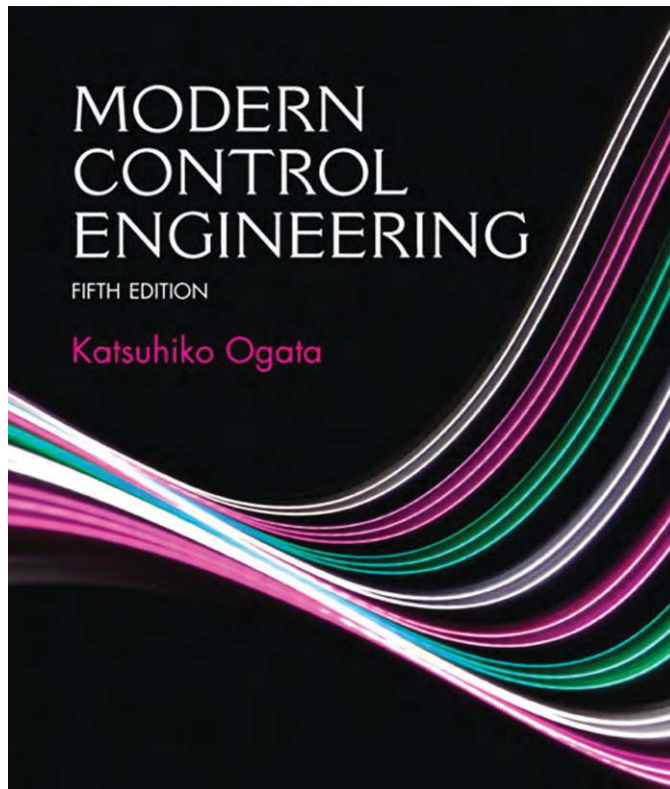


# MODERN CONTROL ENGINEERING

FIFTH EDITION

Katsuhiko Ogata



# Modern Control Engineering

*Fifth Edition*

**Katsuhiko Ogata**

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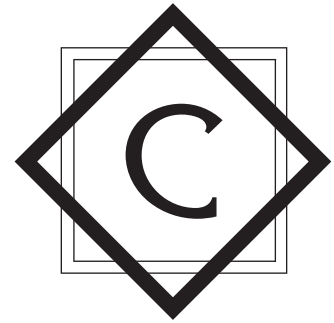
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