm{C}_{5}$ and $\mathrm{C}_{6}$ adsorption.


Figure 7.41: Component Adsorption Data
For propane and butane the amount of adsorption can be calculated from the following equations for $\mathrm{C}_{4}, \log \mathrm{~S}=-0.0988 \frac{T}{M \log \frac{k}{y}}+0.7770$
for $\mathrm{C}_{3}, \log \mathrm{~S}=0.0765 \frac{T}{M \log \frac{k}{y}}+0.6098$
where:

```
\(\mathrm{S}=\) component saturation US gallon/100 lbs adsorbent
\(\mathrm{T}=\) absolute temp. \({ }^{\circ} \mathrm{R}\)
\(\mathrm{M}=\) molecular weight of Component
\(\mathrm{k}=\) Vapour Liquid Equilibrium constant
\(y=\) Mole fraction of component in the inlet gas
```

If we wish to find the length, set percent recovery, find amount of to be adsorbed in cycle time, usually 20 to 30 minutes, then from equilibrium curves or equations the quantity of adsorbent is determined by adding the quantity required for each component. The velocity of the gas sets the diameter. It is usually about $40-45 \mathrm{ft} / \mathrm{mm}$. as a superficial velocity. Thus the length can be determined.


Figure 7.42: Adsorption Progress with Time

### 7.12 Example Problems

## Example Problem 7.3

A debutanizer is designed so that the overhead product has only $2 \%$ of isopentane in it and the bottom has only $3 \%$ n-butane in it. The design feed composition and the top and bottom composition is given in the table below. During the operation of the tower the feed composition is changed to that also shown in the table. Determine what the increase in ref lux ratio has to be to make the separation.

| Comp. | Moles Design <br> Feed | New Feed Moles | Overhead Moles 100 | Bottom Moles 100 <br> Design | Bottom Moles 100 <br> New Feed |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{C}_{3}$ | 0.5 | 0.5 | 0.5 | ---- | ---- |
| $\mathbf{i C}_{4}$ | 10.5 | 10.5 | 10.5 | --- | --- |
| $\mathrm{nC}_{4}$ | 20.0 | 20.0 | 17.9 | 2.1 | 2.1 |
| $\mathbf{i C}_{5}$ | 8.5 | 21.0 | 0.6 | 7.9 | 19.9 |
| $\mathrm{nC}_{5}$ | 10.5 | 20.0 | --- | 10.5 | 20.5 |
| $\mathbf{C}_{6}$ | 10.5 | 12.0 | --- | 10.5 | 12.0 |
| $\mathbf{C}_{7+}$ | 18.5 | 6.5 | ---- | 18.5 | 6.5 |
| $\mathbf{C}_{8}$ | 21.0 | 9.5 | --- | 21.0 | 9.5 |

The tower has 17 actual trays. Assume that the tray efficiency is $70 \%$. The tower operating pressure is 100 psia. The average temperature is $150^{\circ} \mathrm{F}$ which is the feed temperature. Tower top temperature is $120^{\circ} \mathrm{F}$.

## Example Problem 7.4

A fractionation tower is designed to split a feed (as given in the Table) into a top and bottom product, the composition of which are also given in the Table.

## Mole Percent

| Comp. | Feed | Top Product | Bottom Product |
| :---: | :---: | :---: | :---: |
| $\mathrm{iC}_{4}$ | 10.0 | 15.3 | ---- |
| $\mathrm{nC}_{4}$ | 15.0 | 22.7 | ---- |
| $\mathrm{iC}_{5}$ | 17.0 | 25.8 | ---- |
| $\mathrm{nC}_{5}$ | 23.0 | 33.2 | 2.9 |
| $\mathbf{C}_{6}$ | 25.0 | 3.0 | 67.6 |
| $\mathrm{C}_{7}$ | 10.0 | --- | $\mathbf{2 9 . 5}$ |
| Total | $\mathbf{1 0 0 . 0}$ | $\mathbf{1 0 0 . 0}$ | $\mathbf{1 0 0 . 0}$ |

The minimum reflux based on the overhead products is 4 to 1 . An existing condenser is to be used that has a duty such that it is able to totally condense 7 times the amount of overhead product produced. This condenser will condense the overhead product $100^{\circ} \mathrm{F}$ using cooling water.
Calculate the number of actual trays required for this separation. Assume an overall tray efficiency of $75 \%$.

## Example Problem 7.5

It is planned to install a depropanizer the split as given in the table below.

| Comp. | Feed Moles | Overhead Moles / 100 <br> mole feed | Bottom Product Moles / 100 <br> mole feed |
| :---: | :---: | :---: | :---: |
| $\mathbf{C}_{\mathbf{2}}$ | 4.0 | 4.0 | ---- |
| $\mathbf{C}_{3}$ | 40.5 | 39.0 | 1.5 |
| $\mathrm{iC}_{4}$ | 10.5 | 1.0 | 9.5 |
| $\mathrm{nC}_{4}$ | 16.4 | ---- | 16.4 |
| $\mathrm{iC}_{5}$ | 10.7 | --- | 10.7 |
| $\mathrm{nC}_{5}$ | 8.9 | --- | 8.9 |
| $\mathbf{C}_{6}$ | 9.0 | --- | 9.0 |

The minimum reflux ratio for the separation is 1.8 . Determine how many trays are required in the tower.

## Data

A tower with an actual reflux ratio 1.3 times the minimum costs $\$ 500,000$. Each tray more than required with the 1.3 times the minimum actual reflux cost \$30,000 extra to install, including all auxiliaries.

The overhead product to be produced is 25,000 BPD. Extra trays are to be added if they pay out in the fuel savings obtained by reducing reflux requirements. The pay out time is to be 2 years to less.

The heat of condensation of a barrel of overhead product is 33,000 BTU's/BBL.
The cost of fuel is $\$ 1.00 / \mathrm{MMBTU}$ 's delivered to the plant. Assume the fuel is burned in a furnace that is $75 \%$ efficient.

The tower is operating at a pressure of 200 psia . The tower average temperature is $160^{\circ} \mathrm{F}$.
Assume the tower operates 350 days/year. Assume the trays are $80 \%$ efficient.

## Example Problem 7.6

An existing absorption unit handles 300 MMSCFD at 14.4 psia and $60^{\circ} \mathrm{F}$ of gas of the analysis given below. It is operated at an average temperature of $80^{\circ} \mathrm{F}$ with 160 MW oil. It is proposed to increase the recovery of propane and heavier by using a lower molecular weight oil of 100 MW chilling the oil and gas so that the average tower temperature is $0^{\circ} \mathrm{F}$. The oil circulation rate is to remain the same (i.e. the same (GPM). The cost of this revamp is estimated to be $\$ 6,000,000$. If propane is worth $\$ 7.00 / \mathrm{Barrel}, \mathrm{C}_{4}$ 's are worth $\$ 7.70 / \mathrm{BBI}$ and $\mathrm{C}_{5}{ }^{+1}$ s are $\$ 9.50 / \mathrm{BBI}$, determine the payout for the proposed facility.

## Gas Analysis

| Comp. | Moles |
| :--- | :---: |
| $\mathrm{C}_{1}$ | 91.34 |
| $\mathrm{C}_{2}$ | 5.27 |
| $\mathrm{C}_{3}$ | 1.92 |
| $\mathrm{iC}_{4}$ | 0.32 |
| $\mathrm{nC}_{4}$ | 0.60 |
| $\mathrm{iC}_{5}$ | 0.15 |
| $\mathrm{nC}_{5}$ | 0.18 |
| $\mathrm{C}_{6}$ | 0.22 |

## Assumptions

a) The value of the $\mathrm{C}_{3}$ and heavier in the gas is $\$ 1.05 / \mathrm{MM} \mathrm{BTU's}$.
b) The extra operating costs, except raw materials costs, are considered negligible.
c) The present unit is designed for $40 \% \mathrm{C}_{3}$ recovery. The oil rate is minimum for this recovery.
d) The tower operating pressure is 600 psia .
e) Assume $P_{K}$ for any calculation of 2000 psia .
f) Assume just pure products recovered, i.e. do not calculate impurities of commercial $\mathrm{C}_{3}$, $\mathrm{C}_{4}$, etc.

## Example Problem 7.7

A rich oil of the following composition is fed to a stripping tower with 8 theoretical trays.

| Comp. | Mole \% | Moles/Day |
| :--- | :--- | :--- |
| $\mathrm{C}_{3}$ | 12.0 | ---- |
| $\mathrm{iC}_{4}$ | 4.2 | ---- |
| $\mathrm{nC}_{4}$ | 5.6 | --- |
| $\mathrm{iC}_{5}$ | 2.7 | ---- |
| $\mathrm{nC}_{5}$ | 3.0 | ---- |
| $\mathrm{C}_{6}$ | 2.3 | ---- |
| Lean Oil | 70.2 | ---- |
|  | $\mathbf{1 0 0 . 0}$ | $\mathbf{1 0 , 0 0 0}$ |

You are to find the amount of 18 mole wt. stripping gas (in SCFD) to remove most of the butane and lighter, i.e. $90 \%$ of the $\mathrm{nC}_{4}$. The average tower pressure is 200 psia. Temperature at the top is $220^{\circ} \mathrm{F}$ and temperature at the bottom is $400^{\circ} \mathrm{F}$.

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### 8.0 Heat Transfer

- General theory and types of heat transfer.
- Types of equipment and equipment design criteria.


### 8.1 Introduction

This is the transfer of energy between a source and a sink. We are primarily interested in the rate of transfer so that we can size equipment for heat transfer properly. There are three types of heat transfer ${ }^{4}$.

### 8.1.1 Conduction

The transfer of heat from one part of a body to another part of the same body or from one body to another in physical contact with it, without appreciable displacement of the particles of that body. For steady state conduction the rate equation of

$$
\text { Rate }=\frac{\text { driving force }}{\text { resistance }}
$$

or

$$
d Q=K A \frac{d t}{d x}
$$

where:

> dQ = heat transfer rate.
$\mathrm{K}=$ thermal conductivity.
A = area of transfer.
$\mathrm{dt}=$ temperature difference.
$\mathrm{dx}=$ thickness of place in which the transfer is taking place.
or integrated at a steady state
Equation 8-2

$$
Q=\frac{K}{x} A\left(t_{1}-t_{2}\right)
$$

Figure 8.1 shows the system.

[^10]

Figure 8.1: Heat Transfer System
The value of $K$ depends on material:
For insulators - very low.
For conductors - very high.

### 8.1.2 Convection

This is the transfer of heat from one point in a fluid to point in the fluid. Natural convection occurs when there is no except because of heat transfer. Forced convection occurs when in motion, i.e. pumped or agitated. This type of transfer is expressed by the equation

Equation 8-3
$d Q=h A d t$
where:
A = area of transfer.
$\mathrm{dt}=$ the temperature difference.
$\mathrm{h}=\mathrm{a}$ film coefficient which depends on fluid flow rate, the fluid properties, etc.
This is the type of heat transfer is mostly encountered in gas processing.

### 8.1.3 Radiation

This is the transfer of heat from one body to another not in contact with it by means of wave motion. This heat transfer is expressed by the Boltzmann equation:

Equation 8-4

$$
d Q=\sigma \varepsilon d A T^{4}
$$

where:
$\sigma=$ a constant
$\varepsilon=$ emissivity for the substance involved
$\mathrm{T}=$ the absolute temperature.
$\mathrm{dA}=$ the differential area from which heat transfer takes place.
the " $\varepsilon$ " needs defining. It is the actual amount of energy that is absorbed or radiated as compared to a black body which has the value unity.
The transfer of heat between two surfaces can be expressed as:

$$
Q_{12}=0.173 A_{1}\left[\varepsilon_{1}\left(\frac{T_{1}}{100}\right)^{4}-\alpha_{12}\left(\frac{T_{2}}{100}\right)^{4}\right]
$$

or in metric

$$
Q_{12}=2.06 \times 10^{7} A_{1}\left[\varepsilon_{1} T_{1}^{4}-\alpha_{12} T_{2}^{4}\right]
$$

$\alpha_{12}=$ absorptivity at point 2
Quite often $\alpha 12=\varepsilon 1$ and the equation can be simplified.
Figure 8.2 shows the system for which the equation applies.


Figure 8.2: Radiation System
Both convection type heat transfer and radiation type heat transfer will be considered later in this section.

### 8.2 Heat Exchange Equipment

There are many types of heat exchange equipment. A few of the more important types are given in the following discussion.

## Double Pipe Exchanger

One pipe inside the other, used in small size, $300 \mathrm{ft}^{2}\left(28 \mathrm{~m}^{2}\right)$ or lower.

## Shell and Tube Exchanger

Many tubes inside a single shell. Figure 8.3 shows the many types of flow that can be expected in shell and tube exchangers. Also Figure. 8.6 in the GPSA Manual shows some other configurations. These can be divided mechanically as follows:

1. Fixed Tube Sheet - cannot remove tube bundle and thus cannot clean mechanical outside surface of tubes. Use in clean services:

- LPG service
- Sweet gas to gas exchangers

2. Floating Head Exchangers - can remove tube bundle and clean outside of tube surface. Use in dirty services:

- Sour condensate
- Rich/lean Amine

3. U Tubes - can remove tube sheet and clean shell side satisfactorily but need clean tube fluid. Used mainly in reboiler service:

- Amine still reboiler


Tube Sheets Fixed Both Ends Single Shell Pass


Twa Shell Passes with or without Expansion Joint. (Exponsion Joint. Complicates)


Evaporotor or Chiller
Divided Flow
Two Shell Passes Each Section


> U-Bund!e Shel' Single She!! Poss


U-Bundie Two Shell Passes


Ketile Evgporafor U-Bundle or Flooting Tube Shee: Single Shell Pass


Kettle Reboiler U-Bundle
or Floating Tube Sheet
Single Shell Pass

Figure 8.3: Shell and Tube Heat Transfer Equipment

### 8.2.1 Other Liquid to Liquid Exchangers

Other liquid to liquid exchangers sometimes used are:

1. Coil in box exchangers
2. Trombone exchangers (Falling film on outside of pipes).
3. Plate and fin - a series of corrugated fins and a plate as shown in Figure 8.4.


Figure 8.4: Plate and Fin Liquid to Liquid Exchanger

### 8.2.2 Air Exchangers

In this case air is used instead of water as the cooling medium. These units consist of a finned tube section in which the fluid to be cooled is sent through and a fan which either blows air through the tubes or induces it through same.

There have been many problems in locating these units properly in plants because of recirculation problems. Often stacks have to be put on these exchangers to make sure recirculation is minimized. The choice between Air Cooling and Water Cooling requires close study.
Water Cooling gives lower temperatures and thus lower operating pressure but generally requires a cooling tower.

When Air Cooling is used higher operating pressures are needed. This is particularly costly when refrigeration compressors are needed. Figure 8.5 shows some details of aerial coolers.


Figure 8.5: Aerial Coolers

### 8.2.3 Costs

The relative costs of the various exchangers considered are given in the table below.
Table 8.1: Exchanger Costs

| Exchanger Type | Relative Cost in Carbon Steel |
| :--- | :--- |
| Fixed tube sheet | 1.0 |
| Floating Head Tube Sheet | 1.28 |
| U Tube | 1.08 |
| Kettle type U Tube with enlarged shell | $1.2-1.4$ |


| Double Pipe | $0.8-1.4$ |
| :--- | :---: |
| Pipe Coil | $0.5-0.7$ |
| Open Tube Section Water Cooled | $0.8-1.1$ |
| Open Tube Section Air Cooled | $0.8-1.8$ |

### 8.2.4 Furnaces

There are of course, many types of furnaces. Generally they look like:


Figure 8.6: Typical Furnace
A good conservative design is to use 10-12,000 BTU/square feet (110,000-130,000 kjoules $/ \mathrm{m}^{2}$ ) as a heat flux in the radiant section.
Furnace design is a special science which has many problems, such as:

- Whether to put tubes vertical or horizontal.
- How far away from tubes should the fire be.
- The tube material - close review should be made to see if really carbon steel should be used. Often some type of alloy is worthwhile because of its longer service life.


### 8.3 Equipment Sizing

### 8.3.1 Heat Exchangers

In most cases in gas processing the equipment used for heat transfer uses convection as the primary method of heat transfer. Generally the following equation expresses the mechanics:

Equation 8-6

$$
Q=U A \Delta T
$$

where:
$Q=$ heat transfer rate BTU/hr (Watts)
$A=$ area required for transfer $\mathrm{ft}^{2}\left(\mathrm{~m}^{2}\right)$

$$
\mathrm{U}=\text { overall heat transfer coefficient in } \frac{B t u ' s}{h r f t^{2}{ }^{\circ} \mathrm{F}} \frac{\text { Watts }}{m^{3}{ }^{\circ} \mathrm{C}}
$$

$$
\Delta \mathrm{T}=\text { the temperature difference }{ }^{\circ} \mathrm{F}\left({ }^{\circ} \mathrm{C}\right)
$$

The size of the equipment required is determined by the area " A " for heat transfer. This is generally what is to be determined. Let us then consider the other items in the equation.
$\boldsymbol{Q}$ - This is determined by a heat balance around the exchanger, i.e. by the equation:
Equation 8-7

$$
Q=W C_{P}\left(T_{1}-T_{2}\right)=W\left(H_{1}-H_{2}\right)
$$

where:
$\mathrm{W}=$ mass flow rate .
$C_{P}=$ the specific heat.
$\mathrm{T}_{1}=$ the entrance temperature on one side of the exchanger.
$T_{2}=$ the exit temperature from the same side of the exchanger.
$H_{1}=$ Enthalpy of material at temperature ( $T_{1}$ ) (and pressure $P_{1}$ if a gas).
$\mathrm{H}_{2}=$ Enthalpy of material at temperature $\left(\mathrm{T}_{2}\right)$ (and pressure $\mathrm{P}_{2}$ if a gas).
$\boldsymbol{\Delta T}$ - First let us review the temperature in a double pipe exchanger as shown in Figure 8.6. In this case we have what is called true counter flow.


Figure 8.7: Counter Current Exchanger
To determine the average temperature difference for the exchanger shown in Figure 8.6 we use the equation given below:

Equation 8-8

$$
\Delta T_{L M T}=\frac{\left(T_{1}-t_{2}\right)-\left(T_{2}-t_{1}\right)}{\ln \frac{T_{1}-t_{2}}{T_{2}-t_{1}}}
$$

or

$$
\Delta T_{L M T}=\frac{\Delta T_{\text {HOT END }}-\Delta T_{\text {COLD END }}}{\ln \frac{\Delta T_{\text {HOT END }}}{\Delta T_{\text {COLD END }}}}
$$

This equation can be proved to apply for both counter current and parallel flow. Figure 8.1 on page 8.2 of the GPSA Data Book solves this equation for us graphically.

We have another problem in regular shell and tube heat exchangers. That is, we do not have true counter or co-current flow.


