GPGPU computation in mobile robot applications

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Abstract: The paper concerns the results related with GPGPU computing applied for mobile robotics applications. The scalable implementation of the point to point and point to plane 3D data registration methods with an improvement based on regular grid decomposition is shown. 3D data is delivered by mobile robot equipped with 3D laser measurement system for INDOOR environments. Presented empirical analysis of the implementation shows the On-Line computation capability using modern graphic processor unit NVIDIA GF 580. In the paper the discussion concerning the comparison between these two methods is given. It will be shown why the point to plain ICP implementation can achieve better performance than the point to point approach. We show parallel vector computation that is used for semantic objects identifications and for loop closing detection.

Keywords: Data registration, parallel computing, point to point, point to plane, mobile robot.

1. Introduction

Several researches of 3D mapping are based on the so called simulation of 3D laser range finder to obtain 3D cloud of points [1]. In most cases 3D laser simulator is built on the basis of a rotated 2D range finder. The rotation axis can be horizontal [2], vertical [3] or the rotational axis in the middle of the scanner's field of view [4]. Another approach of obtaining 3D cloud of points using two orthogonal lasers is shown in [5]. The applications are related with urban mapping [6].

Alignment and merging of two 3D scans, which are obtained from different sensor coordinates, with respect to a reference coordinate system is called 3D registration [7] [8] [9]. Park [10] proposed a real-time approach for 3D registration using GPU, where the registration technique is based on the Iterative Projection Point (IPP) algorithm. IPP technique is a combination of point-to-plane and point-to-projection registration schemes [11]. Processing time for this approach is about 60ms for aligning two 3D data sets of 76800 points during 30 iterations of the IPP algorithm. Fast searching algorithms such as the k-d tree algorithm are usually used to improve the performance of the closest point search [12] [13]. GPU accelerated nearest neighbor search for 3D registration is proposed in [14], where the advantage of Arya's priority search algorithm described in [15] to fit NNS in the SIMD (Single Instruction Multiple Data) model was used for GPU acceleration purpose. Purcell suggested that k-d tree and priority queue methods are efficient but difficult to be implemented on GPU [16]. Garcia proves, that a brute force NNS approach using NVidia Compute Unified Device Architecture (CUDA) is 400 times faster over the CPU k-d tree implementation [17]. GPU-based NNS with advanced search structures is also used in the context of ray tracing [18], where NNS procedure builds trees with a different manner from a triangle soup, and takes these triangles as the objects of interest. To convert k-d tree into serialized flat array that can be easily loaded into

CUDA device, left-balanced k-d tree was proposed [19] [20]. Another technique for 3D registration using Fast Point Feature Histograms (FPFH) is shown in the work of Rusu [21]. Rusu also proposed a way of characterizing the local geometry of 3D points, using persistent feature histograms, where the relationships between the neighbors of a point are analyzed and the resulted values are stored in a 16-bin histogram [22]. The histograms are pose and point cloud density invariant and cope well with noisy datasets. An alternative concept to ICP algorithm which relies on instantaneous kinematics and on the geometry of the squared distance function of a surface is shown in [23]. The proposed algorithm exhibits faster convergence than ICP, which is supported both by results of a local convergence analysis and by experiments. The ICP algorithm is used in SLAM 6D (Simultaneous Localization and Mapping), where 6 DOF (Degree Of Freedom) of robot position is computed based on aliment of 3D clouds of points and loop-closing technique [24].

