Cheatography

CPSC221MT Cheat Sheet

by Phoenix (cddc) via cheatography.com/26246/cs/7303/

Logarithm Rules and Properties

			_
1.	log_	1 —	n
	IUg,	1 —	v

2.
$$\log_a a = 1$$

$$3. \quad \log_a x^y = y \log_a x$$

$$\mathbf{4.} \quad \log_a xy = \log_a x + \log_a y$$

$$5. \quad \log_a \frac{x}{y} = \log_a x - \log_a y$$

$$6. \quad a^{\log_b x} = x^{\log_b a}$$

7.
$$\log_a x = \frac{\log_b x}{\log_b a} = \log_a b \log_b x$$

Summations for Printing

Useful Formulae

Sum	Closed Form
$\sum_{k=0}^{n} ar^k; r \neq 0$	$\frac{ar^{n+1}-a}{r-1}; r \neq 1$
$\sum_{k=1}^{n} k$	$\frac{n(n+1)}{2}$
$\sum_{k=1}^{n} k^2$	$\frac{n(n+1)(2n+1)}{6}$
$\sum_{k=1}^{n} k^3$	$\frac{n^2(n+1)^2}{4}$
$\sum_{k=0}^{\infty} x^k; x < 1$	$\frac{1}{1-x}$
$\sum_{k=1}^{\infty} kx^{k-1}; x < 1$	$\frac{1}{(1-x)^2}$

Summation Rules

1.
$$\sum_{i=1}^{u} ca_i = c \sum_{i=1}^{u} a_i$$

2.
$$\sum_{i=1}^{u} (a_i \pm b_i) = \sum_{i=1}^{u} a_i \pm \sum_{i=1}^{u} b_i$$

3.
$$\sum_{i=l}^{u} a_i = \sum_{i=l}^{m} a_i + \sum_{i=m+1}^{u} a_i$$
, where $l \le m < u$

4.
$$\sum_{i=1}^{u} (a_i - a_{i-1}) = a_u - a_{l-1}$$

Don't panic



Starting from one end, ensure the sub-array

[0 1 2 3 7]

Selection sort - Algorithm

sorted in each pivot

[1 3]7 2 0

1 3 7 2 0	[0 1 2]3 7
[0]1 3 7 2	[0 1 2 3]7
[0 1]3 7 2	[0 1 2 3 7]

Starting from one end, ensure the sub-array sorted in each pivot

Bubble sort - Algorithm

13720	1 2(0 3)7
1 3(2 7)0	1(0 2)3 7
1 3 2(0 7)	(0 1)2 3 7
1(2 3)0 7	01237

Binary comparison and swap, shift each pivot by at most 1 position in an iteration

Sorting Complexities Algorithm Time Space Best Worst Worst **Bubble Sort** O(n) O(n^2) O(1) Insertion O(n) O(n^2) O(1) Sort Selection O(n^2) O(n^2) O(1) Sort Quicksort O(n O(n^2) O(log(n)) log(n)) Heapsort O(n O(n O(1) log(n)) log(n)) Mergesort O(n O(n O(n) log(n)) log(n))

Asymptotic Notations

Big-O

 $T(n) \in O(f(n))$ if there are constants c > 0 and n0such that $T(n) \le c f(n)$ for all $n \ge n0$

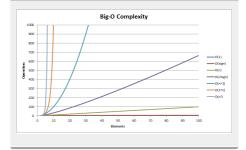
Big-Omega

 $T(n) \in \Omega(f(n))$ if $f(n) \in O(T(n))$

Big-Theta

 $T(n) \in \Theta(f(n)) \text{ if } T(n) \in O(f(n)) \text{ and } T(n) \in \\ \Omega(f(n))$

Big-O Complexity Chart





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Queue ADT

Queue property

FIFO: First In First Out

Core operations

- enqueue - dequeue - is_empty

Priority Queue ADT

Queue property

Lower Priority Value Out First

Core operations

- insert -deleteMin -isEmpty

Stack ADT

Stack property

LIFO: Last In First Out

Core operations

- push - pop - top - is_empty

d-Heap ADT

child $(i-1)^*d+2 \sim i^*d+1$ parent $\lfloor (i-2)/d \rfloor +1$ root 1
next free size+1

(Min) Heap Tree - ADT

Heap-order property

parent's key <= children's keys

Structure property

nearly complete tree

Heapify algorithm

Heapify the tree from bottom up, percolate DOWN a node as deep as needed for each node.