Figure 8.8: Typical Exchanger Configuration
For example we have some cross flow, some counter flow, some cocurrent flow. For this a factor by which the true log mean temperature is multiplied, is calculated. This factor is a function of the terminal temperature and the number of shell passes and tube passes. The average temperature is given by:

Equation 8-10

$$
\Delta T_{M}=F \Delta T_{L M T}
$$

where:
$\mathrm{F}=\mathrm{a}$ factor which is determined from the ratio of temperature difference on each side of the exchanger "R" where

$$
R=\frac{T_{1}-T_{2}}{t_{2}-t_{1}}
$$

and temperature efficiency $P$ which is the tube side temperature difference divided by the difference between the hot temperature entering the exchanger and the cold temperature entering the exchanger. ie.

$$
P=\frac{t_{2}-t_{1}}{T_{1}-t_{1}}
$$

$\Delta \mathrm{T}_{\text {Lмт }}$ is the true log mean temperature.
The charts on pages 8-3 and 8-4 of the GPSA Data Book cover the important cases for determining F. The charts on pages 9-5 and 9-6 of that manual should be used for air exchangers.

The most important item in an exchanger sizing is "U". This is normally determined by the exchanger manufacturer for the conditions given in a specification sheet. However, a knowledge of overall U's is of particualr value to the gas engineer. Figure 8-6 and Figure. 9-5 of the GPSA Data Book gives some common values to be expected. These are somewhat conservative. To see how the $U$ is determined we will review how $U$ is calculated. In a heat exchanger the heat transfer rate across a tube can be given by:

Equation 8-11

$$
\frac{1}{U_{0}}=\frac{1}{h_{0}}+\frac{1}{h_{i}} \frac{D_{0}}{D_{i}}+R
$$

where:
$\mathrm{U}_{\mathrm{O}}=$ overall heat transfer area based on outside of tube surface.
$h_{0}=$ film heat transfer coefficient based on the outside of tube surface.
$R=$ fouling factor as given in the TEMA ratings and discussed later.
For determining $h_{o}$ and $h_{i}$ there are several empirical equations. The GPSA Data Book gives a chart for determining $h_{i}$, Figure 9-7 on Page 9-8. Figure $8-8$ gives the chart for $h_{\circ}$. We will review the method used and give an example problem. We are considering only heat transfer without a change of phase (i.e. no boiling or condensing).
$\mathbf{h}_{\mathbf{i}}$ - the inside film coefficient. An equation that is often used is the Sieder and Tate equation ${ }^{8}$
Equation 8-12

$$
\frac{h_{i} D_{i}}{K}=0.027\left(\frac{D_{i} G}{\mu}\right)^{0.8}\left(\frac{C_{P} \mu}{K}\right)^{\frac{1}{3}}\left(\frac{\mu}{\mu_{W}}\right)^{0.14}
$$

This equation has been expressed in graphical form by plotting
Equation 8-13

$$
j \equiv\left(\frac{h_{i} D}{K}\right)\left(\frac{C_{P} \mu}{K}\right)^{-1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{-0.14}
$$

versus the Reynolds Number. This is given as Figure 9-7 of the GPSA Data Book. The Parameter L/D is also shown on the chart.
where:
$h_{i}=$ heat transfer coefficient $B T U / h r / s q . f t /{ }^{\circ} \mathrm{F}\left(\mathrm{W} / \mathrm{M}^{2}{ }^{\circ} \mathrm{C}\right)$.
$D=$ tube ID in feet.
$\mathrm{K}=$ fluid thermal conductivity $\mathrm{BTU} / \mathrm{hr} / \mathrm{ft} /^{\circ} \mathrm{F}$.
$\mu=$ fluid viscosity lbs/ft ${ }^{2} / \mathrm{hr}$.
$\mathrm{C}_{\mathrm{p}}=$ fluid specific heat $\mathrm{BTU} / \mathrm{lb} /{ }^{\circ} \mathrm{F}$.
$\mu_{\mathrm{w}}=$ viscosity of fluid at tube wall temperature $\mathrm{lbs} / \mathrm{hr} / \mathrm{ft}^{2}$.
$\mathrm{G}=$ mass velocity $\mathrm{lbs} / \mathrm{ft}^{2} / \mathrm{hr}\left(\mathrm{kg} / \mathrm{m}^{2}-\mathrm{s}\right)$.
$\mathrm{L}=$ length of a single tube in ft.
Thus if we know the Re Number and the other fluid properties we can use Figure 9-7 in the GPSA Data Book and find $h_{i}$.
$h_{0}$ - the outside film coefficient. To find $h_{0}$ we use a similar type of equation of a slightly different form developed by Colburn ${ }^{9}$.
The form is:
Equation 8-14

$$
\frac{h_{0} D_{e}}{K}=0.36\left(\frac{D_{e} G_{s}}{\mu}\right)^{0.55}\left(\frac{C_{P} \mu}{K}\right)^{1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{0.14}
$$

where:

$$
\begin{aligned}
& \mathrm{D}_{\mathrm{e}}=\text { equivalent diameter }=\frac{4 \mathrm{x} \text { free area }}{\text { wetted perimeter }} \\
& \mathrm{G}_{\mathrm{s}}=\frac{\text { Mass Flow }}{\text { shell cross flow area }}
\end{aligned}
$$

The shell cross flow area is found at the centre of the bundle and is given by the formula:

$$
A_{s}=\frac{I D\left(C^{\prime} B\right)}{P_{T}(144)}
$$

where:
$A_{s}=$ shell cross sectional area in $\mathrm{ft}^{2}$.
$B=$ baffle spacing in inches.
$C^{\prime}=$ clearance between tubes in inches.
ID = shell ID in inches.
$\mathrm{P}_{\mathrm{T}}=$ pitch (distance between centres of tubes).

$$
J=\left(\frac{h_{o} d_{O}}{K}\right)\left(\frac{c z}{k}\right)^{-1 / 3}\left(\frac{z}{z_{w}}\right)^{-0.14}
$$



Figure 8.9: Heat Transfer for Fluid Flowing across Tube Banks
The figure below shows these symbols.


Figure 8.10: Tube Arrangement and Symbols
We then have a similar graph as for inside tubes (Figure 8.9, which is reproduced from an old edition of the GPSA Data Book. $Z$ is used as a viscosity symbol) where $j$ is plotted versus the Reynolds Number.

Equation 8-16

$$
j=\frac{h_{0} D_{0}}{K}\left(\frac{C_{P} \mu}{K}\right)^{-1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{-0.14}
$$

Probably should use De but the figure has been corrected so as to use $\mathrm{D}_{0}$, which is the outside diameter of the tube.

For Shell and Tube exchangers the GPSA Data Book has developed a slightly different method of calculating the overall "U" (see pages 8-5, 8-6 and 8-7 of the GPSA Data Book). It is based on finding the resistance for both inside and outside tubes based on a set of standard values as given in Figure 8-8 on page 8-7 of the GPSA Data Book.

For example:


Figure 8.11: Thermal Resistance of Typical Uniform Deposits

$$
r 2_{\text {TUBE SIDE NEW Condition }}=f(r 1)_{\text {TUBE SIDE Standard condition }}
$$

where:
f is for turbulent flow on the tube side.
Equation 8-17

$$
f=\left(\frac{\mu_{2}}{\mu_{1}}\right)^{0.27}\left(\frac{K_{1}}{K_{2}}\right)^{0.67}\left(\frac{C_{P 1}}{C_{P 2}}\right)^{0.33}\left(\frac{G_{1}}{G_{2}}\right)^{0.8}\left(\frac{D_{02}}{D_{01}}\right)^{0.2}
$$

A similar equation can be given for the shell side resistance. This is

$$
f=\left(\frac{\mu_{2}}{\mu_{1}}\right)^{0.27}\left(\frac{K_{1}}{K_{2}}\right)^{0.67}\left(\frac{C_{P 1}}{C_{P 2}}\right)^{0.33}\left(\frac{G_{1}}{G_{2}}\right)^{0.6}\left(\frac{D_{02}}{D_{01}}\right)^{0.4}
$$

where:

$$
r_{1}=\text { the standard value at "1". }
$$

For pressure drop a similar set of ratios is given.
Please refer to Section 8 of the GPSA Data Book for further details; particularly Fig. 8-7 and Fig. 88 give tables of all standard relationships and values. When using this method the appropriate standard fluid, i.e. water, HC oil or methane, should be used.

### 8.3.2 Fouling Resistances

## Effect of Fouling

Products of corrosion, dirt, or other foreign materials which deposit on heat transfer surfaces increase the overall thermal resistance and lower the overall heat transfer coefficient of the heat exchanger. Figure 8.10 which is from the TEMA Manual shows the effect of fouling thickness upon resistance for several types of deposits. In order that heat exchangers shall have sufficient surface to maintain satisfactory performance in normal operation, with reasonable service time between cleanings, it is important in design to provide a fouling allowance appropriate to the expected operating and maintenance conditions.

### 8.3.2.1 Considerations in Fouling Resistance Evaluation

The determination of appropriate values for fouling resistance involves both physical and economic factors, many of which vary from user to user, even for identical services.

## Physical Considerations

Among physical factors influencing the extent of heat exchanger fouling are:

- Nature of fluid and material deposited
- Temperature of fluid
- Temperature of tube wall
- Tube wall, material and finish
- Fluid velocity
- Operating time since last cleaning


## Economic Considerations

Economic factors entering into the determination of permissible extent of fouling are:

- Initial cost of exchanger
- Variation of cost with size
- Frequency of cleanings required
- Cost of cleaning, including loss of production
- Depreciation rate
- Tax rate
- Maintenance rate (exclusive of cleaning costs)
- Fluid pumping charges
- Desired net return on investment


### 8.3.2.2 Typical Fouling Resistances

The tables (given at the end of this chapter) present typical fouling resistances referred to the surface on which they occur. In the absence of specific data for setting proper resistances as described in the previous paragraphs, the user may be guided by the values tabulated on pages $43,44,45,46$. In the case of inside surface fokling these values must be multiplied by the outsideinside surface ratio. Figure 10 shows how the fouling resistance builds up with layer thickness.

A more scientific approach to fouling resistance has been proposed in two articles by Taborek, Aohi, Ritter, Palen and Knudson ${ }^{1}$. They state that the basic fouling equation is as follows.

Equation 8-18

$$
\frac{d\left(x_{f} K_{f}\right)}{d t}=\phi d-\phi r
$$

where:
$\mathrm{x}_{\mathrm{f}}=$ thickness of the fouling deposit.
$\mathrm{K}_{\mathrm{f}}=$ the effective thermal conductivity of the fouling layer.
$\Phi d=$ the rate of deposition.
$\Phi r=$ the rate of removal.
or

$$
\frac{d R f}{d t}=\frac{d\left(x_{f} K_{f}\right)}{d t}
$$

where:

$$
\frac{d R f}{d t}=\text { net rate of fouling accumulation. }
$$

Many models solving this general equation have been developed.
These are given in the Table below. Taborek, Aohi, Ritter, Palen and Knudson discuss these models in some detail and present some experimental data on specific fouling test work. This reference should be contacted for more data on fouling.

Table 8.2: Comparison of Fouling Models

| Model | Deposition Term $\boldsymbol{\Phi}_{\mathrm{d}}$ | Removal Term $\boldsymbol{\Phi}_{\mathbf{r}}$ | Characteristics of Fouling Type |
| :--- | :--- | :--- | :--- |
| Kern and Seaton | Proportional to <br> concentration of foulant. | Proportional to fouling layer <br> thickness and shear stress. | Sedimuntation. However, similar <br> trends are seen with other types. |
| Watkinson | Proportional to <br> concentration difference <br> and to Arhenius <br> temperature values. | Used same as Kern and <br> Seaton. | Reaction rate controlled or <br> diffusion rate controlled (The two <br> mechanisms were combined in an <br> attempt to fit both decomposition <br> and sedimentation data). |
| Reitzer | Proportional to <br> supersaturation to the $\mathrm{n}^{\text {th }}$ <br> power. | None. | Combination of diffusion and <br> reaction controlled. |
| Beal | Proportional to <br> concentration gradient as <br> function of tubulent and | None postulated. Assume all <br> particles reaching wall stuck. | Deposition of dust from gas. <br> However, neglecting removal <br> makes model questionable for |

[^11]|  | Brownian diffusivity. |  | high velocity and loose material. |
| :--- | :--- | :--- | :--- |

### 8.3.3 Condensers

The same equation is used for sizing condensers as heat exchangers:

$$
Q=U A \Delta T
$$

and all the parts of the equation are determined as indicated in Section A. However, the film coefficient for condensing is determined from quite a different formula for determining "ho". There are two types of condensing - dropwise of film.
Dropwise gives very high coefficient but requires special conditions. Usually film condensation is considered to take place. Generally the flow is laminar i.e. Reynolds No. is less than 2100. Also two types of situations exist as shown in Figure 8.12. In vertical tubes the flow is down the tube and accumulates as the condensate flows down the tube. In horizontal tubes it also accumulates when flow is inside and drops to the next tube when condensation is on the outside of the tubes.


Figure 8.12: Condensing Methods
The equations that can be used for calculating "h" are as follows. For vertical tubes

$$
h=0.925 K\left(\frac{g \rho_{1}^{2}}{\mu \Gamma}\right)^{1 / 3}
$$

For horizontal tubes

$$
h=0.76 K\left(\frac{g \rho_{1}^{2}}{\mu \Gamma}\right)^{1 / 3}
$$

where:
$h=$ heat transfer coefficient BTU's/hr/ft ${ }^{2} /{ }^{\circ} F$.
$K=$ thermal conductivity of liquid $B T U / h r / f t^{\circ} F$.
$\mathrm{g}=$ gravity $\left(4.18 \times 10^{6}\right) \mathrm{ft} / \mathrm{hr}^{2}$.

$$
\begin{aligned}
& \rho_{1}=\text { density of liquid } \mathrm{lbs} / \mathrm{ft}^{3} . \\
& \mu=\text { viscosity } \mathrm{lbs} / \mathrm{hr} / \mathrm{ft} . \\
& \Gamma=\text { tube loading } \mathrm{lbs} / \mathrm{hr} / \mathrm{ft} .
\end{aligned}
$$

These equations can be applied for both inside and outside tubes. The equation does assume that the flow of condensed fluid is laminar. The calculation of $\Gamma$ is particularly important. In vertical tubes it can be calculated by just dividing the flow of condensed liquid by the tube perimeter. The equation to use is

Equation 8-23

$$
\Gamma=\frac{W}{n \pi \frac{d}{12}}
$$

where:
$\mathrm{W}=$ flow lbs/hr.
$\mathrm{n}=$ number of tubes.
$\mathrm{d}=$ diameter of tubes in inches.
When flow is in horizontal tubes, "Г" may be found from

$$
\Gamma=\frac{W}{2 n L}
$$

for inside tubes
where:

$$
\mathrm{L}=\text { length of tube in feet. }
$$

For outside tubes

$$
\Gamma=\frac{W}{4 n_{r} L}
$$

where:
$n_{r}=$ no. of tubes at centre of exchanger.
Another important feature of condensers is to calculate the overall $\Delta T$. This usually has to be found from a condensing curve when a multi-component mixture is being condensed. Figure 8.12 shows a typical condensing curve for an amine still overhead condenser.


Figure 8.13: Multi-Component Condensing
The overall $\Delta T$ is found by breaking area into several sections and finding $\Delta T$ for each section and the area required for each section. The curve itself is calculated by determining amount of material that condenses at each temperature and the latent heat at that temperature.

Often in a hydrocarbon mix with only a few components the condenser entrance and exit temperatures can be found from the dew point and bubble point respectively and sometimes the log mean $\Delta T$ can be used as the average $\Delta T$.

### 8.3.4 Reboilers

In this equipment we can again use Equation (7) if only convection heat transfer is experienced. However, the calculation of " $\mathrm{h}_{0}$ " is based on a different formula and, as will be seen shortly, often the heat flux Q/A is the limiting design criteria. For boiling liquids consider the conditions shown in Figure 8.13.


Figure 8.14: Types of Boiling
Very high values of $h$ can be obtained in the boiling in the manner shown in Figure 8.14(a) but this is only for low $\Delta \mathrm{T}$. What happens is that film eventually blankets the boiling surface as shown in Figure 8.14(b). Thus $\frac{Q}{A}$ decrease for a while as $\Delta T_{\text {solid-liquid }}$ increases. This is shown in


Figure 8.15: Heat Flux in Boiling
Thus we normally design reboilers for a heat flux. Kern ${ }^{7}$ recommends the following values.
For natural circulation:
$\mathrm{Q} / \mathrm{A}<12,000 \mathrm{BTU} / \mathrm{hr} / \mathrm{ft}^{2}$ for organics ( $130,000 \mathrm{~kJ} / \mathrm{hr} / \mathrm{m}^{2}$ )
and
$\mathrm{Q} / \mathrm{A}<18,000 \mathrm{BTU} / \mathrm{hr} / \mathrm{ft}^{2}$ for water systems (194,000 kJ/ hr/ m${ }^{2}$ )
For forced circulation, in which normally partial vapourization only occurs, higher fluxes can be used.

Q/A $<20,000$ for organics ( $220,000 \mathrm{~kJ} / \mathrm{hr} / \mathrm{m}^{2}$ ) and $<30,000$ for water systems ( $330,000 \mathrm{~kJ} / \mathrm{hr} / \mathrm{m}^{2}$ ) Please refer to the English GPSA ('87) for more specific heat flux ranges; particularly on Page 9-12. Or the maximum flux can be calculated from the following equation:

Equation 8-26

$$
\left(\frac{Q}{A}\right)_{\max }=143 \rho_{V} \lambda\left(\frac{\rho_{L}-\rho_{V}}{\rho_{V}}\right)^{0.6}
$$

where:

$$
\lambda=\text { latent heat of evaporation. }
$$

$$
\rho_{\mathrm{v}}=\text { density of vapour. }
$$

$$
\rho_{\mathrm{L}}=\text { density of liquid. }
$$

The maximum temperature difference between the surface and the boiling fluid can be found from
Equation 8-27

$$
\left(t_{S}-t_{b}\right)_{\max }=\frac{1}{m}\left(\frac{Q}{A}\right)_{\max }
$$

where:
$t_{s}=$ surface temperature ${ }^{\circ} \mathrm{T}$.
$t_{b}=$ boiling temperature.
$m=a$ constant characteristic of the material being boiled. $m$ is available from article by J.R.
Fair.
This article also gives varying values of $h_{b r}$, the boiling coefficient for various materials. It is a good article on reboilers in general.
Also, h for boiling can be calculated from the following equation:
Equation 8-28

$$
\frac{h}{C_{P} G}=4.02\left(\frac{D G}{\mu}\right)^{-0.3}\left(\frac{C_{P} \mu}{K}\right)^{-0.6}\left(\frac{P_{L} \chi}{p^{2}}\right)^{-0.425} \Sigma_{L}
$$

The symbols are as given before and the units are as previously given and where:
$\gamma=$ surface tension dynes/cm.
P - = pressure psia.
$\Sigma=$ surface condition factor 1.0 for steel or copper, lower for stainless steel.
Union Carbide has developed a new tube for boiling called a porous boiling tube (See Martin).
An excellent article on the types of heat exchangers just discussed is "Design of Heat Exchangers" by R.C. Lord, P.E. Minton and R.P. Slusser.

