

Information and Inference: A Journal of the IMA

Editors

**Robert Calderbank, David L. Donoho,
John Shawe-Taylor and Jared Tanner**

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