

7.4 Double and Half Angle Identities

Double Angle Formulas

Half Angle formulas

$\sin 2\theta = 2\sin \theta \cos \theta$	$\sin (\theta/2) = \pm \sqrt{\frac{1 - \cos \theta}{2}}$
$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$	$\cos (\theta/2) = \pm \sqrt{\frac{1 + \cos \theta}{2}}$
$\cos 2\theta = 2\cos^2 \theta - 1$	$\tan (\theta/2) = \pm \sqrt{\frac{1 - \cos \theta}{1 + \cos \theta}}, \cos \theta \neq -1$
$\cos 2\theta = 1 - 2\sin^2 \theta$	
$\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$	

Example 1: If $\sin \theta = (1/4)$ and θ has its terminal side in the first quadrant, find the exact value of $\sin 2\theta$.

Example 2: Use a half-angle identity to find the exact value of $\sin (\pi/12)$.