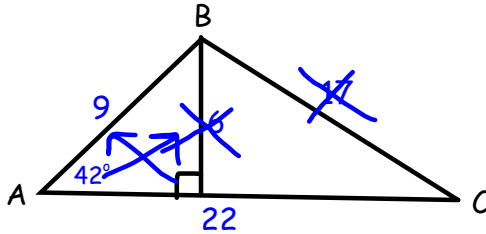


HW: Aim 62 Worksheet; Quiz Tuesday, 3/6 on Aims 61 - 66

Aim #62: How do we find the area of a triangle given the lengths of two adjacent sides and the included angle?

Kickoff: 

Find the area of triangle ABC. Hint: There is extra information!



$$\begin{aligned}
 A &= \frac{1}{2}bh \\
 &= \frac{1}{2}(22)(6) \\
 &= 66 \text{ sq. units}
 \end{aligned}$$

Sep 4-8:29 PM

1. Write the equation of a sine function that has the following characteristics.

a. Amplitude: 2 Period: π Phase Shift: $\frac{1}{2}$ to the right

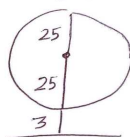
$$y = 2 \sin 2(x - \frac{1}{2})$$

2. Write the equation of a cosine function that has the following characteristics.

a. Amplitude: 3 Period: $\pi/2$ Phase Shift: 2 to the left

$$y = 3 \cos 4(x + 2)$$

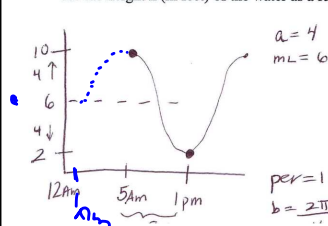
3. A Ferris Wheel with a radius of 25 feet is rotating at a rate of 3 revolutions per minute. When $t=0$, a chair starts at the lowest point on the wheel, which is 5 feet above the ground. Write a model for the height h , in feet, of the chair in terms of time t , in seconds.



$$y = -25 \cos \frac{\pi}{10} t + 30$$

$$\begin{aligned}
 3 \text{ rev} &\Rightarrow 60 \text{ sec} & b &= \frac{2\pi}{20} = \frac{\pi}{10} \\
 1 \text{ rev} &\Rightarrow 20 \text{ sec (per)}
 \end{aligned}$$

4. The height of the water in a bay varies sinusoidally over time. On a certain day off the coast of Maine, a high tide of 10 feet occurred at 5:00 A.M. and a low tide of 2 feet occurred at 1:00 P.M. Write a model for the height h (in feet) of the water as a function of time t (in hours since midnight).



$$a = 4$$

$$m = 6$$

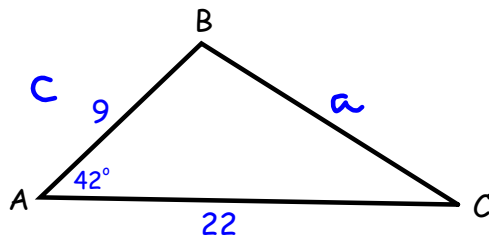
$$y = 4 \cos \frac{\pi}{8}(t - 5) + 6$$

$$\text{per} = 16 \text{ hrs}$$

$$b = \frac{2\pi}{16} = \frac{\pi}{8}$$

Feb 26-2:39 PM

What if we were only given this much information about the triangle?



$$K = \frac{1}{2} ab \sin C$$

$$K = \frac{1}{2} bc \sin A$$

$$K = \frac{1}{2} (22)(9) \sin 42$$

$$K = 66 \text{ sq. units}$$

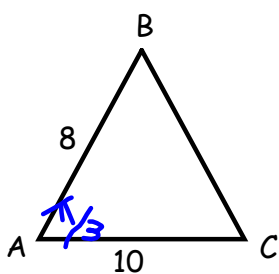
<https://www.youtube.com/watch?v=0bvr4DkKREM>



K
Area of a Triangle

Mar 6-5:13 PM

Try: In $\triangle ABC$, $b = 10$, $c = 8$ and angle $A = \pi/3$. Determine the exact value for the area of the triangle.



