

Review

Laws of Logarithms & Exponents

Base a

Base e

$$a^{\log_a x} = x \qquad e^{\ln x} = x \qquad (1)$$

$$\log_a a^x = x \qquad \ln e^x = x \qquad (2)$$

$$\log_a(xy) = \log_a x + \log_a y \qquad \ln(xy) = \ln x + \ln y \qquad (3)$$

$$\log_a\left(\frac{x}{y}\right) = \log_a x - \log_a y \qquad \ln\left(\frac{x}{y}\right) = \ln x - \ln y \qquad (4)$$

$$\log_a x^r = r \log_a x \qquad \ln x^r = r \ln x \qquad (5)$$

$$\log_a a = 1 \qquad \ln e = 1 \qquad (6)$$

$$\log_a 1 = 0 \qquad \ln 1 = 0 \qquad (7)$$

$$a^{x+y} = a^x \cdot a^y \qquad e^{x+y} = e^x \cdot e^y \qquad (8)$$

$$a^{x-y} = \frac{a^x}{a^y} \qquad e^{x-y} = \frac{e^x}{e^y} \qquad (9)$$

$$(ab)^x = a^x b^x \qquad (3e)^x = 3^x e^x \qquad (10)$$

$$(a^x)^y = a^{xy} \qquad (e^x)^y = e^{xy} \qquad (11)$$

$$a^0 = 1 \qquad e^0 = 1 \qquad (12)$$