

Remember The sum of the interior angles of ALL quadrilaterals adds up to 360° .

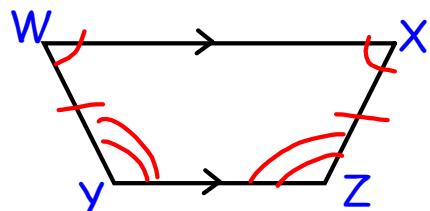
Same side interior angles add up to 180° .

Pythagorean Theorem is $a^2 + b^2 = c^2$ → hypotenuse

(Sides) Definition of a trapezoid: quadrilateral w/
1 pair of // sides

Jan 13-10:01 AM

ISO trap



Legs: $\overline{WY}, \overline{XZ}$

// Bases: $\overline{WX}, \overline{YZ}$

Base angles: $\angle Y \cong \angle Z$

Base angles: $\angle W \cong \angle X$

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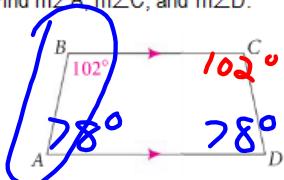
Theorem 6 -15

The base angles of an isosceles trapezoid are congruent

Jan 12-8:43 PM

Target 1: Find the measures of the angles of an isosceles trapezoid.

- a. ABCD is an isosceles trapezoid and $m\angle B = 102^\circ$.
Find $m\angle A$, $m\angle C$, and $m\angle D$.



- b. PQRS is an isosceles trapezoid with $m\angle S = 70^\circ$.
Find the $m\angle P$, $m\angle Q$, $m\angle R$.



$$m\angle P = 110$$

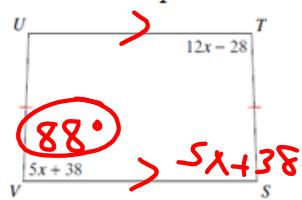
$$m\angle Q = 110$$

$$m\angle R = 70$$

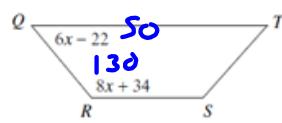
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Target 1: Find the measures of the angles of an isosceles trapezoid.

c. Find $m\angle V$ in trapezoid STUV.



d. Find $m\angle R$ in trapezoid QRST.



$$5x + 38 + 12x - 28 = 180$$

$$\begin{aligned} 17x + 10 &= 180 \\ -10 &\quad -10 \end{aligned}$$

$$\begin{array}{c} 17x = 170 \\ \hline 17 \quad 17 \end{array}$$

$$x = 10$$

This is one angle from each base... that means they're supplementary.

Add them together and set them equal to 180.

$$6x - 22 + 8x + 34 = 180$$

$$14x + 12 = 180$$

$$14x = 168$$

$$x = 12$$

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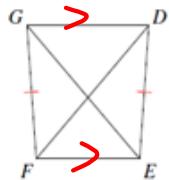
Theorem 6 -16

The diagonals of an isosceles trapezoid are congruent.

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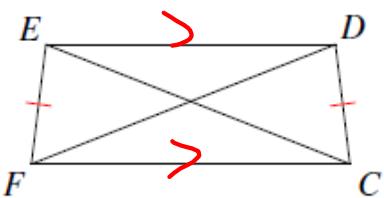
Target 2: Find the measures of the diagonals of an isosceles trapezoid.

- a. DEF_G is a trapezoid. Find EG if DF is 12.



$$\text{EG} = 12$$

- b. CDEF is a trapezoid. Find x if EC = 20 and FD = 5x - 10.



$$\begin{aligned} 5x - 10 &= 20 \\ +10 & \quad +10 \end{aligned}$$

$$5x = 30$$

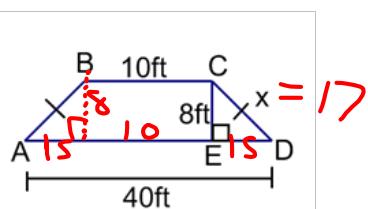
$$\textcircled{x=6}$$

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Not a theorem, but still useful

You can turn an isosceles trapezoid into two congruent right triangles and a rectangle.

$$\begin{array}{r} 40 \\ -10 \\ \hline 30 \end{array}$$



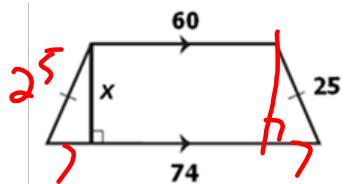
$$8^2 + 15^2 = x^2$$

$$64 + 225 = x^2$$

$$\sqrt{289} = x^2$$

$$\textcircled{x=17}$$

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$$\begin{array}{r} 74 \\ - 60 \\ \hline 14 \end{array}$$

$$7^2 + x^2 = 25^2$$

$$49 + x^2 = 625$$

$$x^2 = 576$$

$$x = 24$$

Jan 10-11:48 AM

Trapezoid Midsegment Theorem

(1) The midsegment of the trapezoid is parallel to the bases.

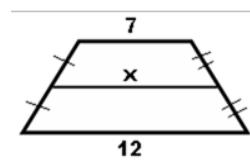
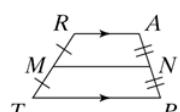
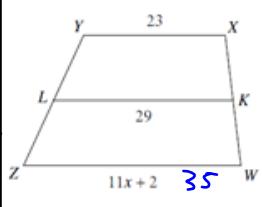
(2) The length of the midsegment of the trapezoid is half the sum of the lengths of the bases.

$$MN \parallel RA, \quad MN \parallel TP$$

$$MN = \frac{1}{2}(RA + TP)$$

$$2MN = RA + TP$$

EXAMPLE: Find x.



$$x = 9.5$$

$$2(29) = 11x + 2 + 23$$

$$\begin{array}{r} 58 = 11x + 25 \\ -25 \quad -25 \\ \hline 33 = 11x \\ 11 \quad 11 \\ \hline x = 3 \end{array}$$

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