Binary Heap Operations Complexity:

Heapify - O(n)

Find Min - O(1)

Insert - O(log(n))

Delete - O(log(n))

Loop -> (Tail) Recursion

```
//Loop
int i = 0;
while (i < n)
    doFoo(i);
    i++;
//Recursion
void recDoFoo(int i, int n) {
    if (i < n) {
        doFoo(i);
        recDoFoo(i + 1, n);}
}
recDoFoo(0, n);</pre>
```

Equivalent for loop:

for (int i=0; i< n; i++) doFoo(i);

Tail Recursion -> Iteration

```
//Tail Recursion
int fact_acc (int n, int acc) {
  if (n)
    return fact_acc(n -1, acc *
  n);
  return acc;
}
//Iteration
int fact_acc (int n, int acc) {
  for(;n;n--)
    acc = acc * n;
return acc;
}
```

Recurrence Simplification Strategy

- 1) Find T(n) for the base cases.
- 2) Expand T(n) for the general patterns.
- 3) Drive the recursive term to the base case.
- 4) Solve and represent k with n by inequality(equality).
- 5) Substitute back to T(n).

```
e.g. T[n <= n0] = C1
T[n] = T[n/2] + C2
-> T[n] = T[n^*(1/2)] + C2
-> T[n] = T[n^*(1/2)^k] + k^*C2
Let n^*(1/2)^k <= n0 -> T(n^*(1/2)^k) = C1
-> n^*(1/2)^k * (2)^k <= n0^* (2)^k
```

- -> n/n0 <= (2)^k
- $-> \log_2(n/n_0) <= \log_2((2)^k)$
- -> log2(n/n0) <= k
- -> T[n] = C1+k*C2 = C1 + C2*log2(n/n0)

Summation Fomulas

```
1. \sum_{i=1}^{a} 1 = \underbrace{1 + 1 + \dots + 1}_{u + i + 1 \text{ in } u} = u - l + 1 \ (l, u \text{ are integer limits, } l \leq u); \quad \sum_{i=1}^{a} 1 = n
2. \sum_{i=1}^{a} 1 = 1 + 2 + \dots + n = \frac{n(u + 1)}{2} \approx \frac{1}{2} n^{2}
3. \sum_{i=1}^{a} i^{2} = 1^{2} + 2^{2} + \dots + n^{2} = \frac{n(u + 1)(2n + 1)}{6} \approx \frac{1}{3} n^{3}
4. \sum_{i=1}^{a} i^{4} = 1^{4} + 2^{4} + \dots + n^{4} \approx \frac{1}{4 + 1} i^{4} + 1
5. \sum_{i=0}^{a} a^{i} = 1 + a + \dots + a^{n} = \frac{a^{n+1} - 1}{a - 1} \ (a \neq 1); \quad \sum_{i=0}^{a} 2^{i} = 2^{n+1} - 1
6. \sum_{i=1}^{a} 12^{i} = 1 \cdot 2 + 2 \cdot 2^{2} + \dots + n2^{n} = (n - 1)2^{n+1} + 2
7. \sum_{i=1}^{a} \frac{1}{i} = 1 + \frac{1}{2} + \dots + \frac{1}{n} \approx \ln n + y, \text{ where } y \approx 0.5772 \dots \text{ (Euler's constant)}
8. \sum_{i=1}^{n} \lg i \approx n \lg n
```



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