### 8.3.5 Air Exchanaers

In air exchangers the equation (6) is used.
$\Delta \mathrm{T}$ is normally calculated for cross flow type of exchanger. The correction factor as obtained from Figures 9-3 and 9-4 in the GPSA Data Book on page 9-5 and 9-6 is used. A is usually expressed as a bare fin tube area. $U$ is calculated as previously indicated for regular exchangers, i.e.
Equation (11). The outside film coefficient for air can be found from Figure 9-9 on page 9-10 of the GPSA Data Book which plots ho versus air velocity. An air velocity of about 675 ft . per minute is often used, which is equivalent to about $3000 \mathrm{lbs} / \mathrm{hr} \mathrm{ft}^{2}\left(4 \mathrm{~kg} / \mathrm{sec} / \mathrm{m}^{2}\right)$. Detailed comparison is made of pressure drop allowed on the air side versus the required area. For finned tubes the $h$ can be found from the following equation:

Equation 8-29

$$
\frac{h d_{r}}{K_{a}(12)}=0.1378\left(\frac{d_{r} G_{m}}{12 \mu}\right)^{0.718}\left(\frac{C_{P} \mu}{K_{a}}\right)^{1 / 3}\left(\frac{S}{l}\right)^{0.296} F_{r}
$$

where:
$\mathrm{h}=$ coefficient of heat transfer for high fin tubes BTU/hr/sq ft/ ${ }^{\circ} \mathrm{F}$.
$\mathrm{K}_{\mathrm{a}}=$ thermal conductivity of air BTU/hr/sq ft/ ${ }^{\circ} \mathrm{F} / \mathrm{ft}$.
$d_{r}=$ root diameter of tube in inches.
$\mathrm{G}_{\mathrm{m}}=$ maximum flow of air at minimum area $\mathrm{lbs} / \mathrm{sec} / \mathrm{ft}^{2}$.
$\mathrm{C}_{\mathrm{p}}=$ specific heat of air (about 0.24 BTU/lb/ ${ }^{\circ} \mathrm{F}$ ).
$S=$ distance between fins in inches $S=1-n t / n$.
$\mathrm{n}=$ number of fins per inch.
$t=$ fin thickness in inches.
$\ell=$ fin height in inches $\mathrm{df}-\mathrm{dr} / 2$.
$F_{r}=$ row factor from 0.810 for two rows to 0.987 for 20 rows.
See Example problem in GPSA Data Book starting page 9-7 on sizing aerial coolers.

### 8.3.6 Furnaces

Furnaces are normally sized by the heat flux allowable $Q / A=$. This is usually set between 10,000 to $15,000 \mathrm{BTU} / \mathrm{hr} / \mathrm{ft}^{2}$, generally $15,000 \mathrm{BTU} / \mathrm{hr} / \mathrm{ft}^{2}$ in the radiant section and $10,000 \mathrm{BTU} / \mathrm{hr} / \mathrm{ft}^{2}$ overall. This varies with the tube material used and fluid being heated. Most furnaces have both a convection section and radiant section. Figure 8.6 shows a typical furnace.
About $70 \%$ of duty is in the radiant section and about $30 \%$ of the duty is in the convection section. However, area in each section is about the same, the different sections use different equations for calculating the area.
Let us first consider the radiation section. The rate of heat transfer can be calculated from the formula:

Equation 8-30

$$
Q_{R r}=\sigma \alpha A_{c p} F\left(T_{g}^{4}-T_{t}^{4}\right)
$$

where:
$Q_{R r}=$ radiant heat transfer rate in radiation section.
$\sigma=$ constant $0.173 \times 10^{-8} \mathrm{BTU} / \mathrm{hr} / \mathrm{sq} \mathrm{ft} /^{\circ} \mathrm{R}$.
$\mathrm{A}_{\mathrm{cp}}=$ cold plane surface area sq ft. (total exposed tube surface area) (tube length times center to center distance).
$\alpha=\mathrm{a}$ factor of comparison of what a tube sees in a furnace and given in Figure 8.16.
$\mathrm{T}_{\mathrm{g}}=$ the gas temperature ${ }^{\circ} \mathrm{R}$.
$T_{t}=$ the tube temperature ${ }^{\circ} \mathrm{R}$ (add $100^{\circ} \mathrm{F}$ to average fluid temperature to determine this).
$\mathrm{F}=\mathrm{an}$ exchange factor as given in Figures 8.16 and 8.17 and Figure 3 and Table 8.3.
To find this it is necessary to use "L" the beam length which is given in the next Table.
For convection in the radiant section the following equation can be used:
Equation 8-31

$$
Q_{R c}=h_{r c} A_{R T}\left(T_{g}-T_{t}\right)
$$

## Table 8.3: Beam Lengths for Gas Radiation

| Dimension Ratio | Mean Beam Length, L |
| :--- | :--- |
| Rectangular Furnaces, Length-Width-Height, (In any Order) |  |
| $1-1-1$ to $1-1-3$ | $2 / 3$ (Furnace Volume) ${ }^{1 / 3}$ |
| $1-2-1$ to $1-2-4$ | $2 / 3$ (Furnace Volume) |
| $1-1-4$ to $1-1-\infty$ | $1 \times$ Smallest Dimension |
| $1-2-5$ to $1-2-\infty$ | $1.3 \times$ Smallest Dimension |
| $1-3-3$ to $1-\infty-\infty$ | $1.8 \times$ Smallest Dimension |
| Cylindrical Furnaces, Diameter-Height |  |
| $1-1$ | $2 / 3 \times$ Diameter |
| $1-2$ to $1-\infty$ | $1 \times$ Diameter |

where:
$Q_{R C}=$ convective heat transfer rate in radiation section.
$A_{R T}=$ tube area in the radiant section.
$h_{\mathrm{rc}}=$ convective heat transfer coefficient usually about 2.0 BTU/hr/sq ft/ ${ }^{\circ} \mathrm{F}$
In the normal furnace $A_{R T}$ is about 2 times $\alpha A_{c p}$ and $F$ is often 0.57 .
$Q_{R C}$ can be expressed as
Equation 8-32

$$
Q_{R c}=7.0 \alpha A_{c p}\left(T_{g}-T_{t}\right)
$$

For the convection section the regular method of finding the overall heat transfer coefficient can be used. To calculate the outside "h" the following equation is used.

$$
h_{c c}=\frac{2.14\left(T_{f}\right)^{0.28}\left(G_{\max }\right)^{0.6}}{d^{0.4}}
$$

where:
$h_{c c}=$ convection section outside film coefficient.
$\mathrm{T}_{\mathrm{f}}=$ average outside gas temperature.
$\mathrm{G}=$ mass velocity $\mathrm{lb} / \mathrm{sq} \mathrm{ft/sec}$.
$d=$ tube OD in inches.
A good article on rating fired heaters is one by R.N. Wimpress.

### 8.4 Specifying Exchangers

Let us now consider what normally people in the gas processing business wish to do. That is, specify an exchanger to fit a heat transfer application. Let us consider shell and tube exchanger only. Air coolers can also be specified in a similar manner. What must be specified:

- Process Conditions
- Physical properties of fluid involved
- Performance conditions
- Mechanical design conditions
- Materials of construction
- Codes


### 8.4.1 Physical Properties

If it is not a well known fluid, should tell exchanger manufacturer all about fluids, i.e. actual fluid, its gravity, viscosity, thermal conductivity, specific heat, etc.

### 8.4.2 Material of Construction

Specify for fluids involved (only if special materials required).

### 8.4.3 Codes

Normally unfired pressure vessel code of Province, and TEMA division, either R or C or B . All rather similar except $B$ and $C$ allow smaller diameter tubes.

### 8.4.4 Mechanical Design Conditions

Specify tube $\Phi$ and length, normally $3 / 4$ " and either 16 or 20 ft . for $U$ bundles or gas to gas exchangers which have 40 and 50 ft . Also tube layout and pitch (clearance between tubes) should be given. Figure 8.19 below explains this.


Figure 8.16: Absorption Efficiency of the Tube-banks


Figure 8.17: Gas Emissivity


Figure 8.18: Overall Radiant Exchanger Factor


Figure 8.19: Tube Layouts

### 8.4.5 Performance Conditions

Overall heat transfer coefficient and the fouling factors. These are generally left up to exchanger supplier and checked by purchaser.
Listing in TEMA, given earlier, gives typical values for the fouling factor.

### 8.4.6 Process Conditions

This is the main part of the specifications for purchaser.

## Heat Transferred

The quantity of fluid flowing is determined from plant process balance. Heat to be transferred from process balance, but modified for temperature limits, as discussed.

## Pressure Drop

This is an economical consideration, pump capacity versus exchanger surface. (See GPSA Data Book for calculations of actual drop). Here are some guidelines:

| Exchanger |  | shell side |
| :--- | :--- | :---: |
|  | tube side | Normal Maximum Allowed |
|  | as above | 10 psi |
| Coolers | shell condensing side | 10 psi |
| Condensers | tubes, cooling side | 3 psi |
|  | shell side, boiling | 10 psi |
| Reboilers | tubes side, condensing | 1 psi |
| Chillers | same as reboilers | 1 psi |
| Air Coolers | process side as above - air side, generally set velocity of air about <br> $600-700$ ft./min. |  |

## Fluid Location

Some general rules are:
In Shell:

- Boiling liquid.
- $\quad$ Condensing liquid.
- Cleanest of two fluids.
- When no other considerations - hot fluid (handles expansion better).

In Tube:

- Dirty fluid.
- High pressure fluid.
- $\quad$ Condensing fluid when boiling a fluid.
- Corrosive fluid.
- When no other consideration - cold fluid.


## Temperatures

These may be set by process balance but there are some special considerations:
Cooling with Water - Cooling water outlet temperature is set by scaling or corrosion conditions. This should be calculated by the stability index - see pages 11-9 and 11-10 in the GPSA Data Book. When this cannot be done do not go over $120^{\circ} \mathrm{F}\left(50^{\circ} \mathrm{C}\right)$. There is also an economic balance on how much to cool with water and how to cool with other fluids.

Economic Temperature Approach - It is necessary to consider what is the economic temperature of the other fluid in an exchanger. Let us consider separate types of heat exchanger equipment:
h) Condensers - a single component condensing; condenser temperature set by pressure of system, no sub-cooling considered. Figure 8.20 below shows this.


Figure 8.20: Single Component Condensing
a) Multi-Component - Condense to within $10^{\circ} \mathrm{F}\left(5^{\circ} \mathrm{C}\right)$ of cold fluid outlet temperature. No crossovers considered. Also we need a condensing curve in this case. Generally consider enthalpy of condensing i.e. for hydrocarbons use dewpoint at entrance to exchanger and bubblepoint at exit from exchanger.
b) Water Exchangers - Can heat up water to point that scaling starts unless water is treated. This is determined by stability index (Fig. 11-9 in GPSA Data Book). If no data, maximum temperature $120^{\circ} \mathrm{F}\left(50^{\circ} \mathrm{C}\right)$
c) True Counter Current Exchangers - i.e. Gas to gas exchangers, double pipe exchangers. No problem with cross-overs here. If flow of fluids is quite different and there is a large difference in temperature at one end, approach can be brought to $10^{\circ} \mathrm{F}\left(5^{\circ} \mathrm{C}\right)$ at other end.
d) Cross Flow Exchangers - Consider the flow in the exchanger shown in Figure 8.21.


Figure 8.21: Crossflow Exchanger without Baffle
Without internal shell baffling $T_{2}$ could not be less than $t_{2}$ as there would be reverse of heat flow. If horizontal baffling is used we now have better counter flow as shown in Figure 8.22.


Figure 8.22: Crossflow Exchanger with Baffle
$\mathrm{T}_{2}$ can be less than $\mathrm{t}_{2}$. However you should be careful. Try to limit cross-over to less than $20^{\circ} \mathrm{F}$ $\left(11^{\circ} \mathrm{C}\right)$ in a single shell.
e) Reboilers, Chillers - If one fluid is at constant temperature and the other is varied, i.e. chillers, steam heaters, etc., use $10^{\circ} \mathrm{F}\left(5^{\circ} \mathrm{C}\right)$ approach as shown in Figure 8.23.


Figure 8.23: Chiller Temperature Curve

### 8.5 Heat Transfer to Buried Pipelines

The problem of designing systems such as heater or hot water tracing systems is actually calculating the loss of heat from the buried pipe and making sure the liquid flowing through it does not cool to a temperature below the hydrate formation temperature of the fluid. The length of line that can be used before reheating or how much the gas has to be heated can be calculated from the following equations (34) and (35).

$$
Q=U A \frac{\left(T_{1}-t\right)-\left(T_{2}-t\right)}{\ln \frac{T_{1}-t}{T_{2}-t}}
$$

where:
$\mathrm{U}=$ the overall heat transfer coefficient for transfer from buried pipes to the ground.
A = area of transfer, i.e. pipe perimeter times its length.
$\mathrm{T}_{1}=$ the initial gas temperature.
$T_{2}=$ the final gas temperature. The final temperature is some temperature above hydrate point (usually about $5^{\circ} \mathrm{F}$ ).
$Q=$ the rate of heat transfer at steady flow rates BTU's/hr.
$\mathrm{t}=$ the ground temperature.
and

$$
Q=W C_{P}\left(T_{1}-T_{2}\right)
$$

or using enthalpies as $C p$ are not readily available $=W\left(H_{1}-H_{2}\right)$

$$
Q=W\left(H_{1}-H_{2}\right)
$$

where:
$\mathrm{W}=$ the rate of flow, lbs/hr.
$\mathrm{Cp}=$ the specific heat of gas.
$\mathrm{T}_{1}=$ as previously —initial gas temperature.
$\mathrm{T}_{2}=$ as previously - final gas temperature.
$\mathrm{H}_{1}=$ enthalpy of material at initial gas temperature.
$\mathrm{H}_{2}=$ enthalpy of material at final gas temperature.
The overall heat transfer coefficient, U's value, varies considerably with the soil conditions. The table below gives some experimentally determined values.

Table 8.4: Overall Heat Transfer to Ground

| Soil | $\mathbf{B T U} / \mathbf{h r} / \mathrm{ft}^{2} /{ }^{\circ} \mathbf{F}$ | $\mathbf{( \mathbf { W } / \mathbf { m } ^ { 2 } / { } ^ { \circ } \mathbf { C } )}$ |
| :--- | :--- | :--- |
| Clay and gravel | 0.618 | $(3.51)$ |
| Shale and muskeg mix | 0.500 | $(2.84)$ |
| Muskeg | 0.400 (after system <br> stabilized and muskeg <br> around pipe dried) | $(2.27)$ |
|  | 2.000 (Wet) | $(11.30)$ |
| Silty gravel | 0.600 | $(3.41)$ |
| Wet soil | 1.500 | $(8.52)$ |

A good design value is $0.65 \mathrm{BTU} / \mathrm{hr}^{2} / \mathrm{ft}^{2} /{ }^{\circ} \mathrm{F}\left(3.69 \mathrm{~W} / \mathrm{m}^{2} /{ }^{\circ} \mathrm{C}\right)$.
If insulated pipe is used a design value of $0.15 \mathrm{BTU} / \mathrm{hr} / \mathrm{ft}^{2} /{ }^{\circ} \mathrm{F}$
( $0.85 \mathrm{~W} / \mathrm{m} / \mathrm{ft}$ ) for overall heat transfer coefficient can be used. Field tests show that the actual values generally run a little lower than this (down to 0.10 ).

## Example Problem 8.1

Calculate the area required for a rich to lean amine exchanger that is to heat the rich amine from $140^{\circ} \mathrm{F}$ to $210^{\circ} \mathrm{F}$ using lean amine at $255^{\circ} \mathrm{F}$. The rich amine flow is 1700 US gpm and the lean amine flow is 1600 US gpm. For simplification assume the properties of rich and lean amine are the same, i.e. the specific gravity of the amine solution is 1.020 and the specific heat at average conditions for both products is 0.95 .

1. Find outlet temperature of lean amine.

$$
\begin{aligned}
& 1700(8.33)(1.020)(60)(.95)(210-140) \\
& =1600(8.33)(1.020)(60)(.95)(255-t) \\
& t=181^{\circ} \mathrm{F}
\end{aligned}
$$

2. Find the $\log$ mean temperature

$$
\Delta T=\frac{(255-210)-(181-140)}{\ln \frac{45}{41}}=43
$$

7. Find the heat duty (amount of heat to be transferred).

$$
Q=1700(8.33)(1.020)(60)(0.95)(210-140)=57,000,000 \mathrm{BTU}
$$

8. Find the area required

$$
Q=U A \Delta T
$$

$$
\mathrm{A}=\mathrm{Q} / \mathrm{U} \Delta \mathrm{~T}
$$

Now U from NGPSA book Figure 8-6 on page 8-5 = 130.

$$
\begin{aligned}
A & =\frac{57,000,000}{130(43)} \\
& =10,200 \mathrm{ft}^{2}
\end{aligned}
$$

Next let us go through a more detailed rating for this how this area would be determined in actual practice. Here are some additional design conditions:

Allowable pressure drop, tube side 10 psi
Allowable pressure drop, shell side 10 psi
We will plan to use an exchanger with $3 / 4 "$ OD tubes 20 ft . long, 14 BWG on a 1 " square pitch. The shell baffles will be spaced every 12". To illustrate the calculations we will used a 2 shell pass, 4 tube pass exchanger. Some additional physical properties of the amines are:

|  | Lean Amine Shell Side | Rich Amine Tube Side |
| :--- | :--- | :--- |
| $\mu$ (viscosity in cp ) | 0.38 | 0.5 |
| K (thermal cond.) $\mathrm{BTU} / \mathrm{hr} / \mathrm{ft}^{2} /{ }^{\circ} \mathrm{F} / \mathrm{ft}$ | 0.312 | 0.312 |

The assumed overall fouling factor will be 0.0030 .
The method of solution is to assume a number of tubes and thus the area, then find the overall heat transfer coefficient using the assumed number of tubes and then calculate the new area and see if this comes close to the assumed area. The overall coefficient $U$ is found from the equation:

$$
\frac{1}{U}=\frac{1}{h_{0}}+\frac{1}{h_{i}} \frac{D_{0}}{D_{i}}+R
$$

$h_{o}$ and $h_{i}$ are found from the curves on Fig. 8 and Fig. 9-7 of the GPSA Data Book. These curves are based on the Sieder and Tate equation inside tubes:

$$
\frac{h_{i} D_{i}}{K}=0.027\left(\frac{D G}{\mu}\right)^{0.8}\left(\frac{C_{P} \mu}{K}\right)^{1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{0.14}
$$

and by the Colburn equation for outside tubes:

$$
\frac{H_{0} D_{e}}{K}=0.36\left(\frac{D_{e} G}{\mu}\right)^{0.55}\left(\frac{C_{P} \mu}{K}\right)^{1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{0.14}
$$