The Iterative Closest Point algorithm with its variations point to point and point to plane is a well known method since it appeared in [25]. It is already proven that the ICP algorithm needs a good prediction to achieve an accurate matching. The fastest implementation that can be found in literature needs 60 ms to align two point clouds, each of 320 x 240 data points [10], but the authors unfortunately did not report about scalability of proposed method. In this paper, we will discuss new implementations of ICP (point to point, point to plane) that are designed especially for high performance with an assumption of scalability for future GPGPU devices. At the current stage of the implementation, we can process two data sets of $2^{10}*2^{10}$ data points in parallel. The main goal was to decrease the bottlenecks, therefore they are limited to copying data from/to host (CPU) to/from device (GPU). All computation related to neighbor search and to calculating the correlation matrix is performed by the GPU. We will show why the point to plain ICP implementation can achieve better performance than the classic point to point approach. In the same time, we demonstrate the weaknesses of this method in contrast to the advantages reported in many articles.

The paper shows an improved implementation and empirical validation of GPGPU ICP point to point and point to plane algorithms and the practical applications for normal vector parallel computation. This algorithms offer online computation. The main difference compared to State of The Art approaches is NNS procedure, where 3D space was divided into regular grid of buckets, therefore there is no need to build complex data structures such as k-d tree, and the time of ICP is decreased. We are optimistic that proposed methods will be used in future real-task applications using for example FPGA or embedded computers with GPUs.

2. Classic point to point iterative closest point algorithm

First classic ICP point to point algorithm will be described. Iterative Closest Points algorithm is aligning two-view range images with respect to the reference coordinate system. Range images are defined as a model set M and data set D, N_m and N_d denotes the number of the elements in the respective set. The alignment of these two data sets is solved by minimization with respect to $\mathbf{R}$,$\mathbf{t}$ of the following cost function:

$$E = (\mathbf{R},\mathbf{t}) = \sum_{i=1}^{N_m} \sum_{j=1}^{N_d} w_{ij} \left\| \mathbf{m}_i - \left(\mathbf{R}\mathbf{d}_j + \mathbf{t} \right) \right\|^2 \tag{1}$$

w_{ij} is assigned 1 if the i-th point of M correspond to the j-th point in D. Otherwise w_{ij}=0. $\mathbf{R}$ is a rotation matrix, $\mathbf{t}$ is a translation matrix. m_i and d_i corresponds to the i-th point from model set M and D respectively. Calculation of the rotation and translation ($\mathbf{R}$,$\mathbf{t}$) is performed using reduced equation 1:

$$\text{where } N = \sum_{i=1}^{N_m} \sum_{j=1}^{N_d} w_{ij} , \tag{3}$$

$$E(\mathbf{R},\mathbf{t}) \propto \frac{1}{N} \sum_{i=1}^{N} \left\| \mathbf{m}_i - \left(\mathbf{R}\mathbf{d}_i + \mathbf{t} \right) \right\|^2 , \tag{2}$$

Algorithm 1 Classic ICP

INPUT: Two point clouds A = $\{a_i\}$, B= $\{b_i\}$, an initial transformation T_0
OUTPUT: The correct transformation T, which aligns A and B
$T \leftarrow T_0$
for $iter \leftarrow 0$ to $maxIterations$ **do**
    for $i \leftarrow 0$ to N **do**
        $m_i \leftarrow$ FindClosestPointInA$(T \cdot b_i)$
        if $\|m_i - T \cdot b_i\| \leq d_{max}$ **then**
            $w_i \leftarrow 1$
        else
            $w_i \leftarrow 0$
        end if
    end for
    $T \leftarrow \underset{T}{argmin} \left\{ \sum_i w_i \|T \cdot b_i - m_i\|^2 \right\}$
end for

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3. GPGPU based point to point iterative closest point algorithm

The algorithm of point to point method using GPU is shown on listing 2.