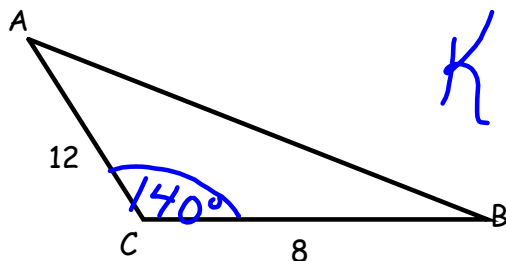
$$K = \frac{1}{2} bc \sin A$$

$$= \frac{1}{2} (10)(8) \sin \frac{\pi}{3}$$

$$= 20 \frac{\sqrt{3}}{2} = \boxed{20\sqrt{3}}$$

Mar 20-5:26 PM

Try: In $\triangle ABC$, $a = 8$, $b = 12$ and angle $C = 140^\circ$. Determine the area of the triangle to the nearest square unit.



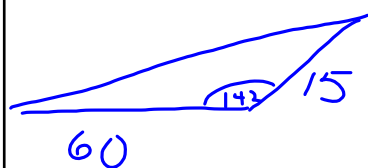
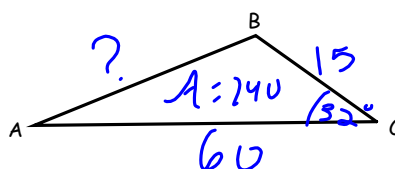
$$K = \frac{1}{2}ab \sin C$$

$$K = \frac{1}{2}(8)(12)\sin 140$$

$$= 31 \text{ Sq. units}$$

Mar 20-5:26 PM

eg. In $\triangle ABC$, $a = 15$ and $b = 60$. Find the measure of angle C to the nearest degree if the area is 240 square units.



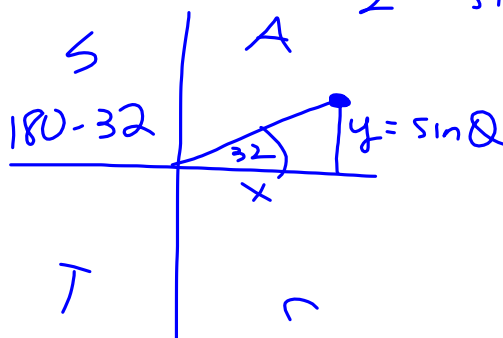
$$K = \frac{1}{2}ab \sin C$$

$$240 = \frac{1}{2}(15)(60) \sin C$$

$$\frac{240}{450} = \frac{450}{450} \sin C$$

$$\frac{8}{15} = \sin C$$

$$2^{\text{nd}} \sin(8/15) = 32^\circ$$



$$148^\circ$$

Mar 20-5:26 PM

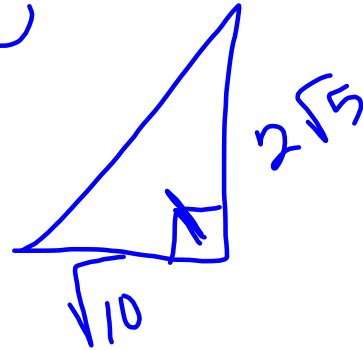
What is the maximum possible area of a triangle that has side lengths of $\sqrt{10}$ and $2\sqrt{5}$?

$$K = \frac{1}{2} (\sqrt{10})(2\sqrt{5}) \sin X$$

$$\frac{1}{2} (\sqrt{10})(2\sqrt{5})$$

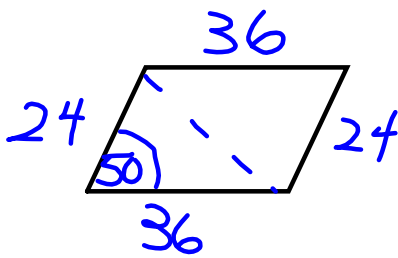
$$\sqrt{50}$$

$$5\sqrt{2}$$



Dec 6-8:23 AM

The lengths of two sides of a parallelogram are 24 and 36 centimeters. Their included angle measures 50° . Find the area of the parallelogram to the nearest ⁵⁰centimeter.



$$K = ab \sin C$$

$$= (24)(36) \sin 50$$

$$=$$

Answer

Feb 5-7:35 PM

In triangle ABC , the ratio of side AB to side AC is $1:2$ and angle $A = 30^\circ$. If the area of triangle ABC is 200 square feet, find the length of side AC to the nearest foot.

Dec 6-8:24 AM