These equations apply only over the turbulent flow range. Please note that the common symbols have been used above. In the GPSA Data Book slightly different symbols are used. Since we have a 2-4 exchanger we must correct the log mean temperature difference. This is done using the Figure 8-3 on page 8-3 of the GPSA Data Book.

$$
\begin{aligned}
& P=\frac{210-140}{255-140}=0.608 \\
& R=\frac{255-181}{210-140}=1.051 \\
& \Delta T=F \Delta T_{\text {LOG MEAN }}=0.89(43)=38^{\circ} F
\end{aligned}
$$

For a first try let us assume 700 tubes per pass. This gives an area of heat transfer of

$$
700(0.1963)(4)(20)=11,000 \mathrm{ft}^{2}
$$

Let us first find $h_{i}$

$$
G=\frac{1700(8.33)(1.02)(60)}{700 \frac{0.2679}{144}}=182 \mathrm{lb} / \mathrm{sec} . f t^{2}
$$

G is the mass velocity
Now use Figure 9-7 in the GPSA Data Book.

$$
\begin{aligned}
& N_{R}=\frac{D V}{Z}=\frac{0.584(182)}{0.5}=213 \\
& J_{1}=1400 \text { from curve } \\
& 1400=\left(\frac{h_{i} D_{i}}{K}\right)\left(\frac{C Z}{K}\right)^{-1 / 3} \frac{Z}{Z_{W}}
\end{aligned}
$$

Ignore viscosity correction $\left(\frac{z}{z_{W}}\right)^{0.14}$

$$
\frac{C Z}{K}=\frac{0.95(0.5)}{0.312}=1.52
$$

Solve for $h_{i}$

$$
1400=\frac{h_{i}(0.584)}{0.312} \frac{1}{1.15}
$$

$$
h_{i}=852
$$

Let us try the new method given in the GPSA Data Book in Section 8 of that manual. Let us for example calculate $h_{i}$. Use water as reference fluid.

$$
\begin{aligned}
& r 2=f r 1=f(0.0009) \\
& f=\left(\frac{\mu_{2}}{\mu_{1}}\right)^{0.47}\left(\frac{K_{1}}{K_{2}}\right)^{0.67}\left(\frac{C_{P 1}}{C_{P 2}}\right)^{0.33}\left(\frac{G_{1}}{G_{2}}\right)^{0.8}\left(\frac{D_{i 2}}{D_{i 1}}\right)^{0.2} \\
& \left(\frac{\mu_{2}}{\mu_{1}}\right)^{0.47}=\left(\frac{0.5}{0.764}\right)^{0.47}=0.819
\end{aligned}
$$

$$
\begin{aligned}
& \left(\frac{K_{1}}{K_{2}}\right)^{0.67}=\left(\frac{0.358}{0.312}\right)^{0.67}=1.09 \\
& \left(\frac{C_{P 1}}{C_{P 2}}\right)^{0.33}=\left(\frac{1.0}{0.95}\right)^{0.33}=1.016 \\
& \left(\frac{G_{1}}{G_{2}}\right)^{0.8}=\left(\frac{265}{182}\right)^{0.8}=1.35 \\
& \left(\frac{D_{i 2}}{D_{i 1}}\right)^{0.2}=\left(\frac{0.62}{62}\right)^{0.2}=1.0 \\
& r 2=0.819(1.09)(1.016)(1.35)(0.0009)=0.0011 \\
& h_{i}=\frac{1}{r}=908
\end{aligned}
$$

This checks close enough with previous values of $h_{i}=852$.
Next let us find $h_{o}$. First must find $G_{m}$ across tubes. Find cross sectional area across which flow occurs.

$$
a_{S}=\frac{(\text { Shell ID })(\text { Opening between tubes })(\text { BaffleSpacing })}{\text { Pitch }(144)}
$$

Let us assume a 60" shell ID (This is actually obtained by a tube count).

$$
a_{S}=\frac{60(1 / 4)(12)}{1(144)}=1.25
$$

Ignore longitudinal flow. Then

$$
G_{m}=\frac{1600(8.33)(1.02)}{60(1.25)}=181 \quad \mathrm{lbs} / \mathrm{sec} . f t^{2}
$$

Find $\mathrm{h}_{\mathrm{O}}$ from Figure 8.8 in this section

$$
\begin{aligned}
& N_{S}=\frac{D_{0} G_{m}}{Z}=\frac{0.75(181)}{0.38}=356 \\
& J_{0}=1800=\frac{h_{0} D_{0}}{K}\left(\frac{C Z}{K}\right)^{-1 / 3} \\
& \frac{C Z}{K}=\frac{0.95(0.38)}{0.312}=1.15 \\
& h_{0}=\frac{1800(0.312)}{0.75(1.15)}=715
\end{aligned}
$$

We can now find $U$ from the equation:

$$
\frac{1}{U}=\frac{1}{h_{0}}+\frac{1}{h_{i}} \frac{D_{0}}{D_{i}}+R=\frac{1}{715}+\frac{1}{852}(1.284)+0.0030=0.0057
$$

So U=170
Now check again using 500 tubes. This gives an area for heat transfer of 500(0.1963)(4)(20) = 7850.

Find new $h_{i}$. Find new $G_{m}$ and new $J_{i}$ factor ( 600 in this case)

$$
h_{i}=974
$$

Similarly find $h_{0}$. We have assumed a much smaller shell.
Find $j_{o}=2000$ and $h_{o}=878$.

$$
\begin{aligned}
& \frac{1}{U}=\frac{1}{878}+\frac{1}{874}(1.284)+0.0030=0.0054 \\
& \text { So } U=185 \\
& \text { Area }=\frac{57,000,000}{184(38)}=8160 \mathrm{ft}^{2}
\end{aligned}
$$

This is close enough. You should now check pressure drop in shell and tubes. We will find it is OK.

Table 8.5: Fouling Factors

| Fouling Resistances for Water |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Temperature of Heating Medium | Up to $240^{\circ} \mathrm{F}$ |  | $240{ }^{\circ} \mathrm{F}-400^{\circ} \mathrm{F}^{*}$ |  |
| Temperature of Water | $125^{\circ}$ For Less |  | Over $125^{\circ} \mathrm{F}$ |  |
|  | Water Velocity Ft./Sec. |  | Water Velocity Ft./Sec. |  |
| Types of Water | 3 Ft. And Less | Over 3 Ft. | 3 Ft. And Less | Over 3 Ft . |
| Sea Water | . 005 | . 001 | . 001 | . 001 |
| Brackish Water | . 002 | . 001 | . 003 | . 002 |
| Cooling Tower and Artificial Spray Pond |  |  |  |  |
| Treated Makeup | . 001 | . 001 | . 002 | . 002 |
| Untreated | . 003 | . 003 | . 005 | . 004 |
| City of Well Water (i.e. Great Lakes) | . 001 | . 001 | . 002 | . 002 |
| Great Lakes | . 001 | . 001 | . 002 | . 002 |
| River Water |  |  |  |  |
| Minimum | . 002 | . 001 | . 003 | . 002 |
| Mississippi | . 003 | . 002 | . 004 | . 003 |
| Delaware, Schuylkill | . 003 | . 002 | . 004 | . 003 |
| East River and New York Bay | . 003 | . 002 | . 004 | . 003 |
| Chicago Sanitary Canal | . 008 | . 006 | . 010 | . 008 |


| Muddy or Silty | .003 | .002 | .004 | .003 |
| :--- | :--- | :--- | :--- | :--- |
| Hard (Over 15 grains/gal.) | .003 | .003 | .005 | .005 |
| Engine Jacket | .001 | .001 | .001 | .001 |
| Distilled | .0005 | .0005 | .0005 | .0005 |
| Treated Boiler Feedwater | .001 | .0005 | .001 | .001 |
| Boiler Blowdown | .002 | .002 | .002 | .002 |

* Ratings in columns 3 and 4 are based on a temperature of the heating medium of $240^{\circ}-400^{\circ} \mathrm{F}$. If the heating medium temperature is over $400^{\circ} \mathrm{F}$ and the cooling medium is known to scale, these ratings should be modified accordingly.

| Fouling Resistances for Industrial Fluids |  |
| :---: | :---: |
| Oils |  |
| Fuel Oil | . 005 |
| Transformer Oil | . 001 |
| Engine Lube Oil | . 001 |
| Quench Oil | . 004 |
| Gases and Vapors |  |
| Manufactured Gas | . 01 |
| Engine Exhaust Gas | . 01 |
| Steam (nonoil bearing) | . 0005 |
| Exhaust Steam (oil bearing) | . 001 |
| Refrigerant Vapors | . 002 |
| Compressed Air | . 002 |
| Industrial Organic Heat Transfer Media | . 001 |
| Liquids |  |
| Refrigerant | . 001 |
| Hydraulic Fluid | . 001 |
| Industrial Organic Heat Transfer Media | . 001 |
| Molten Heat Transfer Salts | . 0005 |
| Fouling Resistances for Chemical Processing Streams |  |
| Gases and Vapors |  |
| Acid Gas | . 001 |
| Solvent Vapors | . 001 |
| Stable Overhead Products | . 001 |
| Liquids |  |
| MBA \& DEA Solutions | . 002 |
| DEG \& TEG Solutions | . 002 |
| Stable Side Draw and Bottom Product | . 001 |
| Caustic Solutions | . 002 |
| Vegetable Oils | . 003 |
| Fouling Resistances for Natural Gas-Gasoline Processing Streams |  |
| Gases and Vapors |  |


| Natural Gas |  |  |  | . 001 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Overhead Products |  |  |  | . 001 |  |  |
| Liquids |  |  |  |  |  |  |
| Lean Oil |  |  |  | . 002 |  |  |
| Rich Oil |  |  |  | . 001 |  |  |
| Natural Gasoline \& Liquefied Petroleum Gases |  |  |  | . 001 |  |  |
| Fouling Resistances for Oil Reginery Streams |  |  |  |  |  |  |
| Crude \& Vacuum Unit Gases and Vapors |  |  |  |  |  |  |
| Atmospheric Tower Overhead Vapors Light Naphthas |  |  |  | . 001 |  |  |
| Vacuum Overhead Vapors |  |  |  | . 002 |  |  |
| Crude \& Vacuum Liquids |  |  |  |  |  |  |
| Crude Oil | $0^{\circ} \mathrm{F}-199^{\circ} \mathrm{F}$ |  |  | $200^{\circ} \mathrm{F}-299^{\circ} \mathrm{F}$ |  |  |
|  | Velocity Ft./Sec. |  |  | Velocity Ft./Sec. |  |  |
|  | Under 2 Ft. | 2-4 Ft. | 4 Ft . and Over | Under 2 Ft . | 2-4 Ft. | 4 Ft . and Over |
| Dry | . 003 | . 002 | . 002 | . 003 | . 002 | . 002 |
| Salt * | . 003 | . 002 | . 002 | . 005 | . 004 | . 004 |
|  | $300^{\circ} \mathrm{F}-499^{\circ} \mathrm{F}$ |  |  | $500^{\circ} \mathrm{F}$ and Over |  |  |
|  | Velocity Ft./Sec. |  |  | Velocity Ft./Sec. |  |  |
|  | Under 2 Ft. | 2-4 Ft. | 4 Ft . and Over | Under 2 Ft . | 2-4 Ft. | 4 Ft . and Over |
| Dry | . 004 | . 003 | . 002 | . 005 | . 004 | . 003 |
| Salt * | . 006 | . 005 | . 004 | . 007 | . 006 | . 005 |

* Normally desalted below this temperature range. (Asterisk to apply to $200^{\circ} \mathrm{F}-299^{\circ} \mathrm{F}, 300^{\circ} \mathrm{F}-499^{\circ} \mathrm{F}$, $500^{\circ} \mathrm{F}$ and over).

| Gasoline | .001 |
| :--- | :--- |
| Naptha \& Light Distillates | .001 |
| Kerosene | .001 |
| Light Gas Oil | .002 |
| Heavy Gas Oil | .003 |
| Heavy Fuel Oils | .005 |
| Asphalt \& Residuum | .010 |
| Cracking \& Coking Unit Streams | .002 |
| Overhead Vapors | .002 |
| Light Cycle Oil | .003 |
| Heavy Cycle Oil | .003 |
| Light Coker Gas Oil | .004 |
| Heavy Coker Gas Oil | .003 |
| Bottoms Slurry Oil (4½ ft./sec. minimum) | .002 |
| Light Liquid Products |  |
| Cataly |  |


| Catalytic Reforming, Hydrocracking \& Hydrodesulfurization Streams |  |
| :--- | :--- |
| Reformer Charge | .002 |
| Reformer Effluent | .001 |


| Hydrocracker Charge \& Effluent ** | .002 |
| :--- | :--- |
| Recycle Gas | .001 |
| Hydrodesulfurization Charge \& Effluent ${ }^{* *}$ | .002 |
| Overhead Vapors | .001 |
| Liquid Product over $50^{\circ}$ A.P.I. | .001 |
| Liquid Product $30^{\circ}-50^{\circ}$ A.P.I. | .002 |

** Depending on charge characteristics and storage history, charge resistance may be many times this value.

| Light Ends Processing Streams |  |
| :--- | :--- |
| Overhead Vapors \& Gases | .001 |
| Liquid Products | .001 |
| Absorption Oils | .002 |
| Alkylation Trace Acid Streams | .002 |
| Reboiler Streams | .003 |

### 8.6 Example Problems

## Example Problem 8.2

The following mix is the feed to a substitute gas plant. It is supplied to the plant as a liquid at $20,000 \mathrm{BPD}$, at 500 psia and saturated.

| Comp. | Mole \% |
| :---: | :---: |
| $\mathrm{C}_{2}$ | 20.5 |
| $\mathrm{C}_{3}$ | 10.5 |
| $\mathrm{iC}_{4}$ | 8.5 |
| $\mathrm{nC}_{4}$ | 11.5 |
| $\mathrm{iC}_{5}$ | 13.6 |
| $\mathrm{nC}_{5}$ | 14.3 |
| $\mathrm{C}_{6+}$ | 21.1 |

It is necessary to vaporize the mix so that it can be fed to a desulphurize reactor which operates only in the vapour phase.
It is planned to use the convection section of a fired heater for this service. The flue gas will enter the convection section at $900^{\circ} \mathrm{F}$ and exit at $450^{\circ} \mathrm{F}$.
Determine the amount of square feet of convection section heat transfer surface required. Assume 2"00 bare schedule 80 pipe is used.

## Assumptions:

a) hc for inside tubes $=120$.
b) ho outside tubes $=50$.
c) Use a Pk of 2,000 for any calculations.
d) Flow is single pass in the convection hydrocarbon section.
e) Use fouling factors .001 for both sides.

## Example Problem 8.3

Determine the square feet of condensing surface required for totally condensing the following mixture from the top of a depentanizer.

| Comp. | Mole \% |
| :--- | :---: |
| $\mathrm{nC}_{4}$ | 5.0 |
| $\mathrm{iC}_{5}$ | 35.5 |
| $\mathrm{nC}_{5}$ | 45.0 |
| $\mathrm{C}_{6+}$ | 14.5 |

The condenser duty is $30,000,000 \mathrm{BTU}$ 's/hr.
The condensing film heat transfer coefficient is $225 \mathrm{BTU} \mathrm{s} / \mathrm{hr} \mathrm{ft}{ }^{2}{ }^{\circ} \mathrm{F}$. Water from the Bow River is to be used. Assume that this water has a minimum fouling factor for river water. The water design inlet temperature is $60^{\circ} \mathrm{F}$ and the outlet temperature is $90^{\circ} \mathrm{F}$.
The condenser operates at 100 psia.
The tubes used in the condenser are $3 / 4$ ", i.e. 0.75 " OD and 0.584 "ID.
The heat transfer coefficient for turbulent water flow is 25020 BTU 's $/ \mathrm{hr}^{\mathrm{ft}}{ }^{2}{ }^{\circ} \mathrm{F}$.

## Example Problem 8.4

You are to determine the area of the convection tubes in a furnace in which the fluid in the tubes is Boiler feed water feeding a boiler that produces steam at 195 psia. The water is fed to convection section at $200^{\circ} \mathrm{F}$ and 205 psia . The specific heat of liquid water in range under consideration is 0.88 BTU/lb/ ${ }^{\circ} F$.
The flue gases enter the convection section at $1500^{\circ} \mathrm{F}$ and leave at $500^{\circ} \mathrm{F}$. The furnace has a duty of $10,000,000$ BTU's/hr input. The furnace is $80 \%$ efficient assuming fuel is measured as net heating value. Also assume the fuel is pure methane and is fired with $20 \%$ excess air.
Data:
a) The specific heat of flue gas is $0.3 \mathrm{BTU} / \mathrm{lb} /{ }^{\circ} \mathrm{F}$
b) The flow of Boiler feed water is 15 USGM measured at $60^{\circ} \mathrm{F}$.
c) The overall "U" for heat transfer is $20 \mathrm{BTU} \mathrm{s} / \mathrm{hr} / \mathrm{ft}^{2}$ of bare tube surface.

## Example Problem 8.5

You are to design the heat exchange system for a simple absorption oil system. The sketch below shows the system without the heat exchangers.


The lean oil is a $140 \mathrm{MW}, 700 \mathrm{API}$ oil and is circulated at the rate of 250 US gpm. Gas of the composition given below flows at a rate of 200 MMSCFD to the absorber.

| Comp. | Mole \% |
| :--- | :---: |
| $\mathrm{C}_{1}$ | 84.0 |
| $\mathrm{C}_{2}$ | 7.8 |
| $\mathrm{C}_{3}$ | 2.2 |
| $\mathrm{iC}_{4}$ | 0.6 |
| $\mathrm{nC}_{4}$ | 1.0 |
| $\mathrm{iC}_{5}$ | 1.2 |
| $\mathrm{nC}_{5}$ | 1.8 |

Assume the following overall heat transfer coefficients.

|  |  | BTU/ft/sq.ft. $/{ }^{\circ}$ F |
| :--- | :--- | :--- |
| Lean Oil | Rich Oil | 80 |
| Lean Oil | Propane Refrigerant | 110 |
| Lean Oil | Cooling Water | 100 |
| Rich Oil | Exhaust Steam | 130 |
| Rich Oil | Fired Heater | 80 * (assumed "U") |

Assume Firebox equivalent temperature of $1000^{\circ} \mathrm{F}$.
The cooling water available is at $60^{\circ} \mathrm{F}$ and can be raised to $90^{\circ} \mathrm{F}$ in the exchanger. The exhaust steam available is 55 psig and saturated.
Assume the following costs for exchangers (installed).

|  |  | $/$ ft $^{2}$ of surface |
| :--- | :--- | :--- |
| Lean Oil | Rich Oil | 8 |
| Lean Oil | Propane | 10 |
| Lean Oil | Water | 7 |
| Rich Oil | Exhaust Steam | 6 |
| Rich Oil | Fired Heater | 30 |

Determine the exchangers to use in the circuit by the minimum installed costs for exchangers.