Algorithm 2 ICP - parallel computing approach

INPUT: Two point clouds $M = \{m_i\}$, $D = \{d_i\}$, an initial transformation T_0
OUTPUT: The correct transformation T, which aligns M and D
$M_{device} \leftarrow M$
$D_{device} \leftarrow D$
$T_{device} \leftarrow T_0$
for $iter \leftarrow 0$ to $maxIterations$ **do**
    for $i \leftarrow 0$ to N {in parallel} **do**
        $m_i \leftarrow$ FindClosestPointInM $(T_{device} \cdot d_i)$ {using regular grid decomposition}
        if $foundClosestPointInNeighboringBuckets$ **then**
            $w_i \leftarrow 1$
        else
            $w_i \leftarrow 0$
        end if
    end for
    $T_{device} \leftarrow \underset{T_{device}}{argmin} \left\{ \sum_i w_i \|T \cdot d_i - m_i\|^2 \right\}$ {calculation T←R,t with SVD}
end for
$M \leftarrow M_{device}$
$D \leftarrow D_{device}$
$T \leftarrow T_{device}$

The main idea of using the GPU is to decompose the 3D space into a regular grid of k*k*k buckets, where $k = 2^n$, n=5,6,7,8. Because we are violating the assumption of full overlap, we are forced to add a maximum matching threshold d_{max} related to the dimension of single bucket. This threshold accounts for the fact that some points will not have any correspondence in the second scan. In most implementations of ICP, the choice of d_{max} represents a trade of between convergence and accuracy. A low value results in bad convergence, a large value causes incorrect correspondences to pull the final alignment away from the correct value. In our implementation the choice of d_{max} is done by a normalization point cloud, which has XYZ coordinates from the interval < 1; 1 >. We improved the state of the art algorithm described in

application we need to compute the SVD of a 3x3 matrix. For such a small matrix, generalized SVD algorithms from libraries like LAPACK (Linear Algebra PACKage) [29] are not beneficial especially when we have to implement them on GPGPU. Our implementation computes the singular values by solving for the roots of a cubic polynomial and then eigenvectors of $A^T A$ for V , then it uses A and V to compute U. The algorithm is executed in 5 steps.

1. Compute A^T and $A^T A$.
2. Determine the eigenvalues of $A^T A$ (by solving the roots of a cubic polynomial) and sort these in descending order. Compute square roots to obtain singular values of A.
3. Construct the diagonal matrix Σ by placing singular values in descending order along its diagonal. Compute Σ^{-1}.
4. Use the ordered eigenvalues from step 2 and compute the eigenvectors of $A^T A$. Place these eigenvectors along the columns of V and compute V^T .
5. Compute $U = AV\Sigma^{-1}$

6. Point to plain ICP

The alignment of the M and D data sets for point to plane ICP is solved by minimization of the following cost function:

$$E = (\mathbf{R}, \mathbf{t}) = \sum_{i=1}^{N_m^P} \sum_{j=1}^{N_d} w_{ij} \left\| \mathbf{m}^P_i - (\mathbf{R}\mathbf{d}_j + \mathbf{t}) \right\|^2$$

(21)

where m^P_i corresponds to projected point from data set D onto the approximation plane of data set M. w_{ij} is assigned 1 if the i_{th} point of M correspond to the j_{th} point in D. Otherwise w_{ij}=0. R is the rotation matrix, t is the translation matrix, d_j corresponds to points from data set D. We also assume that the INDOOR dataset is locally planar. Since we are sampling from two different perspectives, we will not in general sample the exact same point. For this reason, in theory the point to plane method is more accurate than point to point (see Figures 1 and 2). Unfortunately in practical application there are many exceptions where this method is less accurate than classic point to point method. We observed that in some cases it is difficult to find automatically an accurate plane approximation and a correct point to plane correspondence (see Figure 3). Of course everything is determined by the need for high performance using GPU. Therefore, the implementation based on decomposition into a regular grid of buckets may be affected by this problem. The advantage of the point to plane method over point to point is the decreased time of computation, as there is no need to search best correspondence for each bucket. This is also related to the global synchronization of threads busy with executing the same kernel for each bucket. Instead of searching the best correspondence for each bucket, the point to plane method computes a projected point, and all kernels are executed in almost the same time. Therefore, the synchronization of threads does not affect global execution time. In the consequence point to plane method can be 3 times faster than point to point. However, we would like to emphasize the fact that the bottleneck related to the large amount of processed points affects the global performance of the method.
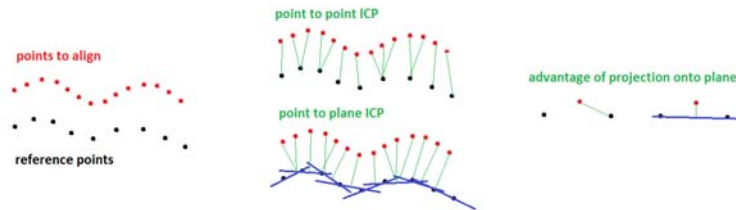

