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# Hypercomplex Analysis and Applications

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Editors

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## Preface

This volume contains some papers written by the participants to the Session “Clifford and Quaternionic Analysis” of the 7th ISAAC Conference (hosted at the Imperial College, London, UK, July 2009). The session proved to be particularly lively, as it hosted more than 35 speakers, and showed how the topic of hypercomplex analysis is fertile. The contents of the contributions cover several different aspects of hypercomplex analysis, ranging from Clifford analysis on superspace to the study of Dirac operators on surfaces, Dunkl monogenic functions, and applications, for example, to operator theory. The contributions represent the most recent achievements in the area and have been refereed.

The editors are grateful to the contributors to this volume and to the referees, for their painstaking and careful work. The editors thank the Imperial College in London for hosting the Conference and Professor Michael Ruzhansky, President of the ISAAC and Chairman of the local organising committee.

August 2010, Irene Sabadini  
Frank Sommen