For any calculations using "K" assume a Pk of 4000 and if needed assume lean oil has same "K" as decane. For simplification, assume that the specific heat of lean oil over the whole range of temperature is $0.60 \mathrm{BTU} / \mathrm{HR} / \mathrm{LB}$ and the specific heat of rich oil over the whole range of temperature and process conditions $0.65 \mathrm{BTU} / \mathrm{LB} / \mathrm{HR}$.
Assume that $5 \mathrm{wt} \%$ of the rich oil flashes when passing through the let down valve from the absorber and that the heat of flashing is $100 \mathrm{BTU} / \mathrm{LB}$.
Also assume an $80 \% C^{3}$ absorption and essentially $100 C_{4+}$ absorption.

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### 9.0 Chemical Kinetics

- A review of the types of reactions.
- A preliminary discussion of the design of reaction vessels for chemical reactions.


### 9.1 Introduction

In handling natural gas and its associated products we are concerned with physical laws for the most part. Occasionally, however, there are chemical reactions taking place and in order to deal with these a knowledge of the chemical kinetics of the system is necessary. Chemical kinetics is a study of the rates and mechanisms of reactions.
Good examples of reactions in which chemical kinetics should be considered are the reactions involved in the production of sulphur. In the recovery of this product it is necessary to burn the $\mathrm{H}_{2} \mathrm{~S}$ in the acid gases from the sweetening unit to form $\mathrm{SO}_{2}$ and to react the $\mathrm{SO}_{2}$ with the remaining $\mathrm{H}_{2} \mathrm{~S}$ to form elemental sulphur. The simplified equations representing this process are:

Equation 9-1

$$
\mathrm{H}_{2} \mathrm{~S}+\frac{3}{2} \mathrm{O}_{2}+\mathrm{SO}_{2}+\mathrm{H}_{2} \mathrm{O}
$$

Equation 9-2

$$
\mathrm{SO}_{2}+2 \mathrm{H}_{2} \mathrm{~S}+3 \mathrm{~S}+2 \mathrm{H}_{2} \mathrm{O}
$$

To get a better understanding of how this process works and how to design the reactor in which these reactions occur, a study of the chemical reactions and the rates at which they occur is necessary.

### 9.2 Chemical Reactions

Let's generalize and consider some simple chemical reactions. For example:
Equation 9-3

$$
A+B \Leftrightarrow C+D
$$

The arrows here indicate a state of dynamic equilibrium. The reaction is said to be at equilibrium when the rate of forward reaction

Equation 9-4

$$
A+B \Rightarrow C+D
$$

is occurring at the same rate as the reverse action

$$
C+D \Rightarrow A+B
$$

The law of Mass Action states that the rate of a chemical reaction is proportional to the molecular concentrations of the reactants with each concentration raised to power equal to the number of molecules of each species participating in the process.

Applying this law to the above elementary reaction one may write:
Equation 9-6

$$
\text { Rate }(\text { forward })=k_{1}[A][B]
$$

and

$$
\text { Rate }(\text { reverse })=k_{2}[C][D]
$$

When the rate of the forward reaction equals the rate of the reverse reaction, dynamic equilibrium (i.e. the reactions continue) is achieved. Therefore

Equation 9-8

$$
k_{1}[A][B]=k_{2}[C][D]
$$

or

$$
\frac{k_{1}}{k_{2}}=K_{\text {equilibrium }}=\frac{[C][D]}{[A][B]}
$$

The expression for the equilibrium constant K is normally written with the concentrations of the products in the numerator and those of the reactants in the denominator. The square bracket [ ] stands for "concentration of". In the equilibrium expression developed above the quantities in the square brackets are given in molar concentrations. In the C.G.S. system the units are gm.moles/litre while in the British Engineering units they are lb.moles/cubic foot.
If during a reaction one of the products is removed from the system, the rate of the reverse reaction is reduced because of the lower concentration of this material in the rate equation. As a result the forward reaction continues until all of the reactants are consumed.

This may happen if a product is a precipitate which settles out of solution or if a gas forms which boils out of a liquid.

For example, the following reaction goes to completion in an aqueous solution.
Equation 9-10

$$
\mathrm{NaCl}+\mathrm{AgNO}_{3} \rightarrow \mathrm{AgCl} \downarrow+\mathrm{NaNO}_{3}
$$

A reaction also could be in the gaseous state and from which one of the products is readily condensed and removed from the reaction. This happens in the case of sulphur production. Sulphur condenses out and the reaction tends towards completion. To determine whether a reaction will go under certain conditions we need to determine the free energy of each of the reactants and products under the proposed reaction conditions. From these values one can determine the change in free energy $\Delta \mathrm{F}$.
$\Delta \mathrm{F}=$ the sum of Free Energies of the Products - the sum of Free Energies of the reactants.
By thermodynamics it is known that
Equation 9-11

$$
\Delta F=-R T \ln K_{\text {equilibrium }}
$$

If the $\Delta \mathrm{F}$ for the reaction is larger in a negative sense, it means that $\mathrm{K}_{\text {equilibrium }}$ will be large. Since the products are in the numerator of the expression, this means that the reaction will go strongly to completion and is likely to be a good commercial reaction. If the value of $\mathrm{K}_{\text {equilibrium }}$ turns out to be very small, it means that the reaction has little tendency to go to give products and may have little chance of commercial success.

### 9.3 Catalysis

A catalyst may be defined as (a) a substance which causes a reaction to go under conditions at which it may not go in the absence of a catalyst or (b) a substance which increases the rate but is not consumed by the reaction. Many different catalysts are used in industry. Examples of a number of reactions which occur in the presence of catalysts are:

1. In the formation of $\mathrm{SO}_{3}$ from $\mathrm{SO}_{2}$ in air, $\mathrm{V}_{2} \mathrm{O}_{5}$ is used as a catalyst.

Equation 9-12

$$
\mathrm{SO}_{2}+1 / 2 \mathrm{O}_{2} \rightarrow\left(\frac{\mathrm{~V}_{2} \mathrm{O}_{5}}{450^{\circ} \mathrm{C}}\right) \rightarrow \quad \mathrm{SO}_{3}
$$

This reaction may be followed by hydration to yield sulphuric acid.
2. In the cracking of heavy hydrocarbons of petroleum, lighter gasoline components are products. In this reaction natural clays and synthetic zeolites are used as catalysts.
3. In the alkylation of isobutylene with isobutane, HF is used as an acid catalyst.
4. In the production of sulphur as given by equation (2) Bauxite is the catalyst mostly used.

There are many other examples.
The function of a catalyst is either (a) to increase the rate of a chemical reaction or (b) to increase a particular reaction to proceed in preference to another. Both of these alternatives may occur. The mechanism of catalytic action is generally quite complex. However, in most gaseous reactions the catalyst is an adsorbent of one or more of the reactants and provides a site on which the reaction may take place. For gaseous catalytic reactions to occur, the following steps take place:

1. Diffusion of the reactant to the surface of the catalyst.
2. Diffusion into the pores of the catalyst.
3. Adsorption of reactants onto the surface.
4. Chemical reaction on the surface.
5. Desorption of the product from the surface.
6. Diffusion of the products out of the pores.
7. Diffusion from the exterior of the catalyst into the gas stream.

Any one of these steps may actually control the catalytic rate. It is thought that the catalyst permits the reaction to go more easily by permitting intermediate complexes to form which have lower "energy of activation" that is observed when the reaction is performed in the absence of a catalyst. To understand "energy of activation" let us consider the following energy diagrams which describe what happens when (a) exothermic and (b) endothermic reactions occur (Figure 9.1 and Figure 9.2).

The energy of activation is always positive and must be supplied to the reactant molecules before they can form the intermediate complex which can then decompose to yield the products.

The effect of a catalyst on a reaction is to reduce the height of the activation energy peak and thereby to permit the reaction to occur at lower temperatures. The effect of a catalyst can be seen in Figure 9.3.


Figure 9.1: Exothermic Reaction


Figure 9.2: Endothermic Reaction


Figure 9.3: Effect of Catalyst on Reaction Rate
Figure 9.3 is for a reaction in which the equilibrium constant becomes less favorable as the temperature is increased.

### 9.4 Reaction Rates

Reaction rate is equal to the change in the concentration of a reactant or product with time.

$$
\text { Rate }=\frac{d c}{d t}
$$

The rate is affected by (a) the concentration of the reactants, (b) the temperature, (c) the presence of catalysts and sometimes (d) diffusional or mass transfer processes.

### 9.4.1 Classification of Reactions



### 9.4.2 The Order of a Reaction

Consider the rate equation in which " r " is the rate

$$
r=k C_{A}^{a} C_{B}^{b}
$$

$\mathrm{C}_{\mathrm{A}}$ and $\mathrm{C}_{\mathrm{B}}$ are the concentrations of the reactants A and B . The power "a" and "b" give the order of the reaction with respect to $A$ and $B$. The "overall order" of the reaction $=a+b$. The proportionality constant " $k$ " is also known as the "specific rate constant".
If the reaction goes as indicated by the equation
Equation 9-15

$$
a A+b B \rightarrow \text { products }
$$

that is, if it is "elementary", then the powers "a" and "b" are the coefficients of $A$ and $B$ in the equation. If the reaction does not occur as this equation suggests, then the powers "a"and "b" need not be the same as the coefficients of the stoichiometric equation.

In order to determine the values of "a" and "b" in the kinetic rate expression, experimental work is required. Plots of some function of the concentration of the reactants are made versus time until a mathematical model is obtained which fits the data in the form of a straight line.
The order of a reaction may be $0,1,2,3$ or fractional. Consider the equation
Equation 9-16

$$
A \rightarrow R+S
$$

where:

$$
\text { rate "r" }=k C_{A}
$$

or
Equation 9-17

$$
\frac{-d C_{A}}{d t}=k C_{A}
$$

Here the negative sign means that the concentration of $\mathrm{C}_{\mathrm{A}}$ is decreasing as the time "t" increases.
If one plots $C_{A}$ versus "t" a curve as indicated in the sketch is obtained (Figure 9.4).
Such a curve does not reveal much. However, if the equation is integrated thus:

$$
-\int_{C_{A 0}}^{C_{A}} \frac{d C_{A}}{C_{A}}=k \int_{0}^{t} d t
$$

one obtains:


Figure 9.4: Concentration Vs Time
Equation 9-19
$-\ln \frac{C_{A}}{C_{A 0}}=k t$
which may be rewritten as
Equation 9-20

$$
\ln C_{A}=-k t+\ln C_{A 0}
$$

and which is in the form of a linear equation $y=m x+b$.
If one plots $\ln C_{A}$ versus $t$, a straight line of slope equal to $k$ is obtained when a first order reaction is being studied.


Figure 9.5: First Order Reaction
Proof that one is dealing with a first order reaction is provided if a straight line plot of the data is obtained.

For a second order reaction it is desirable to change the form of the expression and to let $x$ be the number of moles of A or B converted. Consider the reaction

Equation 9-21

$$
A+B \rightarrow 2 P
$$

Let $w$ and $y$ be the concentrations of $A$ and $B$ initially, then at time $t$
Equation 9-22

$$
C_{A}=w-x
$$

$$
C_{B}=y-x
$$

Upon integration by parts it can be shown that

$$
\frac{1}{w-y} \ln \frac{y(w-x)}{w(y-x)}=k t
$$

If the left hand side is plotted versus time and a straight line results, it may be concluded that the reaction is second order.


Figure 9.6: Second Order Reaction
Again the slope of the straight line yields the value of the rate constant $k$. There are other methods for handling third order and fractional order reactions. When a catalytic reaction is involved, the design work becomes complicated because you do not know which step controls. Pilot plant work is needed to determine experimentally which of the several possible controlling factors actually controls.

### 9.5 Reactor Process Design

### 9.5.1 Types of Reactors

## Simple Batch

In the batch operation the reactants are loaded into the reactor initially, the reaction takes place and then the products are separated upon completion of the reaction.


Figure 9.7: Batch Reactor

## Semi-Batch

In semi-batch operation the reactants are fed and allowed to react for a set time.


Figure 9.8: Semi-Batch Reactor
Continuous Stirred Tank Reactors


Figure 9.9: Continuous Stirred Tank Reactor
Feed is introduced and product taken of $f$ continuously with this type of reactor.
Plug Flow Reactor


Figure 9.10: Plug Flow Reactor
This is essentially a pipe or tubular reactor. Feed is introduced and product removed continuously. Most larger industrial processes are performed in continuous reactors whether the reaction is homogeneous or heterogeneous.
In reactor design work the terms $\frac{V_{R}}{F}$ and $\frac{W}{F}$ are often used.
where:
$V_{R}=$ volume of the reactor.
$\mathrm{F}=$ flow rate in lbs/hr or cu.ft./hr (kg/hr or $\left.\mathrm{m}^{3} / \mathrm{hr}\right)$.
$\mathrm{W}=$ weight of catalyst.
The inverse of these terms, $\frac{F}{V_{R}}$ and $\frac{F}{W}$ is called "space velocity".
where:
$\frac{F}{V_{R}}=\mathrm{lbs}$ feed/(hr)/(cu.ft. of reactor volume) or can be CF of flow/CF of Reactor Volume generally work out to be reciprocal hour as shown next or in the equivalent metric units of flow and volume.

$$
\frac{F}{W}=\mathrm{lbs} \text { feed } /(\mathrm{hr})\left(\mathrm{lb} \text { of catalyst) }=\frac{1}{h r}\right.
$$

If laboratory work indicates that a high space velocity is permissible it means that a smaller plant scale reactor may be used. If a low space velocity is required, the reactor must be large to get much throughput.
Let us consider a flow reactor and develop an equation for use in design.

$$
F_{A O}=\text { Feed of } A / h r
$$



Figure 9.11: Flow Reactor - Fractional Conversion
Disappearance of $A$ in the reaction section is

$$
-r_{A} d v=\frac{\text { moles of } A \text { reacting }}{(\text { time })(\text { volume of reacting fluid })} x \text { volume of fluid in segment considered }
$$

### 9.5.2 Material Balance

Input = Output + disappearance by reaction

$$
F_{A}=\left(F_{A}+d F_{A}\right)+\left(-r_{A}\right) d v
$$

Now, since $\left(1-X_{A}\right)$ is the unconverted fraction
Equation 9-27

$$
F_{A}=F_{A 0}\left(1-X_{A}\right)
$$

$$
d F_{A}=d\left(F_{A 0}\left(1-X_{A}\right)\right)=-F_{A 0} d X_{A}
$$

Therefore

$$
F_{A 0} d X_{A}=\left(-r_{A}\right) d v
$$

This equation accounts for the small fraction of A converted in the section dv of the reactor. Rearranging the equation and integrating:

$$
\int_{0}^{V_{R}} \frac{d v}{F_{A 0}}=\int_{X_{A 0}}^{X_{A 1}} \frac{d X_{A}}{-r_{A}}
$$

$$
\frac{V_{R}}{F_{A 0}}=\int_{X_{A 0}}^{X_{A f}} \frac{d X_{A}}{-r_{A}}
$$

the design equation, where:
$X=$ the fractional conversion of the feed.
$V_{R}=$ the reactor volume.
$-r_{A}=$ the reaction rate which is a function of the reactant concentrations.
$F_{A O}=$ the feed rate in lbs/hr or cu.ft./hr etc.
For catalytic reactors the design equation becomes:

$$
\frac{W}{F_{A 0}}=\int_{X_{A 0}}^{X_{A f}} \frac{d X_{A}}{-r_{A}}
$$

where:
$\mathrm{W}=$ the weight of the catalyst used.
Knowing the conversion required, the feed rate, and the reaction rate, $\mathrm{r}_{\mathrm{A}}$, one can calculate the volume of reactor or the weight of catalyst required.
Sometimes the reaction rate, $r_{A}$, is not known. Instead of determining it you may plot conversion versus reciprocal space velocity, as shown below.


Figure 9.12: Conversion Versus Reciprocal Space Velocity
From the curve for a specific conversion $X$, one can calculate $V_{R}$ or $W$ for a given feed rate $F$. In common reactions the space velocity has been determined. For example, for sulphur production the common value of space velocities used are 700 to $900 \frac{\mathrm{cu} . \mathrm{ft} . / \mathrm{hr} \text { of flow }}{\text { cu.ft.catalyst }}$ or $1 / \mathrm{hr}$. This is based on the total volume of gas feed to the reactor.

### 9.6 Sulphur Plants

This has been an elementary treatise on reaction kinetics. Let's follow through the design of a sulphur plant reaction system to see the considerations that are involved in the design of such a system.
The reactions involved are:

## Reaction Furnace

$$
\begin{aligned}
& \mathrm{H}_{2} \mathrm{~S}+3 / 2 \mathrm{O}_{2} \rightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{SO}_{2} \\
& \Delta \mathrm{H}=-124 \text { to } 138 \mathrm{kcal}
\end{aligned}
$$

## Reactor

$$
\begin{aligned}
& 2 \mathrm{H}_{2} \mathrm{~S}+\mathrm{SO}_{2} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}+3 / e^{S_{e}} \\
& \Delta \mathrm{H}=-21 \text { to }-35 \mathrm{kcal}
\end{aligned}
$$

The term $\frac{3}{e} S_{e}$ is used because of the many forms of S in the vapour (i.e. $\mathrm{S}_{2}, \mathrm{~S}_{6}, \mathrm{~S}_{8}$, are most prominent.)

The design of a reaction system of this process is quite complex. Some of the problems are:

1. The equilibrium reaction of (2) above is favoured at low temperatures $400^{\circ} \mathrm{F}$ to $500^{\circ} \mathrm{F}$ ( $205^{\circ} \mathrm{C}$ to $260^{\circ} \mathrm{C}$ )
2. There is considerable heat evolved from the reaction.
3. The condensation of liquid sulphur on the catalyst poisons it; therefore we must keep reaction above a dewpoint of $350^{\circ} \mathrm{F}$. $\left(176^{\circ} \mathrm{C}\right)$. Generally the temperature is kept above $425^{\circ} \mathrm{F}$. $\left(218^{\circ} \mathrm{C}\right)$
4. The reaction equilibrium can be shifted to the right by removing one of the products.
5. There is some elemental sulphur formed by free flame conversion in the waste heat boiler.

Therefore the process has evolved as follows:

1. Partially burn the $\mathrm{H}_{2} \mathrm{~S}$ - according to equations (33), then cool the effluent gases through a waste heat recovery boiler and a sulphur condenser as shown in the figure below.


## Figure 9.13: Start of a Sulphur Plant

2. Reheat the gases to about $450^{\circ} \mathrm{F}\left(232^{\circ} \mathrm{C}\right)$ and send to \#1 converter.


Figure 9.14: $1^{\text {st }}$ Converter in a Sulphur Plant
Cool the gases from the reactor in a sulphur condenser.
3. Again reheat to $440^{\circ} \mathrm{F}\left(225^{\circ} \mathrm{C}\right)$ and send to the next converter.


Figure 9.15: $2^{\text {nd }}$ Converter in a Sulphur Plant
4. If further conversion is desired a further reheat and catalytic conversion step is carried out.

The condensers and reheaters are sized by common heat transfer calculations. The converters are sized by allowable space velocity. Normally the two converters are sized for the appropriate space velocity and the third is a backup. Because of governmental regulations on sulphur recoveries and discharges to the atmosphere, additional converters are often put in.