Figure 1. An advantage point to plane over point to point method.

d - category/label,

C_B -set of categories in image B,

$\left| P_{d^B \in P_{d^A}} \right|$ - amount of pixels in image B of category d^B from region of category d^A

in image A,

$\left| P_{d^A} \right|$ - amount of pixels in region of category d^A in image A.

Final entropy is given by following equation:

$$E(P_A) = \sum_{d^A \in C_A} \frac{\left| P_{d^A} \right|}{P_A} E_{d^A}(P_{d^A}) \tag{23}$$

where:

P_A -all pixels of image A,

d -category/label,

C_A -set of categories in image A,

$\left| P_{d^A} \right|$ -amount of pixels of category d^A,

$\left| P_A \right|$ - amount of pixels in image A,

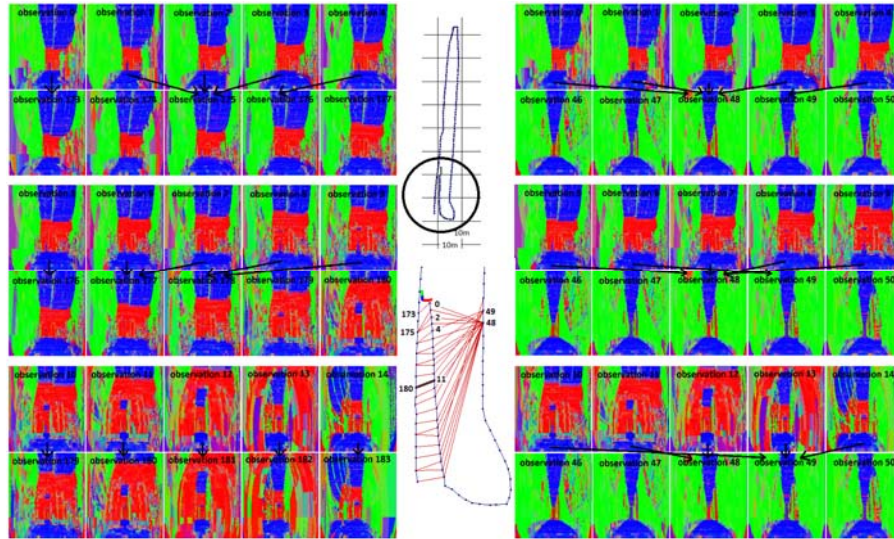$E_{d^A}(P_{d^A})$ - entropy computed using equation 22.

Figure 4. Loop closing with semantic images comparison based on entropy. Corresponding semantic images are connected via black arrows. Corresponding robot position are marked by red lines. Loop closing was found between robot observation 11 and 180, what is related with the minimum value of ICP error and maximum amount of corresponding points between 3D scans. Positive examples are shown on the left, negative example are shown on the right.

