

## Geometry 6-5 Rhombi and Squares

Another special parallelogram is the  (plural is ). A rhombus is a parallelogram in which all four sides are congruent.

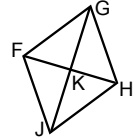
A rhombus is a parallelogram, so all of the properties from 6-2 apply. In addition, a rhombus has other properties.

**Theorem 6.15:** If a parallelogram is a rhombus, then its diagonals are perpendicular.

**Theorem 6.16:** If a parallelogram is a rhombus, then each diagonal bisects a pair of opposite angles.

The diagonals of rhombus FGHI intersect at K. Use the given information to find each value.

If  $FK = 5$  and  $FG = 13$ , find  $KJ$ .



If  $m\angle JF\hat{K} = 6y + 7$  and  $m\angle KFG = 9y - 5$ , find  $y$ .

You could say a  is a rhombus with four right angles. You could say a square is a rectangle with four congruent sides.

All of the properties of a rectangle from 6-4 and all of the properties of a rhombus from this lesson apply to a square.

Just like we did with rectangles, we have a few theorems that help us determine if our parallelogram is a rhombus or a square.

**Theorem 6.17:** If the diagonals of a parallelogram are perpendicular, then the parallelogram is a rhombus.

**Theorem 6.18:** If one diagonal of a parallelogram bisects a pair of opposite angles, then the parallelogram is a rhombus.

**Theorem 6.19:** If one pair of consecutive sides of a parallelogram are congruent, then the parallelogram is a rhombus.

**Theorem 6.20:** If a quadrilateral is both a rectangle and a rhombus, then it is a square.

Given  $J(5,0)$ ,  $K(8,-11)$ ,  $L(-3,-14)$ ,  $M(-6,-3)$ , determine whether parallelogram JKLM is a rhombus, rectangle, or square. List all that apply.