### 9.7 Example Problems

## Example Problem 9.1

The graph attached shows the conversion of $\mathrm{H}_{2} \mathrm{~S}$ to element sulphur versus the reciprocal space velocity at specific pressure and at specific temperature range. Determine whether the two reactors sized for space velocities of 600 cu.ft. per hour/cu.ft. of catalyst or three reactors sized for space velocities of 1000 cu.ft. per hour/cu.ft. of catalyst.
Which system will give the greater \% conversion?

- Assume complete removal of the sulphur after each converter.
- Assume that the $\% \mathrm{H}_{2} \mathrm{~S}$ on the Y axis is based on the $\mathrm{H}_{2} \mathrm{~S}$ present in the feed to each reactor.


## Example Problem 9.2

Isopentane is a very desirable high octane blending stock. Considerable amounts of it can be made by isomerizing $n$ pentane. This process occurs by passing the $n$ pentane through a reactor filled with a platinum catalyst. Below is listed the conversion data.

| Mole \% Converted of $\mathrm{nC}_{5}$ <br> $\mathbf{i C}_{5}$ | Space Velocity <br> $\frac{\text { lbs/hr of feed }}{\text { lbs of Catalyst }}$ |
| :---: | :---: |
| 10 | 20.00 |
| 30 | 10.00 |
| 50 | 4.00 |
| 70 | 2.00 |
| 80 | 1.42 |
| 85 | 1.17 |
| 90 | 1.00 |
| 95 | 0.82 |

The production of $n$ pentane is $5000 \mathrm{~B} / \mathrm{D}$ and it is wished to produce an isopentane product containing 90 mole \% $\mathrm{iC}_{5}$.

Two possible schemes are proposed.


Determine which scheme you would use based on the lowest capital cost.

## Data

- Reactor installed cost $\$ 5.00 / \mathrm{lb}$ of catalyst needed.
- Pentane splitter $60 \phi / \mathrm{lb}$ of feed/hr to it.
- Assume product leaving the pentane splitter is fractionated so as to produce a $90 \% \mathrm{iC}_{5}$ $10 \% \mathrm{nC}_{5}$ stream and that the bottoms is a stream containing $90 \% \mathrm{nC}_{5}$ and $10 \% \mathrm{iC}_{5}$.
- Assume that the reaction gives a yield of a volume product for a volume feed and that it occurs in the liquid phase.
- For ease in calculation assume that both iso and normal pentane have a density of 5.2 lbs/US gallon.


Figure 9.16: $\mathrm{H}_{2} \mathrm{~S}$ Converted to S

# Appendix 1.0 Natural Gas Processing Principles and Technology - Part I 

List of Key Terms

List of Example Problems
List of Equations
Reference of Key Equations

## List of Key Terms

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$=\frac{1.84}{100}\left(\frac{1000}{379}\right)(10.42)=0.54 \frac{\text { US Gallons }}{1000 C F}$ ..... 1-10
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$\frac{1.84}{100} \frac{1000}{23.6} \frac{0.08684}{1000}=0.06770 \quad$ cu.m. ..... 1-10
$\frac{6.14}{100} \frac{1000}{0.0236} \frac{32}{1000}=0.08325$ ..... 1-10
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$P V=R T$ ..... 2-2
$P V=Z R T$ ..... 2-2

$$
\begin{aligned}
& \left(P+\frac{a}{v^{2}}\right)(V-b)=R T \\
& P=\frac{R T}{V^{2}}\left(1-\frac{c}{V T^{3}}\right) V+B_{0}\left(1-\frac{b}{V}\right)-\frac{A_{0}}{V^{2}}\left(1-\frac{a}{V}\right) \\
& \text { 2-2 } \\
& P=R T \rho+\left(B_{0} R T-A-\frac{C_{0}}{T^{2}}+\frac{D_{0}}{T^{3}}-\frac{E_{0}}{T^{4}}\right) \rho^{2}+\left(b R T-a-\frac{d}{T}\right) \rho^{3}+\left(a+\frac{d}{T}\right) \alpha \rho^{6}+\frac{c \rho^{3}}{T^{2}}\left(1+\chi \rho^{2}\right) \exp \left(-\chi \rho^{2}\right) \\
& d^{1 / 3}=\sum_{i} x_{i} d_{i}^{1 / 3} \\
& Z=\frac{1}{1-h}-\frac{A^{2}}{B}\left(\frac{h}{1+h}\right) \\
& P=\frac{R T}{V-b}-\frac{a(T)}{V(V+b)} \text {. }
\end{aligned}
$$

$Z^{3}-Z^{2}+Z\left(A-B-B^{2}\right)-A B=0$ ..... 2-5
$a_{i j}=\left(1-k_{i j}\right)\left(a_{i} a_{j}\right)$ ..... 2-6
$P=\frac{R T}{V-b}-\frac{a(T)}{V(V+b)+b(V-b)}$ ..... 2-6
$H_{T, P}-H_{T, 0}=\left(B_{0} R T-2 A_{0}-\frac{4 C_{0}}{T^{2}}+\frac{5 D_{0}}{T^{3}}-\frac{6 E_{0}}{T^{4}}\right) \rho+0.5\left(2 b R T-3 a-\frac{4 d}{T}\right) \rho^{2}+0.2 \alpha\left(6 a+\frac{7 d}{T}\right) \rho^{5}$$+\frac{c \rho^{2}}{T}\left[3\left(\frac{1-\exp \left(-\chi \rho^{2}\right)}{\chi \rho^{2}}\right)-0.5 \exp \left(-\chi \rho^{2}\right)+\gamma \rho^{2} \exp \left(-\chi \rho^{2}\right)\right]$2-6
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$P_{r}=\frac{P}{P_{c}}=\frac{1014.7}{670.9}=1.52$ ..... 2-8
$\rho=\frac{P M_{W}}{Z R T}=\frac{1014.7(18.4)}{0.855(10.73)(560)}=3.7 \mathrm{lbs} / \mathrm{cu} . \mathrm{ft}$ ..... 2-8
$\rho=\frac{P M_{W}}{Z R T}=\frac{69(18.4)}{0.855(82.057)(305)}=0.059 \mathrm{gram} / \mathrm{cc}$ ..... 2-8
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$$
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$$2-11$T_{r}=\frac{540}{432}=1.25$2-11

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$240-17=223$ ..... 2-11
$p P_{c}^{\prime}=834\left(\frac{401}{432+6}\right)=770$ ..... 2-11$5750\left(\frac{223}{240+3.28}\right)=5270$2-11
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0.69 ..... 2-12
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$\Delta F^{0}{ }_{P-R}=\Delta H^{0}{ }_{P-R}-T \Delta S^{0}{ }_{P-R}$ ..... 2-23
$\left(\frac{\partial H}{\partial P}\right)_{T}=V-T\left(\frac{\partial V}{\partial T}\right)_{P}$ ..... 2-24
$H^{0}-H=R T_{C}\left[\left(\frac{H^{0}-H}{R T_{C}}\right)^{0}+\varpi\left(\frac{H^{0}-H}{R T_{C}}\right)\right]^{1}$ ..... 2-24$\mu=\left(\frac{\partial T}{\partial P}\right)_{H}$2-28
$H_{\text {ideal }}=\sum_{i} x_{i} H_{i}$ ..... 2-29
$H_{r}=\frac{H_{\text {ideal }}}{Z}$ ..... 2-29
$Z=1-\left(x_{1} \sqrt{b_{1}}+x_{2} \sqrt{b_{2}}+\ldots \ldots \ldots+x_{n} \sqrt{b_{n}}\right)^{2}$ ..... 2-29
$\mu=\frac{\text { Shearing Stress }}{\text { Rate of Shear Stress }}$ ..... 2-33
$k$ at high pressure
$k$ at atmospheric pressure from 16.29 ..... 2-36
$\sigma^{0.25}=\frac{P}{M}\left(d_{1}-d_{V}\right)$ ..... 2-36
$\frac{d P}{d T}=\frac{\Delta H}{T \Delta V}$ ..... 3-1
$f(P, T, V)=0$ ..... 3-6
$f(P, T, V, X)=0$ ..... 3-7
$K_{i}=\frac{y_{i}}{x_{i}}$ ..... 4-1
$P_{i}=P_{V P i} x_{i}$ ..... 4-2
$P_{i}=P_{t} y_{i}$ ..... 4-2
$y_{i} P_{t}=P_{V P i} x_{i}$ ..... 4-2

$$
\frac{y_{i}}{x_{i}}=\frac{P_{V P i}}{P_{t}}
$$4-2

$$
K_{i}=\frac{y_{i}}{x_{i}}=\frac{P_{V P i}}{P_{t}}
$$4-2

$\mathrm{RT} \mathrm{d} \ell \mathrm{nf}=\mathrm{VdP}$ ..... 4-3
$\ln \frac{f}{P}=\frac{1}{R T} \int_{0}^{P} v d P$ ..... 4-3
$f_{i}^{v}=y_{i} f_{v i}$ ..... 4-3
$f_{i}^{l}=x_{i} f_{l i}$ ..... 4-3
$f_{i}^{v}=f_{i}^{l}$ ..... 4-3
$K_{i}=\frac{y_{i}}{x_{i}}=\frac{f_{l i}}{f_{v i}}$ ..... 4-3
$K_{i}=\frac{y_{i}}{x_{i}}=\frac{\chi_{i}^{L} f_{l i}}{\chi_{i}^{V} f_{v i}}$ ..... 4-3
$K=\phi\left(P, T, x_{1}, x_{2}, \ldots \ldots \ldots x_{n}\right)$ ..... 4-6
$K=\phi^{\prime}\left(P, T, x_{1}, x_{2}, \ldots \ldots \ldots \ldots \ldots . x_{n-2}\right)$ ..... 4-7
$P_{K}=\phi^{\prime \prime}\left(T, x_{1}, x_{2}, \ldots \ldots \ldots \ldots . . x_{n-2}\right)$ ..... 4-7
$K=\phi^{\prime \prime}\left(P, P_{K}\right)$ ..... 4-7
$P_{K}=\phi^{I V}(T)$ ..... 4-7
$K=\phi^{V}(P, T)$ ..... 4-7
$K_{i}=\frac{\gamma_{i} \nu_{i}^{\circ}}{\phi_{i}}$. ..... 4-11
$f_{i}=\gamma_{i} x_{i} f_{i}^{\text {PureL }}$ ..... 4-11

$$
v_{i}^{\circ}=\frac{f_{i}^{\text {PureL }}}{P}
$$4-11

$$
\phi_{i}=\frac{f_{i}}{P_{i}}=\frac{f_{i}}{y_{i}^{P}} .
$$

$\ln \chi_{i}=\frac{V_{i}\left(\delta_{i}-\delta\right)^{2}}{R T}$4-11

$$
\delta=\frac{\Delta E^{0.5}}{V_{i}}
$$

$\log v_{i}^{0}=\log \left(v_{i}\right)^{0}+\omega \log \left(v_{i}\right)^{1}$
$\log \left(v_{i}\right)^{0}=A_{0}+\frac{A_{1}}{T_{R}}+A_{2} T_{R}+A_{3} T_{R}^{2}+A_{4} T_{R}^{3}+\left(A_{5}+A_{6} T_{R}+A_{7} T_{R}^{2}\right) P_{R}+\left(A_{8}+A_{9} T_{R}\right) P_{R}^{2}-\log P_{R} \ldots \ldots .4-12$
$\log \left(v_{i}\right)^{1}=A+B T_{R}+\frac{C}{T_{R}}+D T_{R}{ }^{3}-0.25\left(P_{R}-0.6\right)$
$P=\frac{R T}{v-b}-\frac{a}{T^{0.5} V(V+b)}$
$z=\frac{1}{1-h}-\frac{A^{2}}{B}\left(\frac{h}{1+h}\right)$
$h=\frac{B P}{z}$
4-13
$\ln \phi_{i}=(Z-1) \frac{B_{i}}{B}-\ln (A-B P)-\frac{A^{2}}{B}\left(\frac{2 A_{i}}{A}-\frac{B_{i}}{B}\right) \ln \left(1+\frac{B P}{Z}\right)$
$P=\frac{R T}{V-b}-\frac{a T}{v(v+b)}$
$P=\frac{R T}{v-b}-\frac{a(T)}{v(v+b)+b(v-b)}$
$P=R T \rho+\left(B_{0} R T-A-\frac{C_{0}}{T^{2}}+\frac{D_{0}}{T^{3}}-\frac{E_{0}}{T^{4}}\right) \rho^{2}+\left(b R T-a-\frac{d}{T}\right) \rho^{3}+\left(a+\frac{d}{T}\right) \alpha \rho^{6}+\frac{c \rho^{3}}{T^{2}}\left(1+\chi \rho^{2}\right) \exp \left(-\chi \rho^{2}\right)$
$B_{0}=\sum_{i} x_{i} B_{0 i}$
$b^{1 / 3}=\sum_{i} x_{i} b_{i}^{1 / 3}$
$A_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{3} x_{i} x_{j} A_{0 i}^{1 / 3} A_{0 j}^{1 / 2}$
$a^{1 / 3}=\sum_{i} x_{i} a_{i}^{1 / 3}$
$C_{0}=\sum_{i} \sum_{j}\left(\frac{m_{1 j}}{2}\right)^{3} x_{i} x_{j} C_{0 i}^{1 / 2} C_{0 j}{ }^{1 / 2}$
$\alpha^{1 / 3}=\sum_{i} x_{i} \alpha_{i}^{1 / 3}$ ..... 4-14
$\chi^{1 / 2}=\sum_{i} x_{i} \chi_{i}^{1 / 2}$ ..... 4-14
$c^{1 / 3}=\sum_{i} x_{i} c_{i}^{1 / 3}$ ..... 4-14$D_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{4} x_{i} x_{j} D_{0 i}^{1 / 2} D_{0 j}^{1 / 2}$

$$
d^{1 / 3}=\sum_{i} x_{i} d_{i}^{1 / 3}
$$

$$
E_{0}=\sum_{i} \sum_{j}\left(\frac{m_{i j}}{2}\right)^{5} x_{i} x_{j} E_{0 i}^{1 / 2} E_{0 j}^{1 / 2}
$$

$$
f_{i}^{v}=f_{i}^{\ell}
$$4-15

$\ln \phi_{i}=\ln \frac{V}{V-b}+\frac{b_{i}}{V-b}-\frac{2 \sum_{i} y_{i} a_{i j}}{R T^{1.5} b} \ln \left(\frac{V+b}{V}\right)+\frac{a b_{i}}{R T^{1.5} b^{2}}\left[\ln \frac{V+b}{V}-\frac{b}{V+b}\right]-\ln z$ ..... 4-15
$\sum_{i=1}^{n} y_{i}=1.0$ ..... 4-17

$$
\sum_{i=1}^{n} x_{i}=1.0
$$4-17

$x_{i}=\frac{y_{i}}{K_{i}}$ ..... 4-17
$y_{i}=K_{i} x_{i}$ ..... 4-18
$\sum_{i=1}^{n} y_{i}=1.0$ ..... 4-18
$K x=1.0$ ..... 4-18
$F=V+L$ ..... 4-20
$z_{i} F=y_{i} V+x_{i} L$ ..... 4-20
$y_{i}=K_{i} x_{i}$ ..... 4-20
$z F=K x V+x L$ ..... 4-20
$z F=x(V K+L)$ ..... 4-20

$$
\begin{aligned}
& x=\frac{\frac{z F}{L}}{K \frac{V}{L}+1} \\
& \sum_{i}^{n} x=1.0 \\
& \sum_{i=1}^{n} x=\sum_{i=1}^{n} \frac{z F}{K \frac{V}{L}+1}=L \\
& W_{\text {mixture }}=Y_{\mathrm{HC}} W_{\mathrm{HC}}+Y_{\mathrm{H}_{2} \mathrm{~S}} W_{\mathrm{H}_{2} \mathrm{~S}}+Y_{\mathrm{CO}_{2}} W_{\mathrm{CO}_{2}} \\
& \overline{P i}=H X i \\
& \text { 5-7 } \\
& \int_{1}^{2} V d P+\Delta\left(\frac{v^{2}}{2 g_{c}}\right)+\Delta z+l w
\end{aligned}
$$

$\frac{\Delta P}{\rho}+\Delta\left(\frac{v^{2}}{2 g_{c}}\right)+\Delta z=l w$ ..... 6-5
$F^{\prime}=f^{\prime} \frac{\rho \pi D L v^{2}}{2 g_{c}}$ ..... 6-6
$\frac{\rho \pi D^{2} d L}{4}$ ..... 6-6
$l w=\frac{F^{\prime} d L}{\rho \pi D^{2} d L / 4}=\frac{4 F^{\prime}}{\rho \pi D^{2}}$ ..... 6-6
$l w=\frac{2 f^{\prime} L v^{2}}{D g_{c}}$ ..... 6-6
$l w=\frac{\Delta P}{\rho}=\frac{2 f^{\prime} L v^{2}}{D g_{c}}$ ..... 6-6
Now let $f=4 f^{\prime} \quad f^{\prime}=\frac{f m}{4}$ ..... 6-6
$\Delta P=\frac{f m \rho L v^{2}}{2 g_{c} D}$ in $l b / f t^{2}$ ..... 6-6
$\Delta P=\frac{\rho f m L v^{2}}{144 D\left(2 g_{c}\right)}$ ..... 6-7
$\Delta P=\frac{f W^{2} L}{5715 \rho D^{5}}$ ..... 6-10
$f=\frac{64}{\operatorname{Re}}$ ..... 6-10
$\mathrm{Pv}^{\mathrm{k}}=$ Constant ..... 6-15
$\left(\frac{P_{2}}{P_{1}}\right)=\left(\frac{V_{1}}{V_{2}}\right)^{k}$ ..... 6-15$k=\frac{C_{P}}{C_{V}}$6-15
$\frac{P_{2}}{P_{1}}=\frac{V_{1}}{V_{2}}$ ..... 6-15$P_{1} V_{1}=U_{2}-U_{1}+\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}+P_{2} V_{2}$6-16

$C_{V}\left(T_{2}-T_{1}\right)=U_{2}-U_{1}$
$\mathrm{PV}=\mathrm{R} T$. ..... 6-16
$C_{V}=\frac{R}{k-1}$ ..... 6-16$\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=P_{1} V_{1}-P_{2} V_{2}+C_{V}\left(T_{1}-T_{2}\right)$6-16
$\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=P_{1} V_{1}-P_{2} V_{2}+\frac{P_{1} V_{1}}{k-1}-\frac{P_{2} V_{2}}{k-1}$ ..... 6-16

$$
\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=\frac{k}{k-1}\left(P_{1} V_{1}-P_{2} V_{2}\right)
$$

$$
\frac{P_{2}}{P_{1}}=\left(\frac{V_{1}}{V_{2}}\right)^{k}=\left(\frac{\rho_{2}}{\rho_{1}}\right)^{k}
$$6-17

$$
\frac{v_{2}^{2}-v_{1}^{2}}{2 g_{c}}=\left(\frac{k}{k-1}\right)\left(\frac{P_{1}}{\rho_{1}}\right)\left[1-\left(\frac{P_{2}}{P_{1}}\right)^{\frac{k-1}{k}}\right] .
$$