The entropy of the same image equals 0, therefore to find corresponding semantic images first we should minimize entropy. To demonstrate an approach figure 4 shows the loop closing procedure performed for data set shown on figure 7. The minimization of entropies is very fast (100ms per matching) but it does not guarantee loop closing, therefore further computation is

To conclude the discussion concerning the Iterative Closest Point method used for odometry correction, we show a result of an additional experiment on figure 7. The idea was to collect 3D data sets by the same robot (PIONEER 3AT equipped with 3DLSN unit and gyroscope odometry correction) two times in the same environment using different types of wheels (PIONEER 3AT indoor wheels and PIONEER 3AT outdoor wheels). The wheels have different radius, size and friction. The result is a longer odometry path for the indoor wheels (figure 7 C). We observed two important aspects of the applied ICP point to point method. First, the odometry error was decreased satisfactory in both cases. Second, there are some situations where the ICP accuracy can be decreased drastically, especially during rotations. Therefore, a proper strategy of data acquisition during robot motion has to be applied to avoid occlusions in the scan.
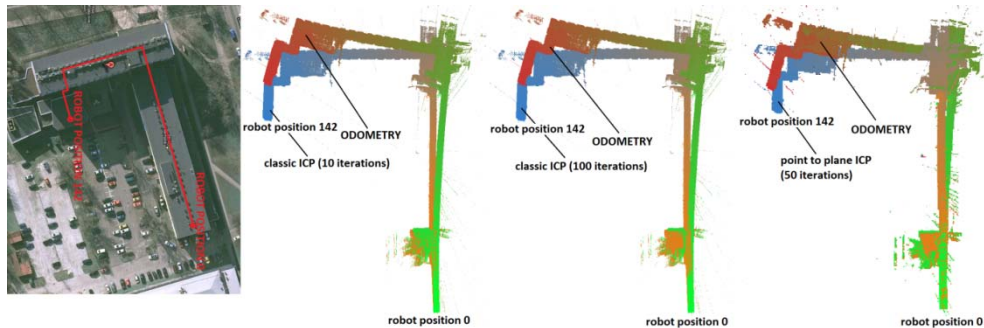

Figure 6. Comparison of ICP variants results. From left – indoor environment (Warsaw University of Technology, Faculty of Mechatronics), ICP point to point 10 iterations, ICP point to point 100 iterations, ICP point to plane 50 iterations.
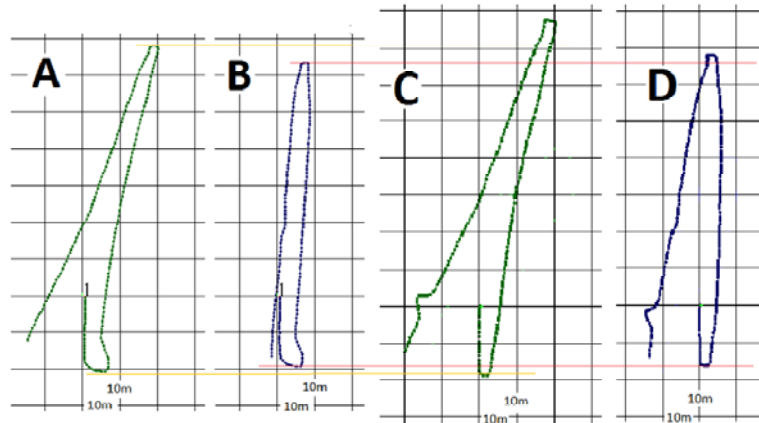

Figure 7. Comparison of ICP point to point (30 iterations) 10dometry correction for robot PIONEER 3AT equipped with 3DLSN unit and two different types of wheels (AB-OUTDOOR, CD-indoor). A-odometry path using OUTDOOR wheels, B-ICP result for A, C-odometry path using indoor wheels, D-ICP result for C. Experiment was performed in MECA laboratory in Royal Military Academy, Brussels, Belgium.

Conclusion

Compared to a state of the art method [10] where 60ms are needed to align two data sets of 320 x 240 data points, our implementation can process 361*498 data sets in 130ms for 30 iterations. Our main contribution was to propose a scalable method with an assumption of satisfying performance. Based on our best knowledge it will be very difficult to improve the performance while increasing amount of processed points because of the bottlenecks. For

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