$W=\frac{A_{2} v_{2}}{V_{2}}$
$W=A \sqrt{\left(\frac{2 k g_{c}}{k-1}\right)\left(\frac{P_{1}}{V_{1}}\right)\left(\frac{P_{2}}{P_{1}}\right)^{\frac{2}{k}}-\left(\frac{P_{2}}{P_{1}}\right)^{\frac{k-1}{k}}}$
$\frac{P_{c}}{P_{1}}=\left(\frac{2}{k+1}\right)^{\frac{1}{k-1}}$
$v_{c}=\sqrt{\frac{2 g_{c}}{k+1} k\left(P_{1} V_{1}\right)}=\sqrt{\frac{k P_{c}}{\rho_{c}}}$.

$$
v_{c}=\sqrt{k g_{c} T_{c} \frac{z_{c} R}{M}} .
$$

$$
V d P+\frac{d\left(v^{2}\right)}{2 g_{c}}+d R=0
$$

$$
d R=\frac{f v^{2} d l}{2 g_{c} D}
$$

$$
\begin{aligned}
& V d P+\frac{v d V}{g_{c}}+\frac{f v^{2} d l}{2 g_{c} D}=0 \\
& \frac{2 g_{c} V d P}{v^{2}}+\frac{2 d v}{v}+\frac{f d l}{D}=0 \\
& P_{1}^{2}-P_{2}^{2}=\frac{v_{1}^{2} P_{1}}{g_{c} V_{1}}\left[2 \ln \frac{v_{2}}{v_{1}}+\frac{f l}{D}\right] \\
& \frac{f l}{D} \gg 2 \ln \frac{v_{2}}{v_{1}} \\
& \frac{P_{1}^{2}-P_{2}^{2}}{P_{1}^{2}}=\frac{f l v_{1}^{2}}{g_{c} D_{1} P_{1} V_{1}} \\
& P_{1}-P_{2}=P_{1}\left[1-\sqrt{1-\frac{f l v_{1}^{2}}{g_{c} D P_{1} V_{1}}}\right] \\
& Q=K \frac{T_{s}}{P_{s}}\left[\frac{\left(P_{1}^{2}-P_{2}^{2}\right) d^{5}}{f L S T Z_{a}}\right]^{\frac{1}{2}}
\end{aligned}
$$

$$
\begin{align*}
& Q=0.0037 \frac{T_{b}}{P_{b}}\left[\frac{P_{1}^{2}-P_{2}^{2}}{S T L Z_{a}}\right]^{\frac{1}{2}} d^{2.667} \\
& \frac{1}{f}=\theta(\operatorname{Re})^{0.73} \\
& Q=K E\left(\frac{T_{b}}{P_{b}}\right)^{\alpha}\left(\frac{P_{1}^{2}-P_{2}^{2}}{T_{a} L Z_{a}}\right)^{\beta} \frac{D^{\chi}}{S^{\nu}} \\
& P_{1}=\left\{P_{2}^{2}+K\left(\frac{Q}{E}\right)^{\alpha}\left(\frac{P_{b}}{T_{b}}\right)^{\beta} \frac{S^{\chi}}{D^{v}} T_{a} L Z_{a}\right\}^{1 / 2} \\
& P_{2}=\left\{P_{1}^{2}-K\left(\frac{Q}{E}\right)^{\alpha}\left(\frac{P_{b}}{T_{b}}\right)^{\beta} \frac{S^{\chi}}{D^{v}} T_{a} L Z_{a}\right\}^{1 / 2}
\end{align*}
$$

$$
\begin{align*}
& D=K\left(\frac{Q}{E}\right)^{\alpha}\left(\frac{P_{b}}{T_{b}}\right)^{\beta}\left(\frac{T_{a} L Z_{a}}{P_{1}^{2}-P_{2}^{2}}\right)^{\chi} \frac{S}{1} \\
& \frac{\Delta z S}{A T_{a} Z_{a}}=\frac{\ln P_{1}}{P_{2}} \\
& \Delta P_{100}=\frac{W^{2}}{e}\left(\frac{0.000336 f_{f}}{d^{5}}\right) \\
& \frac{\Delta P}{100 M}=\frac{W^{2}}{\rho}\left(\frac{62530 \times 10^{2} f}{d^{5}}\right) \\
& \Delta P_{\text {total }}=\Delta P_{\text {two phase flow }}+\Delta P_{\text {elevation change }}+\Delta P_{\text {acceleration change }} \\
& \lambda=\left[\left(\frac{\rho_{g}}{0.075}\right)\left(\frac{\rho_{L}}{62.3}\right)\right]^{1 / 2} \\
& \Psi=\frac{73}{\chi}\left[u_{L}\left(\frac{62.3}{\rho_{L}}\right)^{2}\right]^{1 / 3} \\
& \Delta P_{T P}=\Delta P_{G} \phi_{G T T}^{2} \\
& \text { 6-29 } \\
& \phi_{G T T}=\frac{14.2 x^{0.75}}{L^{0.1}} \text {. } \\
& \phi_{G T T}=\frac{27.315 x^{0.855}}{L^{0.17}} \\
& \phi_{G T T}=\frac{15400 x}{L^{0.8}} \\
& \phi_{G T T}=\frac{1190 x^{0.815}}{L^{0.5}} \\
& \phi_{G T T}=(4.8-0.3125 d)(X)^{0.343-0.021 d} \\
& \text { 6-30 } \\
& x^{2}=\left(\frac{\Delta P_{\text {liquid }}}{\Delta P_{\text {gas }}}\right)=\left(\frac{L}{G}\right)^{1.8}\left(\frac{\rho_{g}}{\rho_{l}}\right)\left(\frac{\mu_{l}}{\mu_{g}}\right)^{0.2} \\
& \left(\frac{\mu_{l}}{\mu_{g}}\right)^{0.2} \approx 1.6 \text {. } \\
& x^{2}=1.6\left(\frac{L}{G}\right)^{1.8}\left(\frac{\rho_{g}}{\rho_{l}}\right)
\end{align*}
$$

$\Delta P_{H}=\frac{\sum h F_{e} \rho_{L}}{144}$ ..... 6-41
$(\Delta P)_{\text {increment }}=\Delta P_{f}+\left(\Delta Z^{+}\right) \rho_{M}$ ..... 6-42
$\rho_{M}=\rho_{L} E_{L}+\rho_{G}\left(1-E_{L}\right)$ ..... 6-42
$\mathrm{U}=\frac{31,194 Z Q}{P d^{2}}$ in ft/sec ..... 6-43
$U=\frac{31194(60)(0.800)}{(8)^{2}(1100)}=21.3 \mathrm{ft} / \mathrm{sec}$ ..... 6-44
$\Delta P_{H}=\frac{\rho_{L} F_{e} \sum h}{144}=\frac{44(0.12)(500)}{144}=18.3 \mathrm{psi}$ ..... 6-44
$\frac{U}{R^{0.32}}=\frac{21.3}{(12)^{0.32}}=9.7$ ..... 6-45
$Q=435.87 E\left(\frac{T_{0}}{P_{0}}\right)^{1.078}\left(\frac{P_{1}^{2}-P_{2}^{2}}{L}\right)^{0.5394}\left(\frac{1}{T}\right)^{0.5394}\left(\frac{1}{G}\right)^{0.4606}\left(\frac{1}{Z}\right)^{0.5} d^{2.6182}$ ..... 6-45
$60 \times 10^{6}=435.87(0.86)\left(\frac{520}{14.65}\right)^{1.078}\left(\frac{1215^{2}-P_{2}^{2}}{L}\right)^{0.5394}\left(\frac{1}{530}\right)^{0.5394}\left(\frac{1}{0.65}\right)^{0.4606}\left(\frac{1}{0.8}\right)^{0.5} 8^{2.6182}$. ..... 6-45
$U=\frac{31194(60)(0.80)}{(10)^{2}(1100)}=13.6 \mathrm{ft} / \mathrm{sec}$ ..... 6-45
$\Delta P_{H}=\frac{44(0.18)(500)}{144}=27.5 \mathrm{psi}$ ..... 6-45
$\frac{U}{R^{0.32}}=\frac{13.6}{2.17}=6.25$ ..... 6-45
$60 \times 10^{6}=435.87(0.77)\left(\frac{520}{14.65}\right)^{1.0781}\left(\frac{1215^{2}-P_{2}^{2}}{10}\right)^{0.5394}\left(\frac{1}{530}\right)^{0.5394}\left(\frac{1}{0.65}\right)^{0.4606}\left(\frac{1}{0.80}\right)^{0.5} 10^{2.6182} \mathrm{P}_{2}=$1138 psi6-45
$\frac{G}{\lambda} v . \frac{L \lambda \Psi}{G}$ ..... 6-46
$\Delta P_{\text {two phase }}=\phi_{G T T}^{2} \Delta P_{G}$ ..... 6-46
$\lambda=\left[\left(\frac{\rho_{G}}{0.075}\right)\left(\frac{\rho_{L}}{62.3}\right)\right]^{1 / 2}=\left[\left(\frac{7.10}{0.075}\right)\left(\frac{44}{62.3}\right)\right]^{1 / 2}=8.1$ ..... 6-46

Gas Flow $(\mathrm{lb} /$ day $)=\frac{60 \times 10^{2}}{384}(0.69)(29)=2.96 \times 10^{6} \mathrm{lb} / \mathrm{day}$.
$G=\frac{2.96 \times 10^{6}}{24\left(\frac{\pi}{4} \frac{10^{2}}{144}\right)}=226000 \frac{\mathrm{lb} / \mathrm{hr}}{\text { sq.ft. }}$.
$\frac{G}{\lambda}=\frac{226000}{8.1}=28000$
$\Psi=\frac{73}{\chi}\left[u_{L}\left(\frac{62.3}{\rho_{L}}\right)^{2}\right]^{1 / 3}$
$\chi=22$ dynes $/ \mathrm{cm} ; \quad u_{L}=0.5$
$\Psi=\frac{73}{22}\left[0.5\left(\frac{62.3}{44}\right)^{2}\right]^{1 / 3}=3.3$
$L=\frac{12(60)(350)(0.7)(144)}{78.9(24)}=13200$
$=\frac{13200}{226000}(8.1)(3.3)=1.56$
$x^{2}=\left(\frac{13200}{226000}\right)^{1.8}\left(\frac{7.10}{44}\right)(1.6)=(0.058)^{1.8}(0.16)(1.6)=0.00152$
$\phi^{2}=\frac{\Delta P_{T P}}{\Delta P_{G}}=1.2 \quad \Delta P_{T P}=0.2(1.2)=0.24$
$\Delta P_{t w o ~ p h a s e ~}=0.24 \mathrm{psi} / 100$ foot of pipe
$W=C_{0} A_{0} \sqrt{\frac{2 g_{c} \rho(\Delta P)}{1-\left(\frac{A_{0}}{A_{1}}\right)^{2}}}$
$Q=C \sqrt{h_{w} P_{f}}$
$Q_{h}=C^{\prime} \sqrt{h_{w}}$
$Q_{T W E}=Q_{M P}\left(\frac{1+R_{H L} E}{1+R_{T L} S}\right)$.
$\mathrm{NPSH}=\mathrm{P}_{1}-\mathrm{VP}+\mathrm{H}_{1}-\mathrm{H}_{2}-\mathrm{F}$. 6-57
$\frac{C_{P}}{C_{V}}=K$ ..... 6-58
$Y_{C_{3}}=K x_{C_{3}}$ ..... 7-2
$L_{n+1}+V_{n-1}=V_{n}+L_{n}$ ..... 7-2
$J_{A}=-D_{A B} \frac{d C_{A}}{d Z}$ ..... 7-4
$J_{B}=-D_{B A} \frac{d C_{B}}{d Z}$ ..... 7-4
$C_{A}=\frac{P_{A}}{R T} \quad$ and $\quad C_{B}=\frac{P_{B}}{R T}$ ..... 7-4
$J_{A}=-\frac{D_{A B}}{R T} \frac{d P_{A}}{d Z}$ ..... 7-5
$J_{B}=-\frac{D_{B A}}{R T} \frac{d P_{B}}{d Z}$ ..... 7-5
$D_{1,2}=\frac{0.04381 T^{1.5}\left(\frac{1}{M_{1}}+\frac{1}{M_{2}}\right)^{0.5}}{p\left(\sigma_{1,2}\right)^{2} \Omega_{D}}$ ..... 7-5
$\frac{\varepsilon}{k}=65.3 T_{C} Z_{C}^{3.6}$ ..... 7-6
$\sigma=0.7402 \frac{\left(M V_{C}\right)^{0.333}}{z_{C}^{1.2}}$ ..... 7-6
$\sigma_{1,2}=\frac{1}{2}\left(\sigma_{1}+\sigma_{2}\right)$ ..... 7-6
$\frac{\varepsilon_{1,2}}{k}=\left[\left(\frac{\varepsilon_{1}}{k}\right)\left(\frac{\varepsilon_{2}}{k}\right)\right]^{0.5}$ ..... 7-6
$D_{1,2}=\frac{1.59 \times 10^{-7}\left(\Psi_{2} M_{2}\right)^{0.5 T}}{\mu\left(\frac{M_{1}}{\rho_{1}}\right)^{0.6}}$ ..... 7-7$N_{A}=\left(N_{A}+N_{B}\right) \frac{P_{A}}{P}-\frac{D_{A B}}{R T} \frac{d P_{A}}{d Z}$7-8
$N_{A}=J_{A}=-N_{B}=-J_{B}$ ..... 7-8
$\frac{d P_{A}}{d Z}=-\frac{d P_{B}}{d Z}$ ..... 7-8
$D_{A B}=D_{B A}=D$ ..... 7-8
$N_{A}=\frac{D}{R T Z}\left(P_{A_{1}}-P_{A_{2}}\right)$ ..... 7-8
$N_{A}=\frac{D_{A B}}{Z}\left(C_{A_{1}}-C_{A_{2}}\right)$ ..... 7-8
$N_{A}=\frac{D P}{R T Z} \ln \left(\frac{P_{B_{2}}}{P_{B_{1}}}\right)$ ..... 7-9$N_{A}=\frac{D P}{R T Z}\left(\frac{P_{B_{2}}-P_{B_{1}}}{P_{B} \log \text { mean }}\right)$.7-9
$N_{A}=\frac{D}{R T Z}\left(\frac{P}{P_{B} \log \text { mean }}\right)\left(P_{A_{1}}-P_{A_{2}}\right)$ ..... 7-9
$P_{B} \log$ mean $=\frac{P_{B_{2}}-P_{B_{1}}}{\ln \frac{P_{B_{2}}}{P_{B_{1}}}}$ ..... 7-9$N_{A}=k_{g}\left(Y_{A}-Y_{A}^{*}\right)$7-10
$k_{g}=\frac{D_{A B}}{R T Z}$ ..... 7-10
$N_{A}=k_{L}\left(X_{A}^{*}-X_{A}\right)$. ..... 7-10
$k_{L}=\frac{D_{A B}}{Z}$ ..... 7-10
$\frac{Y_{A}-Y_{A}^{*}}{X_{A}-X_{A}^{*}}=-\frac{k_{L}}{k_{g}}$ ..... 7-11
$N_{A}=K_{g}\left(Y_{A}-Y_{A L}\right)$ ..... 7-11
$N_{A}=K_{L}\left(X_{A G}-X_{A}\right)$ ..... 7-11
$\frac{1}{K_{g}}=\frac{1}{k_{g}}+\frac{m}{k_{L}}$ ..... 7-12

$$
\frac{1}{K_{L}}=\frac{1}{k_{L}}+\frac{1}{m k_{g}}
$$

$\frac{1}{K_{g}}=\frac{1}{m K_{L}}$$N_{A} A=k_{g} a\left(Y_{A}-Y_{A}^{*}\right) V_{0}=k_{L} a\left(X_{A}^{*}-X_{A}\right) V_{0}=K_{g} a\left(Y_{A G}-Y_{A L}\right) V_{0}=K_{L} a\left(X_{A G}-X_{A L}\right) V_{0}$7-13
$\alpha=\frac{K_{l}}{K_{n}}$
$v=K \sqrt{\frac{\rho_{L}-\rho_{V}}{\rho_{V}}}$ ..... 7-19
$G_{\text {max }}=C \sqrt{\rho_{V}\left(\rho_{L}-\rho_{V}\right)}$ ..... 7-20
$h=2\left(h_{w}+h_{o w}\right)+h_{v}+h_{D}$ ..... 7-23
$\left(\frac{L_{p}}{G_{p}}\right)\left(\frac{\rho_{V}}{\rho_{L}}\right)^{1 / 2} \quad$ versus $\frac{G_{p}^{2} \mu_{L}^{0.1} F_{p}\left(\frac{\rho_{W}}{\rho_{L}}\right)^{0.2}}{32.17 \rho_{V}\left(\rho_{L}-\rho_{V}\right)}$ ..... 7-24
$P P_{a}=x_{a} V P_{a}$ ..... 7-27
$y_{A}=\frac{P P_{a}}{P T}$ ..... 7-27
$y_{a}=x_{a} \frac{V P_{a}}{P T}$ ..... 7-27
$y_{a}=K_{a} x_{a}$ ..... 7-27
$\mathrm{F}=\mathrm{D}+\mathrm{W}$ ..... 7-29
$V_{n+1}+L_{n-1}=V_{n}+L_{n}$ ..... 7-29
$V_{n+1}\left(y_{n+1}\right)+L_{n-1}\left(x_{n-1}\right)=V_{n} y_{n}+L_{n} x_{n}$ ..... 7-29
$y_{n+1}+x_{n-1}=y_{n}+x_{n}$ ..... 7-29
$V=L+D=D(R+1)$ ..... 7-29
$R=\frac{L}{D}$ ..... 7-30
$V y_{n+1}=L x_{n}+D x_{D}$ ..... 7-30
$y_{n+1}=\frac{L}{V} x_{n}+\frac{D}{V} x_{D}$ ..... 7-30
$y_{n+1}=\frac{L}{D(R+1)} x_{n}+\frac{D}{D(R+1)} x_{D}$7-30
$y_{n+1}=\frac{R}{R+1} x_{n}+\frac{x_{D}}{R+1}$ ..... 7-30
$\frac{\bar{L}}{\bar{V}}=\frac{\bar{L}}{\bar{L}-W}$ ..... 7-31
$q=\frac{\bar{L}-L}{F}=\frac{H_{V}-H_{F}}{H_{V}-H_{L}}$ ..... 7-31
$q$ ..... 7-31

$$
q-1
$$

$$
y=\frac{q x}{q-1}-\frac{z_{F}}{q-1}
$$

.7-32
$\frac{q}{q-1}=0$ ..... 7-32$\frac{q}{q-1}=\infty=\frac{1}{0}$7-32
$H_{L}=C_{P L}\left(t_{L}-t_{0}\right) M_{a v}+D_{S}$ ..... 7-33
$F=D+W$ ..... 7-36
$F z_{F}=D y_{D}+W x_{w}$ ..... 7-36
$\frac{D}{W}=\frac{z_{F}-x_{w}}{y_{D}-z_{F}}$ ..... 7-36
$F H_{F}=D H_{D}+W H_{W}$ ..... 7-36
$\frac{D}{W}=\frac{H_{F}-H_{W}}{H_{D}-H_{F}}$ ..... 7-37
$\frac{D}{W}=\frac{z_{F}-x_{w}}{y_{D}-z_{F}}=\frac{H_{F}-H_{W}}{H_{D}-H_{F}}$ ..... 7-37$\frac{1}{\text { slope }}=\frac{y_{D}-z_{F}}{H_{D}-H_{F}}=\frac{z_{F}-x_{w}}{H_{F}-H_{W}}$ with a common point $T$7-37
$\frac{\text { Distillate }}{\text { Bottoms }}=\frac{\overline{W F}}{F D}$ ..... 7-37
$\frac{\text { Bottoms }}{\text { Feed }}=\frac{\overline{F D}}{W D}$. ..... 7-38
$\frac{\text { Distillate }}{\text { Feed }}=\frac{\bar{F} \bar{W}}{W D}$ ..... 7-38
$F z_{F}=D x_{D}+W x_{w}$ ..... 7-38
$F H_{F}+q_{r}=D H_{D}+W H_{W}+q_{c}$ ..... 7-38
$Q_{D}=\frac{q_{c}}{D} \quad B T U / l b$ of $D$ ..... 7-38
$Q_{W}=\frac{q_{r}}{W} \quad B T U / l b$ of $W$ ..... 7-38
$F H_{F}=D\left(h_{D}+Q_{D}\right)+W\left(h_{B}-Q_{W}\right)$ ..... 7-38
$F H_{F}=\Delta_{D}+\Delta_{W}$ ..... 7-38
$V_{n} H_{n}=L_{n+1} H_{n+1}+D h_{D}+q_{c}$ ..... 7-39
$V_{n} H_{n}-L_{n+1} H_{n+1}=D\left(h_{D}+Q_{D}\right)=\Delta_{D}$ ..... 7-39
$\frac{V_{n+1}}{D} H_{D}-\frac{L_{0}}{D} h_{0}=h_{0}+Q_{D}$ ..... 7-39
$V_{n+1}=L_{0}+D$ ..... 7-39
$\frac{L_{0}}{D}=\frac{h_{0}+Q_{D}-H_{D}}{H_{D}-h_{0}}$ ..... 7-39

$$
\alpha_{L K}^{S M}=\frac{\left(X_{L K D}\right)\left(X_{H K W}\right)}{\left(X_{L K W}\right)\left(X_{H K D}\right)}
$$7-45

$\frac{\alpha_{1} x_{1 F}}{\alpha_{1}-\theta}+\frac{\alpha_{2} x_{2 F}}{\alpha_{2}-\theta}+\ldots \ldots+\frac{\alpha_{n} x_{n F}}{\alpha_{n}-\theta}=1-q$ ..... 7-45

$$
=\frac{H_{V}-H_{F}}{H_{V}-H_{L}} .
$$7-45

$\frac{S-S_{\min }}{S+1}=f \frac{R-R_{\min }}{R+1}$ ..... 7-47

$$
\alpha_{L K}=\frac{K C_{3}}{K i C_{4}}
$$7-49

$$
\alpha_{L K}=\frac{1.6}{0.92}=1.74
$$7-49

$$
\alpha_{L K}^{S M}=\frac{\left(X_{L K D}\right)\left(X_{H K W}\right)}{\left(X_{L K W}\right)\left(X_{H K D}\right)}
$$

$(1.74)^{S M}=\frac{(20.5)(6.7)}{(0.5)(0.3)}=925 \quad$ so $S M=12.3$ ..... 7-49$\log _{10}\left(\frac{\text { Plates above feed }}{\text { Plates below feed }}\right)=0.206 \log _{10}\left[\left(\frac{W}{D}\right)\left(\frac{Z_{H K}}{Z_{L K}}\right)\left(\frac{X_{L K W}}{X_{H L D}}\right)^{2}\right]$.7-50
$E($ overall efficiency $)=\frac{n^{*}(\text { number of theoretical trays })}{n(\text { number of actual trays })}$ ..... 7-50
$P_{v}=P_{v p} x$ ..... 7-52
$P_{v}=m^{\prime} x$ ..... 7-53
$Y=\frac{\text { moles solute }}{\text { moles inert carrier gas }} \quad$ and $\quad X=\frac{\text { moles solute }}{\text { moles inert solvent in liquid }}$. ..... 7-53$L_{0}\left(X_{i}-X_{i-1}\right)=V_{n+1}\left(Y_{i+1}-Y_{i}\right)$7-54
$y_{i}=\frac{Y_{i}\left(V_{n+1}\right)}{V_{i}}$. ..... 7-55$x_{i}=\frac{X_{i} L_{0}}{L_{i}}$7-55
$y_{i}=K_{i} x_{i}$ ..... 7-55
$Y_{i-1}=K_{i-1} x_{i-1}$ ..... 7-56
$Y_{i}=K_{i} \frac{L_{0}}{L_{i}} \frac{V_{i}}{V_{n+1}} X_{i}$ ..... 7-56
$Y_{i-1}=K_{i-1} \frac{L_{0}}{L_{i-1}} \frac{V_{i}}{V_{n+1}} X_{i-1}$ ..... 7-56$Y_{i}=\frac{Y_{i+1}+\frac{L_{i-1}}{K_{i-1} V_{i-1}} Y_{i-1}}{L+\frac{L_{i}}{K_{i} V_{i}}}$7-56Let $\quad A=\frac{L}{K V}$ or $A_{i}=\frac{L_{i}}{K_{i} V_{i}}$ or $A_{i-1}=\frac{L_{i-1}}{K_{i-1} V_{i-1}}$.7-56

$$
Y_{i}=\frac{Y_{i+1}+A_{i-1} Y_{i-1}}{L+A_{i}} .
$$7-56

Absorption $\%=\frac{Y_{n+1}-Y_{1}}{Y_{n+1}-Y_{0}}=\frac{A^{n+1}-A_{0}}{A^{n+1}-1}$ ..... 7-56
$\underline{Y_{n+1}-Y_{1}}$ ..... 7-57
$\overline{Y_{n+1}-Y_{0}}$
$\frac{X_{m+1}-X_{1}}{X_{m+1}-X_{0}}=\frac{S^{m+1}-S}{S^{m+1}-1}$ ..... 7-57
$V_{i}=V_{1} \frac{n+1-i}{n}$ ..... 7-59
$\frac{V_{i}}{V_{i+1}}=\frac{V_{1}^{1 / n}}{V_{n+1}}$ ..... 7-59
$L_{i}=L_{0}+V_{i+1}-V_{1}$ ..... 7-59
$\frac{T_{n}-T_{i}}{T_{n}-T_{0}}=\frac{V_{n+1}-V_{i+1}}{V_{n+1}-V_{1}}$ ..... 7-59
$A_{e}=\sqrt{A_{n}\left(A_{1}+1\right)+0.25}-0.5$ ..... 7-59
$w_{i}=\alpha\left(p_{i}\right)^{n}$ ..... 7-62
Rate $=\frac{\text { driving force }}{\text { resistance }}$ ..... 8-1
$d Q=K A \frac{d t}{d x}$ ..... 8-1
$Q=\frac{K}{x} A\left(t_{1}-t_{2}\right)$ ..... 8-1
$\mathrm{dQ}=\mathrm{hAdt}$ ..... 8-2
$d Q=\sigma \varepsilon d A T^{4}$ ..... 8-2
$Q_{12}=0.173 A_{1}\left[\varepsilon_{1}\left(\frac{T_{1}}{100}\right)^{4}-\alpha_{12}\left(\frac{T_{2}}{100}\right)^{4}\right]$ ..... 8-3
$Q_{12}=2.06 \times 10^{7} A_{1}\left[\varepsilon_{1} T_{1}^{4}-\alpha_{12} T_{2}^{4}\right\rfloor$ ..... 8-3
$Q=U A \Delta T$ ..... 8-7
$Q=W C_{P}\left(T_{1}-T_{2}\right)=W\left(H_{1}-H_{2}\right)$ ..... 8-8
$\Delta T_{L M T}=\frac{\left(T_{1}-t_{2}\right)-\left(T_{2}-t_{1}\right)}{\ln \frac{T_{1}-t_{2}}{T_{2}-t_{1}}}$ ..... 8-8

$$
\begin{align*}
& \Delta T_{L M T}=\frac{\Delta T_{H O T E N D}-\Delta T_{\text {COLD END }}}{\ln \frac{\Delta T_{\text {HOT END }}}{\Delta T_{\text {COLD END }}}} . \\
& \Delta T_{M}=F \Delta T_{L M T} \\
& \frac{1}{U_{0}}=\frac{1}{h_{0}}+\frac{1}{h_{i}} \frac{D_{0}}{D_{i}}+R \\
& \frac{h_{i} D_{i}}{K}=0.027\left(\frac{D_{i} G}{\mu}\right)^{0.8}\left(\frac{C_{P} \mu}{K}\right)^{\frac{1}{3}}\left(\frac{\mu}{\mu_{W}}\right)^{0.14} . \\
& j \equiv\left(\frac{h_{i} D}{K}\right)\left(\frac{C_{P} \mu}{K}\right)^{-1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{-0.14} . \\
& \frac{h_{0} D_{e}}{K}=0.36\left(\frac{D_{e} G_{s}}{\mu}\right)^{0.55}\left(\frac{C_{P} \mu}{K}\right)^{1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{0.14} \\
& A_{s}=\frac{I D\left(C^{\prime} B\right)}{P_{T}(144)} \\
& j=\frac{h_{0} D_{0}}{K}\left(\frac{C_{P} \mu}{K}\right)^{-1 / 3}\left(\frac{\mu}{\mu_{W}}\right)^{-0.14} \\
& r 2_{\text {TUBE SIDE NEW Condition }}=f(r 1)_{\text {TUbe Side Standard condition }} \\
& f=\left(\frac{\mu_{2}}{\mu_{1}}\right)^{0.27}\left(\frac{K_{1}}{K_{2}}\right)^{0.67}\left(\frac{C_{P 1}}{C_{P 2}}\right)^{0.33}\left(\frac{G_{1}}{G_{2}}\right)^{0.8}\left(\frac{D_{02}}{D_{01}}\right)^{0.2} \\
& f=\left(\frac{\mu_{2}}{\mu_{1}}\right)^{0.27}\left(\frac{K_{1}}{K_{2}}\right)^{0.67}\left(\frac{C_{P 1}}{C_{P 2}}\right)^{0.33}\left(\frac{G_{1}}{G_{2}}\right)^{0.6}\left(\frac{D_{02}}{D_{01}}\right)^{0.4} \\
& \frac{d\left(x_{f} K_{f}\right)}{d t}=\phi d-\phi r \text {. } \\
& \frac{d R f}{d t}=\frac{d\left(x_{f} K_{f}\right)}{d t} \\
& Q=U A \Delta T \\
& h=0.925 K\left(\frac{g \rho_{1}^{2}}{\mu \Gamma}\right)^{1 / 3} \text {. }
\end{align*}
$$

$h=0.76 K\left(\frac{g \rho_{1}^{2}}{\mu \Gamma}\right)^{1 / 3}$.
$\Gamma=\frac{W}{n \pi \frac{d}{12}}$
$\Gamma=\frac{W}{2 n L}$
$\Gamma=\frac{W}{4 n_{r} L}$.
$\left(\frac{Q}{A}\right)_{\max }=143 \rho_{V} \lambda\left(\frac{\rho_{L}-\rho_{V}}{\rho_{V}}\right)^{0.6}$
$\left(t_{S}-t_{b}\right)_{\max }=\frac{1}{m}\left(\frac{Q}{A}\right)_{\text {max }}$
$\frac{h}{C_{P} G}=4.02\left(\frac{D G}{\mu}\right)^{-0.3}\left(\frac{C_{P} \mu}{K}\right)^{-0.6}\left(\frac{P_{L} \chi}{p^{2}}\right)^{-0.425} \Sigma_{L}$
$\frac{h d_{r}}{K_{a}(12)}=0.1378\left(\frac{d_{r} G_{m}}{12 \mu}\right)^{0.718}\left(\frac{C_{P} \mu}{K_{a}}\right)^{1 / 3}\left(\frac{S}{l}\right)^{0.296} F_{r}$

$Q_{R c}=h_{r c} A_{R T}\left(T_{g}-T_{t}\right)$.
8-21
$Q_{R c}=7.0 \alpha A_{c p}\left(T_{g}-T_{t}\right)$.
$h_{c c}=\frac{2.14\left(T_{f}\right)^{0.28}\left(G_{\max }\right)^{0.6}}{d^{0.4}}$
$Q=U A \frac{\left(T_{1}-t\right)-\left(T_{2}-t\right)}{\ln \frac{T_{1}-t}{T_{2}-t}}$
$Q=W C_{P}\left(T_{1}-T_{2}\right)$
8-28
$Q=W\left(H_{1}-H_{2}\right)$ 8-28
$\mathrm{H}_{2} \mathrm{~S}+\frac{3}{2} \mathrm{O}_{2}+\mathrm{SO}_{2}+\mathrm{H}_{2} \mathrm{O}$
$\mathrm{SO}_{2}+2 \mathrm{H}_{2} \mathrm{~S}+3 \mathrm{~S}+2 \mathrm{H}_{2} \mathrm{O}$
9-1
$A+B \Leftrightarrow C+D$ ..... 9-1
$A+B \Rightarrow C+D$ ..... 9-1
$C+D \Rightarrow A+B$ ..... 9-1
Rate (forward) $=k_{1}[A][B]$ ..... 9-2
Rate (reverse) $=k_{2}[C][D]$ ..... 9-2
$k_{1}[A][B]=k_{2}[C][D]$ ..... 9-2
$\frac{k_{1}}{k_{2}}=K_{\text {equilibrium }}=\frac{[C][D]}{[A][B]}$ ..... 9-2
$\mathrm{NaCl}+\mathrm{AgNO}_{3} \rightarrow \mathrm{AgCl} \downarrow+\mathrm{NaNO}_{3}$ ..... 9-2
$\Delta F=-R T \ln K_{\text {equilibrium }}$ ..... 9-3
$\mathrm{SO}_{2}+1 / 2 \mathrm{O}_{2} \rightarrow\left(\frac{\mathrm{~V}_{2} \mathrm{O}_{5}}{450^{\circ} \mathrm{C}}\right) \rightarrow \mathrm{SO}_{3}$ ..... 9-3
Rate $=\frac{d c}{d t}$ ..... 9-6
$r=k C_{A}^{a} C_{B}^{b}$ ..... 9-6
$a A+b B \rightarrow$ products ..... 9-6
$A \rightarrow R+S$ ..... 9-7
$\frac{-d C_{A}}{d t}=k C_{A}$ ..... 9-7
$-\int_{C_{A 0}}^{C_{A}} \frac{d C_{A}}{C_{A}}=k \int_{0}^{t} d t$ ..... 9-7
$-\ln \frac{C_{A}}{C_{A 0}}=k t$ ..... 9-7
$\ln C_{A}=-k t+\ln C_{A 0}$ ..... 9-8
$A+B \rightarrow 2 P$ ..... 9-8
$C_{A}=w-x$ ..... 9-8
$C_{B}=y-x$ ..... 9-8
$\frac{1}{w-y} \ln \frac{y(w-x)}{w(y-x)}=k t$ ..... 9-9
$-r_{A} d v=\frac{\text { moles of } A \text { reacting }}{(\text { time })(\text { volume of reacting fluid })} x$ volume of fluid in segment considered ..... 9-11
$F_{A}=\left(F_{A}+d F_{A}\right)+\left(-r_{A}\right) d v$ ..... 9-11
$F_{A}=F_{A 0}\left(1-X_{A}\right)$ ..... 9-11
$d F_{A}=d\left(F_{A 0}\left(1-X_{A}\right)\right)=-F_{A 0} d X_{A}$ ..... 9-11
$F_{A 0} d X_{A}=\left(-r_{A}\right) d v$ ..... 9-12
$\int_{0}^{V_{R}} \frac{d v}{F_{A 0}}=\int_{X_{A 0}}^{X_{A f}} \frac{d X_{A}}{-r_{A}}$ ..... 9-12

$$
\frac{V_{R}}{F_{A 0}}=\int_{X_{A 0}}^{X_{A f}} \frac{d X_{A}}{-r_{A}} .
$$9-12

$\frac{W}{F_{A 0}}=\int_{X_{A 0}}^{X_{A f}} \frac{d X_{A}}{-r_{A}}$ ..... 9-12
$\mathrm{H}_{2} \mathrm{~S}+3 / 2 \mathrm{O}_{2} \rightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{SO}_{2}$ ..... 9-13
$\Delta H=-124$ to 138 kcal ..... 9-13
$2 \mathrm{H}_{2} \mathrm{~S}+\mathrm{SO}_{2} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}+3 / e \mathrm{~S}_{e}$ ..... 9-13
$\Delta H=-21$ to -35 kcal ..... 9-13


[^0]:    ${ }^{1}$ Published by the Gas Processors Suppliers Association and the Gas Processors Association, Tulsa, Oklahoma. Latest edition is the 10th edition which is published in English Units only. Page No.'s in the text refer to the Metric edition or the 9th English edition unless otherwise noted.

[^1]:    Natural Gas Processing Principles and Technology - Part I
    University of Calgary
    Printed: 26 April 2004 - [Natural Gas Processing Principles and Technology - Part I.doc]

[^2]:    Natural Gas Processing Principles and Technology - Part I
    University of Calgary

[^3]:    Natural Gas Processing Principles and Technology - Part I
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    Printed: 26 April 2004 - [Natural Gas Processing Principles and Technology - Part I.doc]

[^4]:    ${ }^{\nabla}$ See Figure 15-50 in the GPSA Data Book for more complete Specs (or Fig. 2.4 English GPA Data Book).

[^5]:    Natural Gas Processing Principles and Technology - Part I
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[^6]:    Natural Gas Processing Principles and Technology - Part I
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[^7]:    * Based on Gross Heating Value

[^8]:    ${ }^{1}$ An earlier method proposed by Haddon alone requires the calculation of the liquid phase weight composition and an iterative type of calculation to find critical temperature and pressure of the pseudo heavy component.

[^9]:    $\oplus$ Computer Values from NGSMA (1957)
    ${ }^{1}$ Assume to be decane $\left(\mathrm{C}_{10}\right)$. Could also possibly use data from "K" versus Boiling Point Curves. Assume $\mathrm{C}_{10}$ to be Lean Oil

[^10]:    ${ }^{4}$ The student should read and study in some detail: Chapter 8 - Fired Equipment, Chapter 9 - Heat Exchangers and Chapter 10 - Air Cooled Exchangers of the new English GPSA Data Book as a supplement to this chapter.

[^11]:    Natural Gas Processing Principles and Technology - Part I
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